# HIGGS BOSON DECAYS INTO A PAIR OF SUPERSYMMETRIC PARTICLES 

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#### Abstract

Within the framework of the Minimal Supersymmetric Standard Model, the $H, h, A$ and $H^{ \pm}$Higgs bosons decay channels into a pair of supersymmetric particles were studied: into a pair of chargino $H(h ; A) \Rightarrow \chi_{i}^{-} \chi_{j}^{+}$; a pair of neutralino $H(h ; A) \Rightarrow \chi_{i}^{0} \chi_{j}^{0}$; in a pair of chargino - neutralino $\mathrm{H}^{ \pm} \Rightarrow \chi_{i}^{ \pm} \chi_{j}^{0}$; into a pair of scalar fermions $H(h ; A) \Rightarrow \tilde{f}_{i} \bar{f}_{j}, \mathrm{H}^{ \pm} \Rightarrow \tilde{f}_{i} \overline{\tilde{f}}_{j}^{\prime}$. Analytical expressions for these decays widths are obtained, the degree of longitudinal polarizations of the chargino and neutralino and the dependence of the decay width on the Higgs boson mass are studied in detail.


Keywords: Standard Model, Minimal Supersymmetric Standard Model, Higgs boson, chargino, neutralino, decay width, sfermion.
PACS: $14.80 \mathrm{Da}, 14.80 \mathrm{Ly}, 14.80 \mathrm{Nb}$.

## 1. INTRODUCTION

The discovery of the Higgs boson $H_{S M}$ with characteristics corresponding to the predictions of the Standard Model (SM) was carried out by the ATLAS and CMS collaborations in the Large Hadron Collider (LHC) in 2012 [1,2] (see also reviews [3-5]). With the discovery of the Higgs boson, a missing brick was found in the SM building and the mechanism for generating masses of fundamental particles, the mechanism of spontaneous breaking of the Braut -Englert-Higgs symmetry, was experimentally confirmed [6,7]. It should be noted that the path to the discovery of the Higgs boson was a long one; at the same time, much work began on its determination of the physical characteristics of this particle.

According to the SM, there are six leptons and six quarks, each comprising three families. The carriers of strong, electromagnetic, and weak interactions are gluons, a photon, charged $W^{ \pm}$and neutral $Z$ - bosons. Now they are supplemented by the fourth Yukawa interaction carried by Higgs boson $H_{S M}$.
$S M$ allows you to accurately calculate the Feynman diagrams of various processes and compare with the corresponding experimental data. The agreement between the $S M$ and the experience is strikingly good. Nevertheless, SM has its own difficulties. Many of them are connected with the fact that this model describes a lot, but is not able to explain where it came from, does not allow it to be deduced from deeper principles.

One of the difficulties of $S M$ is related to the problem of hierarchy. According to quantum field theory, vacuum is not an absolute void, but a sea of virtual particles. All real particles of our world are particles dressed in a virtual fur coat. Masses, charges and other characteristics of the observed particles are the characteristics of particles dressed in a fur coat. Theorists take this phenomenon into account using a mathematical procedure called renormalization. The fact is that renormalization works well for all particles, but in the case of the Higgs boson, a problem arises: the influence of virtual particles on the Higgs boson mass is too strong, as a result, the boson mass increases trillions of times, and such a particle can no longer play
the role of the Higgs boson. This difficulty is called the hierarchy problem. This way out of this situation is possible. If in nature there are some other particles that do not exist in the SM, then in a virtual form they can compensate for the influence of the boson on the Higgs mass. The most important thing here is that in supersymmetric theories such compensation itself arises from the construction of the theory. It is such a supersymmetric theory that most attracts theorists.

Another important difficulty of $S M$ is the lack of dark matter particles in it. In astrophysics, it is believed that in the Universe, in addition to ordinary matter in the form of stars, black holes, planets, gas and dust clouds, and. etc., there are particles of a completely different nature. These are particles of dark matter, we do not see them, they practically do not interact with ordinary matter and radiation. Possible candidates for dark matter particles may be neutralino, sneytrino, gluino, gravitino, the existence of which is assumed in the Minimum Supersymmetric Standard Model (MSSM) [8-11].

Unlike the $S M$, the $M S S M$ introduces two doublets of the scalar field with hypercharges -1 and +1 :

$$
\varphi_{1}=\binom{H_{1}^{0}}{H_{1}^{-}}, \quad \varphi_{2}=\binom{H_{2}^{+}}{H_{2}^{0}}
$$

To obtain the physical fields of Higgs bosons, $\varphi_{1}$ and $\varphi_{2}$ we represent in the form

$$
\begin{aligned}
\varphi_{1} & =\frac{1}{\sqrt{2}}\binom{v_{1}+H_{1}^{0}+i P_{1}^{0}}{H_{1}^{-}} \\
\varphi_{2} & =\frac{1}{\sqrt{2}}\binom{H_{2}^{+}}{v_{2}+H_{2}^{0}+i P_{2}^{0}}
\end{aligned}
$$

where $H_{1}^{0}, P_{1}^{0}, H_{2}^{0}$ and $P_{2}^{0}$ are the fields describing the excitations of the system relative to vacuum states $\left\langle\varphi_{1}\right\rangle=\frac{1}{\sqrt{2}} v_{1}$ and $\left\langle\varphi_{2}\right\rangle=\frac{1}{\sqrt{2}} v_{2}$.

The $C P$-even Higgs bosons $H$ and $h$ are obtained by mixing the fields $H_{1}^{0}$ and $H_{2}^{0}$ (mixing angle $\alpha$ ):

$$
\binom{H}{h}=\left(\begin{array}{cc}
\cos \alpha & \sin \alpha \\
-\sin \alpha & \cos \alpha
\end{array}\right)\binom{H_{1}^{0}}{H_{2}^{0}}
$$

Similarly, mixing $P_{1}^{0}$ and $P_{2}^{0}$, as well as $H_{1}^{ \pm}$and $H_{2}^{ \pm}$, one obtains Goldstone bosons $G^{0}$ and $G^{ \pm}, C P$ an odd Higgs boson $A$ and charged Higgs bosons $H^{ \pm}$ (mixing angle $\beta$ ):

$$
\begin{aligned}
& \binom{G^{0}}{A}=\left(\begin{array}{cc}
\cos \beta & \sin \beta \\
-\sin \beta & \cos \beta
\end{array}\right)\binom{P_{1}^{0}}{P_{2}^{0}} \\
& \binom{G^{ \pm}}{H^{ \pm}}=\left(\begin{array}{cc}
\cos \beta & \sin \beta \\
-\sin \beta & \cos \beta
\end{array}\right)\binom{H_{1}^{ \pm}}{H_{2}^{ \pm}}
\end{aligned}
$$

Thus, there are five Higgs bosons in the MSSM: CP even $H$ and $h$ - bosons, $C P$-odd $A$-boson, charged $H^{ \pm}$bosons.

The Higgs sector of the MSSM is characterized by six parameters $M_{H}, M_{h}, M_{A}, M_{H^{ \pm}}, \alpha$ and $\beta$. Of these, the parameters $M_{A}$ and $\tan \beta=\frac{v_{1}}{v_{2}}$ are free. The parameter $\tan \beta$ varies within

$$
1 \leq \tan \beta \leq \frac{m_{t}}{m_{b}}=35.5
$$

here $m_{t}=173.2 \mathrm{GeV}$ and $m_{b}=4.88 \mathrm{GeV}$ of masses of $t$ - and $b$ - quarks.

