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# ANALYSIS OF MAIN ARTIFACTS IN SCANNING PROBE MICROSCOPY (I) 

S.D. ALEKPEROV ${ }^{1,2}$<br>${ }^{1}$ The branch of MSU named by M.V. Lomonosov in Baku, AZ-1141, F. Agayev str., 14, Baku<br>${ }^{2}$ H.M. Abdullayev Institute of Physics of Azerbaijan National Academy of Sciences AZ-1143, G.Javid str., 33, Baku<br>e-mail: sdalekperov@mail.ru


#### Abstract

The analysis of experiment carrying methodology in the scanning probe microscopy (SPM) region is carried out, the main parameters influencing on image quality are revealed. In order to reveal the artifact reason the main components of SPM signal which are divided on 5 groups: the useful signal; noises connected with external influences and temperature drift; distortions connected with piezoceramics and piezo-scanner non-ideality; probe geometry influence; apparatus noises are considered. The main methods of removal and minimization of the given artifacts are considered. The second and third groups of main components of SPM signal are considered in the article first part.


Keywords: scanning probe microscopy (SPM); scanning tunneling microscopy (STM); atomic force microscopy (AFM). PACS :81.05.Je, 81.70.-q

## INTRODUCTION

The advantages of probe microscopy methods [1,2] opposite to traditional investigation methods are difficultly overestimated. Let's enumerate the advantages of these methods: 1) high resolution up to atomic one $\sim 0,1 \mathrm{~nm}$ [3] in the combination with investigation locality allow us to compare SPM with transmission electron microscope; 2) the locality(the measurements are carried out directly in each surface point) gives to SPM the advantages in the comparison with investigation integral methods where the information is collected from any surface area or volume and further is averaged; 3) low interaction energies with the investigated object make the SPM methods indestructible ones, the average electron energy is milli-electron-volt order in scanning tunneling microscope STM, the interaction forces are usually nano-newton order in atomic force microscope AFM. This is very important at the investigation of "delicate" molecular objects, thin films, smooth polymer materials and bioobjects [5-7]; 4) the investigations by SPM methods can be carried out practically in any mediums in situ [8,9]: from super-high vacuum up to liquid solutions in the difference from all other surface investigation methods requiring the high vacuum. The limit condition is only one: the probe inertia to investigation medium; 5) the electroconductivity of investigated surface $[10,11]$ isn't critic one for SPM methods. This fact allows us to investigate the objects of any conductance that also provides the advantage in the comparison with electron microscopy and other methods of surface electron analysis.
However, in spite of all these facts, the following and systematization of possible artifact appearance mechanisms are essentially important ones for adequate SPM application in wide-ranging scientific investigations. The last ones are the hardware effects leading to observation of false or distorted properties of investigated objects which can be caused by the influence of the research tool itself and etc. These artifacts as a rule, are easily taken into account on qualitative level at SPM result interpretation, however, the specifics of series of tasks can require the qualitative estimations and recombination of object real geometry methods. SPM images towards with useful information contain also much secondary information distorting the data about morphology and surface properties. In order to reveal the artifact reason, let's consider
the main components of SPM signal. They can be divided on 5 groups: 1) the useful signal; 2) noises connected with external influences and temperature drift; 3) distortions connected with piezoceramics and piezo-scanner nonideality; 4) the influence of the probe geometry; 5) hardware noises. The last 4 groups contribute the essential distortions into obtained surface relief. In first part of the article we will consider the second and third groups of main components of SPM signal.

## 1. THE NOISES CONNECTED WITH EXTERNAL INFLUENCES AND TEMPERATURE DRIFT

One should make compromise between value maximal sweep of scanning element and its resonance frequency [12] in the constructions of modern microscopes. The typical values of resonance frequencies for scanners are in the range $10-100 \mathrm{kHz}$. The different types of vibration isolation systems [13] are used for devise defense from external influences. The vibration isolation systems can be conditionally divided on active and passive ones. The main idea, consisting in passive vibration isolation systems, is the following one. The amplitude of forced oscillations of mechanical system strongly decreases at the difference increase between excitation force frequency and resonance eigenfrequency of system (the typical amplitude-frequency characteristics (AFC) of oscillation system is given on fig.1). That's why the external influences with $w_{2} \gg w_{1}$ frequencies don't practically essentially influence on oscillation system. As the proper frequencies of SPM heads are $10-100 \mathrm{kHz}$ so choosing the resonance eigenfrequency of vibration isolation system enough low one (by $5-10 \mathrm{kHz}$ order), one can effectively defense the device from external vibrations.