The Higgs masses of the $H$ - and $h-\left(H^{ \pm}-\right)$bosons are expressed by the masses $M_{A}$ and $M_{Z}\left(M_{A}\right.$ and $\left.M_{W}\right)$ :

$$
\begin{gathered}
M_{H(h)}^{2}=\frac{1}{2}\left[M_{A}^{2}+M_{Z}^{2} \pm \sqrt{\left(M_{A}^{2}+M_{Z}^{2}\right)^{2}-4 M_{A}^{2} M_{Z}^{2} \cos ^{2} 2 \beta}\right] \\
M_{H^{ \pm}}^{2}=M_{A}^{2}+M_{W}^{2}
\end{gathered}
$$

Higgs bosons $\boldsymbol{H}, \boldsymbol{h}, \boldsymbol{A}$ and $\boldsymbol{H}^{ \pm}$can decay through different channels (see [8, 11-18] and references in them to primary sources. Along with decays of these bosons into ordinary particles, their decay into supersymmetric ones is also possible (SUSY) particles:

Chargino, neutralino, and scalar fermions (sfermions) are such particles. The present work is devoted to the study of the decay channels of the Higgs bosons $\boldsymbol{H}, \boldsymbol{h}$ and $\boldsymbol{A}$ into a pair of chargino

$$
\begin{array}{cl}
H(h ; A) \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}, & (i, j=1,2), \\
H(h ; A) \Rightarrow \tilde{\chi}_{i}^{0}+\tilde{\chi}_{j}^{0}, & (i, j=1 \div 4) \\
H^{ \pm} \Rightarrow \tilde{\chi}_{i}^{ \pm}+\tilde{\chi}_{j}^{0}, & (i=1,2, j= \\
H(h ; A) \Rightarrow \tilde{f}_{i}+\overline{\tilde{f}}_{j}, & (i, j=1,2) \\
H^{ \pm} \Rightarrow \tilde{f}_{i}+\overline{\tilde{f}}_{j}^{\prime}, & (i, j=1,2)
\end{array}
$$

Within the framework of the MSSM and taking into account the polarization states of the chargino, analytical expressions for the width of the indicated decays are obtained, the degrees of the longitudinal and transverse polarizations of the chargino are determined, the dependence of these characteristics and the width of the decays on the mass of Higgs bosons is studied.

## 2. HIGGS BOSON DECAYS IN A PAIR OF CHARGINO

The supersymmetric partnyors of the gauge $W^{ \pm}$ and Higgs $H^{ \pm}$- bosons are calibrino (vino) $\widetilde{W}^{ \pm}$and Higgsino $\widetilde{H}^{ \pm}$. The mass matrix of these spinor fields is off-diagonal, which leads to their mixing. Chargino $\tilde{\chi}^{ \pm}$ is a four-component. Dirac fermion that occurs when vino $\widetilde{W}^{ \pm}$and Higgsino $\widetilde{H}^{ \pm}$are mixed. The masses and coupling constants of the chargino with the Higgs bosons $H, h, A, H^{ \pm}$are determined by the mass matrix.

$$
M_{\tilde{\chi}^{ \pm}}=\left(\begin{array}{cc}
M_{2} & \sqrt{2} M_{W} \sin \beta \\
\sqrt{2} M_{W} \cos \beta & \mu
\end{array}\right)
$$

where $M_{2}$ and $\mu$ - mass parameters of vino and Higgsino. This matrix is diagonalized by two real two-
row $U$ and $V$ matrices.

$$
\begin{gathered}
U M_{\tilde{\chi}^{ \pm}} V^{-1} \Rightarrow U=R_{-} \text {and } \\
V=\left\{\begin{array}{cc}
R_{+}, & \text {if } \operatorname{det} M_{\tilde{\chi}^{ \pm}}>0 \\
\sigma_{3} R_{+}, & \text {if } \operatorname{det} M_{\tilde{\chi}^{ \pm}}<0,
\end{array}\right.
\end{gathered}
$$

where $\sigma_{3}$ is the Pauli matrix, which makes the chargino mass positive, $R_{ \pm}$are the rotation matrices with angles $\theta_{ \pm}$:

$$
R_{ \pm}=\left(\begin{array}{cc}
\cos \theta_{ \pm} & \sin \theta_{ \pm} \\
-\sin \theta_{ \pm} & \cos \theta_{ \pm}
\end{array}\right)
$$

and the angles $\theta_{+}$and $\theta_{-}$are defined as

$$
\begin{aligned}
\tan 2 \theta_{+} & =\frac{2 \sqrt{2} M_{W}\left(M_{2} \sin \beta+\mu \cos \beta\right)}{M_{2}^{2}-\mu^{2}+2 M_{W}^{2} \cos \beta} \\
\tan 2 \theta_{-} & =\frac{2 \sqrt{2} M_{W}\left(M_{2} \cos \beta+\mu \sin \beta\right)}{M_{2}^{2}-\mu^{2}-2 M_{W}^{2} \cos \beta}
\end{aligned}
$$

After diagonalizing the matrix $M_{\tilde{\chi}^{ \pm}}$, new states of chargeino with masses are obtained:

$$
\begin{align*}
m_{\tilde{\chi}_{1,2}^{ \pm}}^{2} & =\frac{1}{2}\left\{M_{2}^{2}+\mu^{2}+2 M_{W}^{2} \mp\left[\left(M_{2}^{2}+\mu^{2}\right)^{2}+4 M_{W}^{2}\left(M_{W}^{2} \cos ^{2} 2 \beta+M_{2}^{2}+\mu^{2}+\right.\right.\right. \\
& \left.\left.\left.+2 M_{2} \mu \sin 2 \beta\right)\right]^{1 / 2}\right\} \tag{6}
\end{align*}
$$

If one of the two parameters $\mu$ or $M_{2}$ has a very large value, then one state of the chargino corresponds to the calibrino state and the other to the Higgsino state. In this case, the masses of the chargino are equal: at

$$
|\mu| \gg M_{Z}, \quad M_{2} \sim M_{Z}: m_{\tilde{\chi}_{1}^{ \pm}} \sim M_{2}, \quad m_{\tilde{\chi}_{2}^{ \pm}} \sim|\mu| ;
$$

at

$$
|\mu| \sim M_{Z}, \quad M_{2} \gg M_{Z}: m_{\tilde{\chi}_{1}^{ \pm}} \sim|\mu|, \quad m_{\tilde{\chi}_{2}^{ \pm}} \sim M_{2} .
$$

Figure 1 shows the dependence of the chargino mass $\tilde{\chi}_{1}^{ \pm}$and $\tilde{\chi}_{2}^{ \pm}$on the parameter $\mu$ at $\tan \beta=30$ and the fixed mass $M_{2}=150 \mathrm{GeV}$. As can be seen, with an increase in the moduls of the parameter $|\mu|$ the mass of light (heavy) chargino $m_{\tilde{\chi}_{1}^{ \pm}}\left(m_{\tilde{\chi}_{2}^{ \pm}}\right)$monotonously increases and approaches the value of 147 GeV
( 512 GeV ) at $\mu=-500 \mathrm{GeV}$ and $145 \mathrm{GeV}(514 \mathrm{GeV})$ at $\mu=500 \mathrm{GeV}$. The minimum value of the chargino mass $m_{\tilde{\chi}_{1}^{ \pm}}$and $m_{\tilde{\chi}_{2}^{ \pm}}$is observed at a zero value of the
parameter $\mu: \quad m_{\tilde{\chi}_{1}^{ \pm}}(\mu=0)=2,696 \mathrm{GeV}$,

$$
m_{\tilde{\chi}_{2}^{ \pm}}(\mu=0)=188.192 \mathrm{GeV}
$$



Fig. 1. Chargino masses $m_{\tilde{\chi}_{ \pm}^{ \pm}}$and $m_{\tilde{\chi}_{2}^{ \pm}}$as a function of the parameter $\mu$


Fig. 2. Dependence of the mass $m_{\tilde{\chi}_{1}^{ \pm}}$(a) and $m_{\tilde{\chi}_{2}^{ \pm}}$(b) on the parameter $\tan \beta$

Note that, for a given parameter $\mu$, the chargino masses $m_{\tilde{\chi}_{1}^{ \pm}}$and $m_{\tilde{\chi}_{2}^{ \pm}}$are very sensitive to the $\tan \beta$ parameter (see fig. 2 , where the dependence of the mass $m_{\tilde{\chi}_{1}^{ \pm}}$and $m_{\tilde{\chi}_{2}^{ \pm}}$of the $\tan \beta$ parameter for $M_{2}=150 \mathrm{GeV}, \mu=$ -200 GeV ). As can be seen from the figure, with an increase in the parameter $\tan \beta$, the chargino mass $m_{\tilde{\chi}_{1}^{ \pm}}$monotonously decreases, and the charge chargino $m_{\tilde{\chi}_{\frac{1}{2}}^{ \pm}}$on the contrary, increases monotonously. With a positive value of the parameter $\mu=200 \mathrm{GeV}$, an inverse relationship is observed: with an increase in the $\tan \beta$ parameter, the chargino mass $m_{\tilde{\chi}_{1}^{ \pm}}$increases and the mass $m_{\tilde{\chi}_{2}^{ \pm}}$on the contrary, decreases.

The Feynman diagram of the Higgs boson decay $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$is shown in fig. 3 (the $k=1,2,3$ index corresponds to the neutral Higgs bosons $H, h, A$ and the $i, j=1,2$ indexes correspond to the chargino).


Fig. 3. Feynman diagram for $H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}$decay. In the figure $p, p_{1}$ and $p_{2}$ denote 4 -momenta of Higgs boson $H_{k} \tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$chargino, $s_{1}$ and $s_{2}$ 4 - polarization vectors of chargino.

According to the MSSM, the amplitude corresponding to the diagram in fig. 3 can be written in the following form:

$$
\begin{equation*}
M\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)=i g\left[g_{i j k}^{L} \bar{u}\left(p_{1}, s_{1}\right) P_{L} v\left(p_{2}, s_{2}\right)+g_{i j k}^{R} \bar{u}\left(p_{1}, s_{1}\right) P_{R} v\left(p_{2}, s_{2}\right)\right] \tag{7}
\end{equation*}
$$

where $g$ is a constant determining the mass of the gauge $W$ - boson

$$
M_{W}^{2}=\frac{1}{2} g^{2}\left(v_{1}^{2}+v_{2}^{2}\right)
$$

$P_{L, R}=\frac{\left(1 \pm \gamma_{5}\right)}{2}$ is chirality matrices, $g_{i j k}^{L}$ and $g_{i j k}^{R}$ is interaction constants of the Higgs boson $H_{k}$ with chargino $\tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}[8,11]$

$$
\begin{gather*}
g_{i j k}^{L}=\frac{1}{\sqrt{2}}\left[V_{j 1} U_{i 2} e_{k}-V_{j 2} U_{i 1} d_{k}\right] \\
g_{i j k}^{R}=\frac{1}{\sqrt{2}}\left[V_{i 1} U_{j 2} e_{k}-V_{i 2} U_{j 1} d_{k}\right] \epsilon_{k} \tag{8}
\end{gather*}
$$

$\epsilon_{1}=\epsilon_{2}=-\epsilon_{3}=1$; the coefficients $e_{k}$ and $d_{k}$ are equal to:

$$
\begin{align*}
e_{1} & =\cos \alpha, e_{2}=-\sin \alpha, e_{3}=-\sin \beta \\
d_{1} & =-\sin \alpha, d_{2}=-\cos \alpha, d_{3}=\cos \beta \tag{9}
\end{align*}
$$

To find the probabilities (width) of the Higgs boson decay into a pair of chargino, we must squared the amplitude moduls $\left|M\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)\right|^{2}$. In the standard way for the squared amplitude module, we find:

$$
\begin{align*}
& \left|M\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)\right|^{2}=\frac{g^{2}}{2}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left[\left(p_{1} \cdot p_{2}\right)+m_{\tilde{\chi}_{i}} m_{\tilde{\chi}_{j}}\left(s_{1} \cdot s_{2}\right)\right]+\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \times\right. \\
& \left.\times\left[m_{\widetilde{\chi}_{i}}\left(p_{2} \cdot s_{1}\right)+m_{\tilde{\chi}_{j}}\left(p_{1} \cdot s_{2}\right)\right]+2 g_{i j k}^{L} g_{i j k}^{R}\left[-m_{\widetilde{\chi}_{i}^{-}} m_{\tilde{\chi}_{j}^{+}}-\left(p_{1} \cdot p_{2}\right)\left(s_{1} \cdot s_{2}\right)+\left(p_{1} \cdot s_{2}\right)\left(p_{2} \cdot s_{1}\right)\right]\right\} . \tag{10}
\end{align*}
$$

In the Higgs boson rest system $H_{k}$ the energy and the modules of the three-dimensional chargino momentum are determined by the expressions:

$$
\begin{aligned}
& E_{1}=\frac{1}{2} M_{H}\left(1+r_{i}-r_{j}\right), \quad E_{2}=\frac{1}{2} M_{H}\left(1-r_{i}+r_{j}\right) \\
& \left|\vec{p}_{1}\right|=\left|\vec{p}_{2}\right|=|\vec{p}|=\frac{1}{2} M_{H} \sqrt{\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}}
\end{aligned}
$$

here the notation

$$
r_{i}=\left(\frac{m_{\chi_{i}^{ \pm}}}{M_{H_{k}}}\right)^{2}, r_{j}=\left(\frac{m_{\chi_{j}^{ \pm}}}{M_{H_{k}}}\right)^{2}
$$

Given the polarization states of the chargino $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$, the decay width $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$has the form:

$$
\begin{align*}
& \frac{d \Gamma\left(\vec{\xi}_{1}, \vec{\xi}_{2}\right)}{d \Omega}=\frac{G_{F} M_{W}^{2}}{32 \sqrt{2} \pi^{2}} M_{H_{k}} \sqrt{\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}}\left\{[ ( g _ { i j k } ^ { L } ) ^ { 2 } + ( g _ { i j k } ^ { R } ) ^ { 2 } ] \left[\left(1-r_{i}-r_{j}\right)\left(1-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)+\right.\right. \\
& \left.+2 \sqrt{r_{i} r_{j}} \times\left(-\left(\vec{\xi}_{1} \vec{\xi}_{2}\right)+\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)\right]+\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}}\left[\left(\vec{n} \vec{\xi}_{1}\right)-\right. \\
& \left.\left.-\left(\vec{n} \vec{\xi}_{2}\right)\right]-4 g_{i j k}^{L} g_{i j k}^{R} \times\left[\sqrt{r_{i} r_{j}}\left(1-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)-\frac{1}{2}\left(1-r_{i}-r_{j}\right)\left(\left(\vec{\xi}_{1} \vec{\xi}_{2}\right)-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)\right]\right\} \tag{11}
\end{align*}
$$

where $\vec{n}$ is the unit vector, in the direction of the charge of the chargino $\tilde{\chi}_{i}^{-}, \vec{\xi}_{1}$ and $\vec{\xi}_{2}$ are the unit vectors characterizing the polarization of the chargino $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$in the rest systems of each of these particles, respectively; $\quad \lambda\left(r_{i}, r_{j}\right)=\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}$ is the kinematic function of a two-particle phase volume.