However, it is difficult to realize the low frequencies in practices. For spring platforms and elastic suspensions the frequency is equal to $\omega_{0}=\sqrt{\frac{\kappa}{m}}$ where $k$ is spring constant (or elastic suspension), $m$ is mass of vibration isolation platform with SPM head. Let's estimate the vibration isolation system parameters providing the depression of highfrequency vibrations. From equilibrium condition it is followed that $m g=k \Delta l$, where $\Delta l$ is elongation (or compression) of elastic element, $g$ is free fall acceleration.

Then for the elongation value we obtain: $\Delta l=\frac{g m}{k}=\frac{g}{\omega_{0}^{2}}=\frac{g}{(2 \pi v)^{2}} \cong 0,25 \times \frac{m(H z)^{2}}{v^{2}}$. Thus, for obtaining of resonance frequency of vibration isolation system by 1 kHz order it is necessary that elongation (or compression) of elastic element is 25 cm . One can easily realize such elongations with the help of spring or rubber suspensions. Taking into consideration that spring tension can achieve $100 \%$, for realization of suspension resonance frequency in 1 Hz the elastic element length should be 25 cm and consequently, the out-to-out measure of vibration isolation system is 50 cm . If we decrease the requirements to resonance frequency, then we can achieve the essential decrease of vibration isolation system sizes. Thus, the elastic element compression should be $2,5 \mathrm{~mm}$ for realization of frequency 10 Hz . Such compression enough easily occurs in practices with help of stack of metallic plates with rubber layers that significantly decreases the vibration isolation system sizes. The active systems of external vibration depression are also successfully used for defense of SPM heads. Such devices present themselves the negative feedback electro-mechanical systems which causes the stable position of vibration isolation platform in space. The principle of operation of active systems can be considered on the following simple example. The vibration gauge (accelerometer), which is the device reacting on acceleration endured by platform, is posited on platform. The signal from the gauge receives to feedback system (FS) where it increases and in antiphase is given to piezoelectric blocks which displaces to opposite side, damp the acceleration endured by platform. This is so-called proportional regulation. Indeed, let's under external force influence, the platform oscillates on $w$ frequency so that its displacement is $u=u_{0} \sin (w t)$.


Fig.1. The schematic image of amplitude-frequency characteristics of oscillation system ( $w_{l}$ is proper system resonance frequency; $w_{2}$ is external vibration frequency).

Then the acceleration of platform is equal to
$\frac{d^{2} u}{d t^{2}}=-w^{2} u_{0} \sin (w t)$. The feedback system in this case gives the antiphase signal on blocks as a result of which the platform displacement will present itself the superposition of two displacements :

$$
u=u_{0} \sin (w t)-A \sin (w t)=\left(u_{0}-A\right) \sin (w t)
$$

Moreover, the feedback system will increase signal amplitude $A$ till that platform acceleration will be equal to zero:
$\frac{d^{2} u}{d t^{2}}=-w^{2}\left(u_{0}-A\right) \sin (w t)$. The operation frequency band of active systems is defined by frequency band of stable work of feedback electromechanical system. In the case of nonharmonic vibrations $u=u(t)$ signal from accelerometer is integrated two times by hardware and in antiphase is given on piezoelectric blocks so that platform oscillation amplitude tends to zero:

$$
\frac{d^{2} u}{d t^{2}}=u(t)-A \iint \frac{d^{2} u}{d t^{2}}(t) d t \Rightarrow 0
$$

The one of SPM important problem is the task of probe stabilization position over investigated sample surface. The temperature change of environment or microscope construction element heat during the microscope work [14] is the main source of probe instability position. The solid body temperature change leads to appearance of thermoelastic deformations: $u_{i k}=\alpha_{i k} \Delta T$, where $u_{i k}$ is deformation tensor, $\alpha_{i k}$ is tensor of material thermal expansion coefficients; $\Delta T$ is temperature increment.