We consider particular cases of the decay width formula (9). First, suppose that the chargino is

$$
\vec{\xi}_{1}=\vec{n} \lambda_{1}, \vec{\xi}_{2}=-\vec{n} \lambda_{2},
$$

where $\lambda_{1}$ and $\lambda_{2}$ are the spiralities of the chargino $\tilde{\chi}_{i}^{-}$ and $\tilde{\chi}_{j}^{+}$

In this case, the decay width $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$is determined by the expression: polarized longitudinally, while

$$
\begin{equation*}
\Gamma\left(\lambda_{1}, \lambda_{2}\right)=\frac{1}{4} \Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)\left[1+\lambda_{1} \lambda_{2}+\left(\lambda_{1}+\lambda_{2}\right) P\right], \tag{12}
\end{equation*}
$$

here
$\Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)=\frac{G_{F} M_{W}^{2}}{2 \sqrt{2} \pi} M_{H_{k}} \sqrt{\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-\right.$
$\left.4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}\right\}$
is the decay width in the case of unpolarized chargino, and $P$ is the degree of longitudinal polarization of chargino, defined by the formula

$$
\begin{equation*}
P=\frac{\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{\left(1-r_{i}-r_{j}\right)^{2}-4 r_{i} r_{j}}}{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}} . \tag{14}
\end{equation*}
$$

It follows from the decay width (12) that, in the Higgs boson decay $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$the chargino $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$must have the same $\lambda_{1}=\lambda_{2}= \pm 1$ helicities $\left(\tilde{\chi}_{i R}^{-} \tilde{\chi}_{j R}^{+}\right.$or $\left.\tilde{\chi}_{i L}^{-} \tilde{\chi}_{j L}^{+}\right)$. This is a consequence of maintaining the full moment in $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$decays. Consider this decay in the resting system of the Higgs boson $H_{k}$. In this system, the momenta of the chargino $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$are equal in magnitude and opposite in
direction (see fig. 4, which shows the directions of the charge and spin of the chargino). Since the Higgs boson $H_{k}$ is zero, the process $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$is allowed only if the chargino $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}$are in the same helicity state. It is in this case that the projection of the total moment of two chargino in the direction of movement of chargino $\tilde{\chi}_{i}^{-}$(or $\tilde{\chi}_{j}^{+}$) is zero.


Fig. 4. Direction of momenta and spins in $H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}$decay

We estimate the degree of longitudinal polarization of chargino (12) at $\tan \beta=1$. Calculations show that, at this value of the parameter $\tan \beta$, the interaction constants $g_{i j k}^{L}$ and $g_{i j k}^{R}$ are equal to each other in the decays $H(h ; A) \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$, as a result of which the degree of longitudinal polarization of the chargino vanishes.

Now consider the case when the charginos are transversely polarized. Where in

$$
\left(\vec{n} \vec{\xi}_{1}\right)=\left(\vec{n} \vec{\eta}_{1}\right)=0,\left(\vec{n} \vec{\xi}_{2}\right)=\left(\vec{n} \vec{\eta}_{2}\right)=0
$$

$$
\left(\vec{\xi}_{1} \vec{\xi}_{2}\right)=\left(\vec{\eta}_{1} \vec{\eta}_{2}\right)=\eta_{1} \eta_{2} \cos \varphi
$$

where $\vec{\eta}_{1}$ and $\vec{\eta}_{2}$ are the transverse components of the chargino vectors $\tilde{\chi}_{i}^{-}$and $\tilde{\chi}_{j}^{+}, \varphi$ is the angle between these vectors. In this case, the decay width $H_{k} \Rightarrow$ $\tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$is
$\frac{d \Gamma\left(\eta_{1} \eta_{2}\right)}{d \Omega}=\frac{1}{4} \frac{d \Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{+}\right)}{d \Omega}\left[1+\eta_{1} \eta_{2} P_{\perp}\right]$,
where

$$
\begin{align*}
& \quad \frac{d \Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i} \tilde{\chi}_{j}^{+}\right)}{d \Omega}=\frac{G_{F} M_{W}^{2}}{8 \sqrt{2} \pi^{2}} M_{H_{k}} \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-\right. \\
& 4 g_{i j k}^{L} g_{\left.i j k \sqrt{R} \sqrt{r_{i} r_{j}}\right\}}^{\text {(16) }} \tag{16}
\end{align*}
$$

is the decay width for unpolarized chargino, and $P_{\perp}$ is the degree of transverse polarization of chargino :

$$
\begin{equation*}
P_{\perp}=\frac{2 g_{i j k}^{L} g_{i j k}^{R}\left(1-r_{i}-r_{j}\right)-2\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{r_{i} r_{j}}}{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}} \cdot \cos \varphi . \tag{17}
\end{equation*}
$$

At $\tan \beta=1$ due to the equality of the interaction constants $g_{i j k}^{L}=g_{i j k}^{R}$ the degree of transverse polarization depends only on the cosinus of the angle between the spin vectors $\vec{\eta}_{1}$ and $\vec{\eta}_{2}$ :

$$
\begin{equation*}
P_{\perp}=\cos \varphi \tag{18}
\end{equation*}
$$

At $\varphi=0^{\circ}$ the degree of transverse polarization of the chargino is +1 , with increasing angle $\varphi$, the degree of transverse polarization decreases and vanishes at an angle $\varphi=90^{\circ}$. Then, the degree of transverse polarization changes sign and decreases to -1 at $=180^{\circ}$. A further increase in the angle $\varphi$ from $180^{\circ}$ to $360^{\circ}$
leads to an increase in the degree of transverse polarization from -1 to +1 . It should be noted that in the approximation $|\mu| \gg M_{2}$ or $M_{2} \gg|\mu|$ the decays of the Higgs bosons into a pair of identical chargino $H_{k} \Rightarrow \tilde{\chi}_{1}^{-}+\tilde{\chi}_{1}^{+}\left(\tilde{\chi}_{2}^{-}+\tilde{\chi}_{2}^{+}\right)$are suppressed.

In this case, the decays of the heavy $H$ and $A$ bosons into a pair of different $H(A) \Rightarrow \tilde{\chi}_{1}^{-}+\tilde{\chi}_{2}^{+}$ chargino dominate. In fig. 5 shows the dependence of decay $H \Rightarrow \tilde{\chi}_{1}^{-}+\tilde{\chi}_{2}^{+}$width on the Higgs boson mass $M_{H} \quad$ at $\quad \tan \beta=1, \quad \mu=160 \mathrm{GeV}, \quad M_{2}=$ $150 \mathrm{GeV}, M_{W}=80.385 \mathrm{GeV}, M_{Z}=91.1875 \mathrm{GeV}$.

With an increase in the Higgs boson mass $M_{H}$ the decay width increases.


Fig. 5. Dependence of the decay width $H \Rightarrow \tilde{\chi}_{1}^{-} \tilde{\chi}_{2}^{+}$on the mass $M_{H}$


Fig. 6. Dependence of the decay width $\Gamma\left(H(A) \Rightarrow \tilde{\chi}_{1}^{-} \tilde{\chi}_{2}^{+}\right)$on the mass $M_{\Phi}$

In the $M_{A} \gg|\mu| \gg M_{2}$ limit, the partial decay widths of $H \Rightarrow \tilde{\chi}_{1}^{ \pm}+\tilde{\chi}_{2}^{\mp}$ and $A \Rightarrow \tilde{\chi}_{1}^{ \pm}+\tilde{\chi}_{2}^{\mp}$ are equal

$$
\begin{gather*}
\Gamma\left(H \Rightarrow \tilde{\chi}_{1}^{-} \tilde{\chi}_{2}^{+}\right)=\frac{G_{F} M_{W}^{2}}{4 \sqrt{2} \pi} M_{H}  \tag{18}\\
\Gamma\left(A \Rightarrow \tilde{\chi}_{1}^{-} \tilde{\chi}_{2}^{+}\right)=\frac{G_{F} M_{W}^{2}}{4 \sqrt{2} \pi} M_{A}
\end{gather*}
$$

The dependence of the width of these decays on the Higgs mass $M_{H}$ and $M_{A}$ boson is shown in fig. 6. At $M_{\Phi}=305 \mathrm{GeV}$, the decay width is 4 GeV , with an increase in the Higgs boson mass, the decay width increases, and with a mass $M_{\Phi}=602 \mathrm{GeV}$, the decay width reaches 8 GeV .

## 3. HIGGS BOSON DECAYS INTO A PAIR OF NEUTRALINO

Neutral vino $\widetilde{W}^{0}$ and bino $\widetilde{B}^{0}$, as well as Higgsino $\widetilde{H}_{1}^{0}$ and $\widetilde{H}_{2}^{0}$ interact weakly, they are not proper mass states. The four mass states of the neutralino $\tilde{\chi}_{i}^{0}(i=$ $1,2,3,4$ ) are alternating combinations of the particles mentioned above. Neutralino - Majorana fermions, their antiparticles coincide with their particles. The neutralino mass matrix, as in the case of the chargino, depends on the parameters, $M_{2}, \tan \beta$ and also on the new mass parameter $M_{1}$ of the bino $\tilde{B}^{0}[8,11]$. As in the case of the chargino, with a large value of one of the parameters $\mu$ or $M_{2}$, two neutralino correspond to a pure gaugino-like state, and the other neutralino ones correspond to a pure Higgsino-like state. In these limiting states, the neutralino masses are equal to:



The decay width of the Higgs bosons $H_{k}$ into a neutralino pair for arbitrarily polarized particles is determined by a formula similar to formula (11). In a particular case, the decay width $H_{k} \Rightarrow \tilde{\chi}_{i}^{0}+\tilde{\chi}_{j}^{0}$ in the case of the production of a longitudinally polarized neutralino pair is determined by the expression:

$$
\begin{equation*}
\Gamma\left(\lambda_{1}, \lambda_{2}\right)=\frac{1}{4} \Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{0} \tilde{\chi}_{j}^{0}\right)\left[1+\lambda_{1} \lambda_{2}+\left(\lambda_{1}+\lambda_{2}\right) P\right] \tag{19}
\end{equation*}
$$

here

$$
\begin{equation*}
\Gamma_{0}\left(H_{k} \Rightarrow \tilde{\chi}_{i}^{0} \tilde{\chi}_{j}^{0}\right)=\frac{G_{F} M_{W}^{2}}{2 \sqrt{2} \pi} M_{H_{k}} \delta \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 \varepsilon_{i} \varepsilon_{j} g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}\right\} \tag{20}
\end{equation*}
$$

is the width of this decay in the case of unpolarized neutralino, and $P$ is the degree of longitudinal polarization of neutralino, defined by the expression

$$
\begin{equation*}
P=-\frac{\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{\lambda\left(r_{i}, r_{j}\right)}}{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 \varepsilon_{i} \varepsilon_{j} g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}} ; \tag{21}
\end{equation*}
$$

the factor $\delta$ in formula (20) is equal to $1\left(\frac{1}{2}\right)$, if a pair of different (identical) neutralinos are born, $\varepsilon_{i}$ and $\varepsilon_{j}$ determine the sign of the parameter $\mu, g_{i j k}^{L}$ and $g_{i j k}^{R}$ are the interaction constants of the Higgs boson $H_{k}$ with a pair of neutralino [8,11] :

$$
\begin{gather*}
g_{i j k}^{L}=\frac{1}{2}\left(Z_{j 2}-\tan \theta_{W} Z_{j 1}\right)\left(Z_{i 3} e_{k}+Z_{i 4} d_{k}\right)+i \rightarrow j \\
g_{i j k}^{R}=\frac{1}{2}\left(Z_{j 2}-\tan \theta_{W} Z_{j 1}\right)\left(Z_{i 3} e_{k}+Z_{j 4} d_{k}\right) \varepsilon_{k}+i \rightarrow j \tag{22}
\end{gather*}
$$

$Z$ is $4 \times 4$ matrix diagonalizing the neutralino mass matrix ; $\varepsilon_{1}=\varepsilon_{2}=-\varepsilon_{3}=1$; the coefficients $e_{k}$ and $d_{k}$ are given by expressions (9) ; $\theta_{W}$ is the Weinberg angle.

Denote the simplest neutralino by $\tilde{\chi}^{0}$; it can be the easiest SUSY particle. Then all other SUSY particles will decay into $\tilde{\chi}^{0}$ and ordinary SM particles. Table 1 shows the upper bounds on the masses of SUSY particles for various values of the parameter $\tan \beta$. In the table, $\tilde{\tau}$ and $\tilde{t}$ are sfermions - stau lepton and stop quark.

Table 1.
Upper Boundaries for SUSY Particle Masses

| $\tan \beta$ | $\tilde{\chi}^{0}$ | $\tilde{\chi}^{-}$ | $\tilde{\tau}$ | $\tilde{t}$ |
| :--- | :---: | :---: | :---: | :---: |
| 10 | 155 | 280 | 170 | 580 |
| 15 | 168 | 300 | 185 | 640 |
| 20 | 220 | 400 | 236 | 812 |
| 30 | 260 | 470 | 280 | 990 |

Calculations show that the decay widths of the heavy Higgs bosons $H$ and $A$ into a pair of different neutralinos $\tilde{\chi}_{1}^{0} \tilde{\chi}_{3}^{0}, \tilde{\chi}_{1}^{0} \tilde{\chi}_{4}^{0}, \tilde{\chi}_{2}^{0} \tilde{\chi}_{3}^{0}$ and $\tilde{\chi}_{2}^{0} \tilde{\chi}_{4}^{0}$ are prevailed. The widths of these decays are shown in Table 2 (in units of $\frac{G_{F} M_{W}^{2}}{8 \sqrt{2} \pi} M_{H_{k}}$ ).

Table 2.
Decay widths of H and A into a neutralino pair

| Neutralino pair | $\Gamma\left(H \Rightarrow \tilde{\chi}_{i}^{0} \tilde{\chi}_{j}^{0}\right)$ | $\Gamma\left(A \Rightarrow \tilde{\chi}_{i}^{0} \tilde{\chi}_{j}^{0}\right)$ |
| :--- | :--- | :---: |
| $\tilde{\chi}_{1}^{0} \tilde{\chi}_{3}^{0}$ | $\tan ^{2} \theta_{W}(1+\sin 2 \beta)$ | $\tan ^{2} \theta_{W}(1-\sin 2 \beta)$ |
| $\tilde{\chi}_{1}^{0} \tilde{\chi}_{4}^{0}$ | $\tan ^{2} \theta_{W}(1-\sin 2 \beta)$ | $\tan ^{2} \theta_{W}(1+\sin 2 \beta)$ |
| $\tilde{\chi}_{2}^{0} \tilde{\chi}_{3}^{0}$ | $(1+\sin 2 \beta)$ | $(1-\sin 2 \beta)$ |
| $\tilde{\chi}_{2}^{0} \tilde{\chi}_{4}^{0}$ | $(1-\sin 2 \beta)$ | $(1+\sin 2 \beta)$ |

Fig. 7(a) and (b) illustrate the dependence of the decay width $H \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{3}^{0}$ and $\mathrm{A} \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{4}^{0}$ on the Higgs boson mass $M_{H}$ and $M_{A}$ for $\tan \beta=3, \sin ^{2} \theta_{W}=0.2315$. In these figures, the decay width $H \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{3}^{0}$ and $\mathrm{A} \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{4}^{0}$ with an increase in the Higgs boson masses the $H$ and A are observed.