For isotropic materials the thermal expansion coefficient is scalar value so $\alpha_{i k}=\alpha \cdot \delta_{i k}$, where $\delta_{i k}$ is Kronecker unit tensor, $\alpha$ is absolute value of thermal expansion coefficient. The absolute elongation of microscope construction elements can be estimated from the following relations:

$$
u=\frac{\Delta l}{l_{0}}=\alpha \cdot \Delta T ; \Delta l=l_{0} \alpha \cdot \Delta T
$$

The typical values of material thermal expansions are $10^{-5}-10^{-6}$ degree $^{-1}$. So at body heating by length 10 cm on $1^{\circ} \mathrm{C}$ its length increases on the value by $1 \mu \mathrm{~m}$ order. Such deformations essentially influence on the work of probe microscopes. The thermostating of PSM measuring heads is applied for decrease of thermo-drift or thermo-compensating elements are introduced into head construction. Any SPM construction can be presented in the form of element series with different thermal expansion coefficients. The thermocompensating elements having the different expansion coefficients are introduced into construction of SPM measuring heads for thermo-drift compensation so that the following condition $\Delta L=\sum_{i} \Delta l_{i}=\Delta T \sum_{i} \alpha_{i} l_{i} \Rightarrow 0$ for temperature expansion sum in construction different arms is satisfied. The introduction of SPM compensating elements from the same material and with the same character sizes that the main elements have, is simplest method of thermo-drift decrease of probe position along Z axis. The probe displacement along Z direction will be minimal one at temperature change of such construction.

## 2. THE DISTORTIONS CONNECTED WITH PIEZOCERAMICS

 NONIDEALITYThe piezoelectric engines [15] are used for controlled needle displacement on super-small distances in SPM. Their task is to provide the precision mechanical scanning by probe of the investigated sample by the way of probe displacement relatively immovable sample or sample displacement relatively immovable probe. The operation of many
piezoelectric engines applied in modern SPM is based on the use of reversal piezoeffect which is in change of piezomaterial sizes at electric field influence. The basis of many piezoceramics used in SPM is $\mathrm{PbZr}_{1-\mathrm{x}} \mathrm{Ti}_{\mathrm{x}} \mathrm{O}_{3}$ composition (lead zirconate-titanate) with different additions [16]. The piezoplate elongation fixed from one edge is defined by the expression: $\Delta l=l \frac{U}{h} d_{31}$, where $l$ is plate length, $h$ is plate thickness, $U$ is electric voltage applied to electrodes posited on piezoplate faces, $d_{31}$ is material piezomodule. Piezomodule $d_{31}$ defining the voltage transformation in displacement in longitudinal direction is usually equal to $(30-350) \cdot 10^{-12} \mathrm{~m} / \mathrm{V}$. The piezomodule big coefficients are important for less scanner sizes and less controlling voltages. The maximal value of piezomaterial deformation defining the maximal scanning field is limited by electric field strength value at which the material electrical breakdown appears. The minimal step or displacement delicacy are mainly defined by noises of controlling electric voltage, mechanical vibration level and thermo-drift value. One can select main piezoceramic characteristics applied in SPM: small requisite power and absence of heat generation; $d_{31}$ piezomodule stability at low temperatures (up to helium $\sim 4,2 \mathrm{~K}$ ) that is important for low-temperature SPM; Curie temperature $170 \div 350{ }^{\circ} \mathrm{C}$; small sizes, high regidity and as a result, the high resonance frequencies (> 10 kHz ) necessary for defense from vibrations. The high resonance frequency allows us also to increase the scanning velocity, i.e. to decrease of SPM data obtaining time; applicability in different mediums and super-high vacuum as they are chemically aren't active ones and don't form the electromagnetic fields.