Fig. 7. Dependence of the decay width $H \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{3}^{0}$ (a) and $\mathrm{A} \Rightarrow \tilde{\chi}_{2}^{0}+\tilde{\chi}_{4}^{0}$ (b) on the masses $M_{H}$ and $M_{A}$

## 4. DECAYS OF HIGGS BOSON $H^{ \pm}$INTO THE CHARGINO - NEUTRALINO PAIR

The charged Higgs boson $\mathrm{H}^{ \pm}$can decay into a pair of chargino-neutralino along the channel $H^{ \pm} \Rightarrow \tilde{\chi}_{i}^{ \pm}+\tilde{\chi}_{j}^{0}$. Having performed standard calculations, we obtain for the decay width $H^{-} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{0}$ in the Higgs boson rest system :

$$
\begin{align*}
& \frac{d \Gamma\left(\vec{l}_{1}, \vec{\xi}_{2}\right)}{d \Omega}=\frac{G_{F} M_{W}^{2}}{32 \sqrt{2} \pi^{2}} M_{H^{-}} \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left\{[ ( g _ { i j k } ^ { L } ) ^ { 2 } + ( g _ { i j k } ^ { R } ) ^ { 2 } ] \left[\left(1-r_{i}-r_{j}\right)\left(1-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)-2 \sqrt{r_{i} r_{j}} \times\right.\right. \\
& \left.\times\left(\left(\vec{\xi}_{1} \vec{\xi}_{2}\right)-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)\right]+\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left[\left(\vec{n} \vec{\xi}_{1}\right)-\left(\vec{n} \vec{\xi}_{2}\right)\right]+2 g_{i j k}^{L} g_{i j k}^{R} \times \\
& \left.\times\left[\left(1-r_{i}-r_{j}\right)\left(\left(\vec{\xi}_{1} \vec{\xi}_{2}\right)-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)-2 \sqrt{r_{i} r_{j}}\left(1-\left(\vec{n} \vec{\xi}_{1}\right)\left(\vec{n} \vec{\xi}_{2}\right)\right)\right]\right\} . \tag{23}
\end{align*}
$$

Here $\vec{n}$ is a unit vector in the direction of the mometum of the chargino; $\vec{\xi}_{1}$ and $\vec{\xi}_{2}$ are unit vectors characterizing the polarization of chargino and neutralino; $d \Omega=\sin \theta d \theta d \varphi$ is the solid angle of departure of the chargino; $\lambda\left(r_{i}, r_{j}\right)$ is a kinematic function;

$$
r_{i}=\left(\frac{m_{\tilde{\chi}_{i}^{-}}}{M_{H^{-}}}\right)^{2}, r_{j}=\left(\frac{m_{\widetilde{\chi}_{j}^{0}}}{M_{H^{-}}}\right)^{2}
$$

$g_{i j k}^{L}$ and $g_{i j k}^{R}$ are the interaction constants of the Higgs boson $H_{k}=H_{4}=H^{ \pm}$with the chargino - neutralino pair:

$$
\begin{gather*}
g_{i j k}^{L}=\frac{1}{2}\left(Z_{j 2}-\tan \theta_{W} Z_{j 1}\right)\left(Z_{i 3} e_{k}+Z_{i 4} d_{k}\right)+i \rightarrow j \\
g_{i j k}^{R}=\frac{1}{2}\left(Z_{j 2}-\tan \theta_{W} Z_{j 1}\right)\left(Z_{i 3} e_{k}+Z_{j 4} d_{k}\right) \varepsilon_{k}+i \rightarrow j \tag{24}
\end{gather*}
$$

$Z-4 \times 4$ matrix diagonalizing the neutralino mass matrix; $\varepsilon_{1}=\varepsilon_{2}=-\varepsilon_{3}=1$; the coefficients $e_{k}$ and $d_{k}$ are given by expressions (9).

In the case of a longitudinally polarized chargino-neutralino pair, the decay width $H^{-} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{0}$ takes the form:

$$
\begin{equation*}
\Gamma\left(\lambda_{1}, \lambda_{2}\right)=\frac{1}{4} \Gamma_{0}\left(H^{-} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{0}\right)\left[1+\lambda_{1} \lambda_{2}+\left(\lambda_{1}+\lambda_{2}\right) P\right] \tag{25}
\end{equation*}
$$

here
$\Gamma_{0}\left(H^{-} \Rightarrow \tilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{0}\right)=\frac{G_{F} M_{W}^{2}}{2 \sqrt{2} \pi} M_{H^{-}} \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}\right\}$
is the decay width of the charged Higgs boson into a pair of unpolarized chargino - neutralino, $\lambda_{1}$ and $\lambda_{2}$ are chargino and neutralino helicities, and $P$ is a degree of longitudinal polarization of chargino (neutralino)

$$
\begin{equation*}
P=\frac{\left[\left(g_{i j k}^{L}\right)^{2}-\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{\lambda\left(r_{i}, r_{j}\right)}}{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}} \tag{27}
\end{equation*}
$$

In the case when the chargino and neutralino are transversely polarized, for the decay width $H^{-} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{0}$ we obtain the following expression:

$$
\begin{equation*}
\frac{d \Gamma\left(\eta_{1} \eta_{2}\right)}{d \varphi}=\frac{1}{4} \frac{d \Gamma_{0}\left(H^{-} \Rightarrow \tilde{\chi}_{i}^{-} \widetilde{\chi}_{j}^{0}\right)}{d \varphi}\left[1+\eta_{1} \eta_{2} P_{\perp}\right] \tag{28}
\end{equation*}
$$

Here
$\frac{d \Gamma_{0}\left(H^{-} \Rightarrow \widetilde{\chi}_{i}^{-} \tilde{\chi}_{j}^{0}\right)}{d \varphi}=\frac{G_{F} M_{W}^{2}}{4 \sqrt{2} \pi^{2}} M_{H^{-}} \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left\{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}\right\}$
is a differential decay width and

$$
\begin{equation*}
P_{\perp}=\cos \varphi \frac{2 g_{i j k}^{L} g_{i j k}^{R}\left(1-r_{i}-r_{j}\right)-2\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right] \sqrt{r_{i} r_{j}}}{\left[\left(g_{i j k}^{L}\right)^{2}+\left(g_{i j k}^{R}\right)^{2}\right]\left(1-r_{i}-r_{j}\right)-4 g_{i j k}^{L} g_{i j k}^{R} \sqrt{r_{i} r_{j}}} \tag{30}
\end{equation*}
$$

is a degree of transverse polarization of chargino neutralino. It can be seen that the degree of transverse polarization $P_{\perp}$ is very sensitive to the angle $\varphi$ between the transverse spin vectors $\vec{\eta}_{1}$ and $\vec{\eta}_{2}$. With parallel ( $\vec{\eta}_{1} \uparrow \uparrow \vec{\eta}_{2}$ ) and antiparallel ( $\vec{\eta}_{1} \uparrow \downarrow \vec{\eta}_{2}$ ) spin vectors, the degree of transverse polarization modul reaches a maximum value. If the transverse spin vectors $\vec{\eta}_{1}$ and $\vec{\eta}_{2}$ are mutually perpendicular ( $\vec{\eta}_{1} \perp \vec{\eta}_{2}$ ), then the degree of transverse polarization $P_{\perp}$ vanishes.

Note that in the $H^{-} \Rightarrow \tilde{\chi}_{1}^{-} \tilde{\chi}_{3}^{0}$ decay the coupling constants $g_{i j k}^{L}$ and $g_{i j k}^{R}$ are equal to each other, as a result, the degree of longitudinal polarization of the chargino (neutralino) vanishes, and the degree of transverse polarization of the chargino-neutralino will depend only on the angle $\varphi$ between the transverse spin vectors $\vec{\eta}_{1}$ and $\vec{\eta}_{2}$ :

$$
P_{\perp}=\cos \varphi
$$

In the approximation $M_{A} \gg|\mu| \gg M_{2}$, the parsial decay widths of the charged Higgs boson into a
chargino-neutralino pair are given in Table 3 (in $\frac{G_{F} M_{W}^{2}}{4 \sqrt{2} \pi} M_{H^{ \pm}}$units).

Table 3.
Parsial decay widths $\mathrm{H}^{ \pm} \Rightarrow \tilde{\chi}_{i}^{ \pm} \tilde{\chi}_{j}^{0}$

| Chargino - neutralino | $\Gamma\left(\mathrm{H}^{ \pm} \Rightarrow \tilde{\chi}_{i}^{ \pm} \tilde{\chi}_{j}^{0}\right)$ |
| :---: | :---: |
| $\tilde{\chi}_{1}^{ \pm} \tilde{\chi}_{3}^{0}$ | 1 |
| $\tilde{\chi}_{1}^{ \pm} \tilde{\chi}_{4}^{0}$ | 1 |
| $\tilde{\chi}_{2}^{ \pm} \tilde{\chi}_{1}^{0}$ | $\tan ^{2} \theta_{W}$ |
| $\tilde{\chi}_{2}^{ \pm} \tilde{\chi}_{2}^{0}$ | 1 |

In fig. 8 shows the dependence of the decay width $\mathrm{H}^{-} \Rightarrow \tilde{\chi}_{2}^{-}+\tilde{\chi}_{1}^{0}$ on the Higgs mass of the boson $M_{\mathrm{H}^{-}}$at $\tan \beta=3$ and $\sin ^{2} \theta_{W}=0.2315$. With an increase in the Higgs boson mass $M_{\mathrm{H}^{-}}$, the decay width increases.


Fig 8. Dependence of the decay width $\mathrm{H}^{-} \Rightarrow \tilde{\chi}_{2}^{-} \tilde{\chi}_{1}^{0}$ on the mass $M_{\mathrm{H}^{-}}$

Note that for large Higgs boson masses, the total decays widths $H, A, H^{ \pm}$into a pair of chargino and neutralino does not depend on the parameters $M_{2}, \mu, \tan \beta$ and in the asymptotic limit $M_{H_{k}} \gg m_{\tilde{\chi}}$ we have

$$
\begin{equation*}
\Gamma_{0}\left(H_{k} \Rightarrow \sum_{i, j} \tilde{\chi}_{i} \tilde{\chi}_{j}\right)=\frac{3 G_{F} M_{W}^{2}}{4 \sqrt{2} \pi} M_{H_{k}}\left(1+\tan ^{2} \theta_{W}\right) \tag{31}
\end{equation*}
$$

We also introduce the width of the Higgs boson decay channels $(A) \Rightarrow t+\bar{t}, H(A) \Rightarrow b+\bar{b}, H^{+} \Rightarrow t+\bar{b}$, then we have the expression for branching
$B R\left(H_{k} \Rightarrow \sum_{i, j} \tilde{\chi}_{i} \tilde{\chi}_{j}\right)=\frac{\Gamma\left(H_{k} \Rightarrow \sum_{i, j} \widetilde{\chi}_{i} \widetilde{\chi}_{j}\right)}{\Gamma\left(H_{k} \Rightarrow \sum_{i, j} \widetilde{\chi}_{i} \tilde{\chi}_{j}\right)+\Gamma\left(H_{k} \Rightarrow t \bar{t}+b \bar{b}+t \bar{b}\right)}=\frac{\left(1+\frac{1}{3} \tan ^{2} \theta_{W}\right) M_{W}^{2}}{\left(1+\frac{1}{3} \tan ^{2} \theta_{W}\right) M_{W}^{2}+m_{t}^{2} c t a n}{ }^{2} \beta+m_{b}^{2} \tan ^{2} \beta \quad$

In fig. 9 illustrates the dependence of branching (32) on the parameter $\tan \beta$ in the asymptotic regime $M_{A} \sim M_{H} \sim M_{H^{ \pm}} \approx 1$ ТэВ $\gg m_{\chi}$ at $\sin ^{2} \theta_{W}=0.2315$.


Fig 9. Branching $B R\left(H_{k} \Rightarrow \sum_{i, j} \tilde{\chi}_{i} \tilde{\chi}_{j}\right)$ as a function of $\tan \beta$

As can be seen from the figure, with the parameter $\tan \beta$ increasing, the branching also increases and reaches a maximum at $\tan \beta=5$, and a further increase in the parameter $\tan \beta$ leads to a decrease in branching

## 5. HIGGS BOSON DECAYS INTO A PAIR OF SFERMIONS

The scalar partners of fermions (sfermions) form a set of new particles: $v_{\tau L}, \tau_{L}, \tau_{R}, \tilde{t}_{L}, \tilde{t}_{R}, \tilde{b}_{L}, \tilde{b}_{R}$ are in the third family. All of them are complex scalar fields and the indices $\mathrm{L}, \mathrm{R}$ are used to denote the SM fermions with which these fields partner. The sfermions $\tilde{f}_{L}$ and $\tilde{f}_{R}$ mix with each other and new states $\tilde{f}_{1}$ и $\tilde{f}_{2}$ with masses arise

$$
\begin{equation*}
m_{\tilde{f}_{1}, \tilde{f}_{2}}^{2}=m_{f}^{2}+\frac{1}{2}\left[m_{\tilde{f}_{L}}^{2}+m_{\tilde{f}_{R}}^{2} \mp \sqrt{\left(m_{\tilde{f}_{L}}^{2}-m_{\tilde{f}_{R}}^{2}\right)^{2}+4 m_{f}^{2}\left(A_{f}-\mu r_{f}\right)^{2}}\right] \tag{33}
\end{equation*}
$$

where $A_{f}$ and $r_{f}$ is some parameters.
The interaction constants of neutral Higgs bosons with sfermions are determined by the expressions

$$
\begin{gather*}
g_{H_{k} \tilde{f}_{L} \tilde{f}_{L}}=m_{f}^{2}+M_{Z}^{2}\left(I_{3}(f)-Q_{f} \sin ^{2} \theta_{W}\right) g_{2} \\
g_{H_{k} \tilde{f}_{R} \tilde{f}_{R}}=m_{f}^{2} g_{1}+M_{Z}^{2} Q_{f} \sin ^{2} \theta_{W} g_{2}  \tag{34}\\
g_{H_{k} \tilde{f}_{L} \tilde{f}_{R}}=-\frac{1}{2} m_{f}\left(\mu g_{3}-A_{f} g_{4}\right)
\end{gather*}
$$

where the coefficients $g_{i}(i=1,2,3,4)$ are given in Table 4.
Table 4.
Coefficients $\mathrm{g}_{\mathrm{i}}(i=1,2,3,4)$

| $\tilde{f}$ | $H_{k}$ | $g_{1}$ | $g_{2}$ | $g_{3}$ | $g_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\tilde{t}$ | $H$ | $\sin \alpha / \sin \beta$ | $\cos (\alpha+\beta)$ | $\cos \alpha / \sin \beta$ | $\sin \alpha / \sin \beta$ |
|  | $h$ | $\cos \alpha / \sin \beta$ | $-\sin (\alpha+\beta)$ | $-\sin \alpha / \sin \beta$ | $\cos \alpha / \sin \beta$ |
|  | $A$ | 0 | 0 | 1 | $-\operatorname{ctan} \beta$ |
| $\tilde{b}$ | $H$ | $\cos \alpha / \cos \beta$ | $\cos (\alpha+\beta)$ | $\sin \alpha / \cos \beta$ | $\cos \alpha / \cos \beta$ |
|  | $h$ | $-\sin \alpha / \cos \beta$ | $-\sin (\alpha+\beta)$ | $\cos \alpha / \cos \beta$ | $-\sin \alpha / \cos \beta$ |
|  | $A$ | 0 | 0 | 1 | $-\tan \beta$ |

The interaction constants of the charged Higgs boson $H^{ \pm}$with a sfermion pair $\tilde{t}_{\alpha} \tilde{b}_{\beta}(\alpha, \beta=L, R)$ can be expressed as:

$$
\begin{equation*}
g_{H^{ \pm} \tilde{t}_{\alpha} \tilde{b}_{\beta}}=\frac{1}{\sqrt{2}}\left(g_{1}^{\alpha \beta}+M_{W}^{2} g_{2}^{\alpha \beta}\right) \tag{35}
\end{equation*}
$$

The coefficients $g_{1}^{\alpha \beta}$ and $g_{2}^{\alpha \beta}$ are shown in Table 5.
Table 5.

$$
\text { Coefficients } g_{i}^{\alpha \beta}(i=1,2 ; \alpha, \beta=L, R)
$$

| $i$ | $g_{i}^{L L}$ | $g_{i}^{R R}$ | $g_{i}^{L R}$ | $g_{i}^{R L}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $m_{t}^{2} \operatorname{ctan}+m_{b}^{2} \tan \beta$ | $m_{t} m_{b}(\operatorname{ctan}+\tan \beta)$ | $m_{b}\left(\mu+A_{b} \tan \beta\right)$ | $m_{t}\left(\mu+A_{t} \operatorname{ctan} \beta\right)$ |
| 2 | $-\sin 2 \beta$ | 0 | 0 | 0 |

The parsial Higgs boson decay widths $H_{k}\left(k=1,2,3\right.$ and 4 correspond to the bosons, $H, h, A$ and $\left.H^{ \pm}\right)$in the sfermion pair $\tilde{f}_{i} \tilde{f}_{j}(i, j=1,2)$ can be written as follows:

$$
\begin{equation*}
\Gamma\left(H_{k} \Rightarrow \tilde{f}_{i} \tilde{f}_{j}\right)=\frac{N_{c} G_{F}}{2 \sqrt{2} \pi M_{H_{k}}} \sqrt{\lambda\left(r_{i}, r_{j}\right)}\left(g_{H_{k} \tilde{f}_{i} \tilde{f}_{j}}\right)^{2} \tag{36}
\end{equation*}
$$

where $N_{c}$ is the color factor $\left(N_{c}=3(1)\right)$ at the birth of a squark (slept on) pair $r_{i}=\left(\frac{m_{\tilde{f}_{i}}}{M_{H_{k}}}\right)^{2}, r_{j}=\left(\frac{m_{\tilde{f}_{j}}}{M_{H_{k}}}\right)^{2}$; interaction constants $g_{H_{k} \tilde{f}_{i} \tilde{f}_{j}}$ can be obtained from the interaction constants (34) and (35) using the mixing relations of sfermions. These constants are given in [8,11].

To estimate the decay width (36), we consider $H^{ \pm}$boson decay into a pair of $\tilde{u}_{L} \overline{\tilde{d}}_{L}$ - squarks. In this decay, the interaction constant $g_{H^{+} \tilde{u}_{L} \tilde{d}_{L}}$ is equal to:

$$
\begin{equation*}
g_{H^{+} \widetilde{u}_{L} \tilde{d}_{L}}=-\frac{1}{\sqrt{2}}\left[m_{u}^{2} \operatorname{ctan} \beta+m_{d}^{2} \tan \beta-M_{W}^{2} \sin 2 \beta\right] \tag{37}
\end{equation*}
$$

Since the masses of $u$ - and $d$ - quarks are much smaller than the mass of the gauge $W$ - boson $\left(M_{W} \gg m_{u}, m_{d}\right)$, for the interaction constant $g_{H^{+} \tilde{u}_{L} \tilde{d}_{L}}$ we have :

$$
\begin{equation*}
g_{H^{+} \tilde{u}_{L} \tilde{d}_{L}}=-\frac{1}{\sqrt{2}} M_{W}^{2} \sin 2 \beta \tag{38}
\end{equation*}
$$

Thus, in the first and second families with massless fermions, the pseudoscalar $A$ - boson does not decay into a pair of sfermions, and the decay widths of the heavier $H^{ \pm}$and $H$ - bosons into a sfermion pair are proportional to the expression
$\Gamma\left(H^{ \pm}(H) \Rightarrow \tilde{f} \tilde{f}\right) \sim \frac{G_{F} M_{W}^{4}}{2 \sqrt{2} \pi M_{H^{ \pm}(H)}} \sin ^{2} 2 \beta$.
These decay widths are maximum for small values of the parameter $\operatorname{tg} \beta \approx 1$.

Figure 10 shows the dependence of the decay width $H^{ \pm} \Rightarrow \tilde{t}_{R}+\tilde{b}_{L}$ on the Higgs boson mass $\mathrm{M}_{H^{ \pm}}$ for $m_{\tilde{t}}=160 \mathrm{GeV}, \quad m_{\tilde{b}}=140 \mathrm{GeV}, \quad \tan \beta=10$,
$\mu=160 \mathrm{GeV}$ and $\mathrm{A}_{t}=320 \mathrm{GeV}$. It can be seen from the figure that with an increase in the Higgs boson mass $\mathrm{M}_{H^{ \pm}}$the decay width increases and reaches a maximum at $\mathrm{M}_{H^{ \pm}}=425 \mathrm{GeV}$, and then the decay width decreases and near $\mathrm{M}_{H^{ \pm}}=650 \mathrm{GeV}$ secondary maximum and with a further increase in the Higgs boson mass, its decay width decreases again.


Fig 10. Dependence of the decay width $\Gamma\left(H^{ \pm} \Rightarrow \tilde{t}_{R} \tilde{b}_{L}\right)$ on the mass $\mathrm{M}_{H^{ \pm}}$

## CONCLUSION

We discussed the decay widths of the Higgs bosons $H, h, A$ and $H^{ \pm}$into supersymmetric particles, precisely decays into a pair of chargino $H_{k} \Rightarrow \tilde{\chi}_{i}^{-}+\tilde{\chi}_{j}^{+}$, decays into a pair of neutralino $H_{k} \Rightarrow \tilde{\chi}_{i}^{0}+\tilde{\chi}_{j}^{0}$, decays into a pair of chargino-neutralino $H_{k}^{ \pm} \Rightarrow \tilde{\chi}_{i}^{ \pm}+\tilde{\chi}_{j}^{0}$, decays into a pair of sfermions $H_{k} \Rightarrow \tilde{f}_{i}+\bar{f}_{j}$. In the framework of the MSSM, analytical expressions are obtained for the decay width of the Higgs boson mass. The research results are illustrated by graphs.
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