In spite of mentioned advantages, the piezoceramics also have some disadvantages which can introduce the specified distortions in SPM images:

1) Non-linearity

The piezoceramic deformation is the complex function of external field: $\Delta l=f(U)$. The typical values of $E^{*}$ fields at which the non-linear effects are seen, are $100 \mathrm{~V} / \mathrm{mm}$ order. That's why for correct work of scanning elements the controlling fields in the ceramic linearity region $\left(E<E^{*}\right)$ are usually used.
2) Hysteresis

SPM scanner hysteresis leads to displacement of scanning region (and correspondingly, SPM-images) obtained at direct and reversal displacements. That's why for exclusion of distortions of sample surface SPM-images connected with hysteresis, it is necessary to carry out the measurements only at direct or only reversal scanner motion.
3) Creep

If the applied voltage is in the form of step then the displacement continuance in the form of the given on the fig. 2 (piezoceramic bounce) is observed. The creep is revealed in the distortion of scan initial region at big squares and scanning velocities, i.e. when the voltage applied to piezomaterial, changes enough rapidly. The creep influence decreases at scanning velocity decrease and also after scanner "training". It is clear that creep reveals at strongly scanner displacement into required initial scanning point, that's why the strong jumps of controlling voltage are excluded in
algorithms of scanner control and time delays taking into consideration the creep are introduced.


Fig. 2. The piezoceramic creep and bounce.

## 4) Temperature drift

The occasional temperature changes always existing in the laboratory lead to change of construction element length and relative displacement of probe and sample. For example, at temperature change on $\Delta T=1^{\circ} \mathrm{C}$, the piezotube by $l=20 \mathrm{~mm}$ length with thermal linear expansion coefficient $\beta=2 \cdot 10^{-6} K^{-1}$ changes its length on $\Delta l=\beta \cdot l \cdot \Delta T=40 \AA$. The slow temperature drift along Z coordinate in scanning process leads to inclination of sample plane on SPM-image. The change of linear sizes along $X$ and $Y$ coordinates leading to mutual displacement of probe and sample in sample plane leads to the image scale change. As a whole, these distortions of piezoceramic properties are similar to ones caused by ceramic creep.

The nonideality of piezoceramic properties leads to the fact that SPM image obtained with the help of piezoceramic scanner contains the series of specific distortions. For tripod scanner the probe at scanning will move in Z-direction on arc of a circle and for tube scanner the probe trajectory at scanning will be describe the complex hyperbolic function. In both cases the image which is seen curved even when real sample surface is totally plane, is obtained. Partially these images can be excluded on hardwire level using the linearization methods of scanner characteristics. There are the several methods of scanner nonlinearity corrections in scanning probe microscopes. The most reliable and the most expensive method to solve of this problem is in the direct measurement of scanner momentary position and nonlinearity correction in real time by means of the feedback circuit. The capacity gauges [17] and tensogauges [18], photodetectors [19] or optical interferometers can be used in the capacity of displacement gauges.


Fig. 3. The surface deduction of 2-d order from SPM surface image.

The second more simple method is in the use of such nonlinear voltages for piezoceramics that scanner resultant displacement should be approximately linear one. For this the scanner should be previously standardized, i.e. the function of displacement dependence on applied voltage is found. The
scanner calibration is usually carried out with use of samples with periodic structures of before known sizes (so-called testobjects). However, in spite of this, not all distortions can be excluded on hardwire level. In particular, as it is above mentioned, the scanner movement in sample plane influences on probe position over surface (on Z axis), SPM images present themselves the superposition of real relief and some surface of $2 d$ (and higher) order.

For exclusion of such type distortions by the lest square method the approximating surface of $2 d$ order $P^{(2)}(x, y)$ having the minimal inclinations from inital functions $Z=f(x, y)$ is found and further, the given surface is deducted from initial SPM-image: $Z_{i j}^{\prime}=Z_{i j}-P_{i j}^{(2)}$. The deduction result of surface of $2 d$ order from real surface AFM-image [20] is presented on fig.3. The one more type of distortions is connected with nonlinearity and nonorthogonality of scanner displacement in X,Y plane. This leads to distortion of geometric proportions in different parts of SPM surface image. For exclusion of such distortions the correction procedure of SPM images with the help of correction factor fail which is formed at scanning by concrete scanner of test structures with well known relief is carried out. Concerning scanner resonance frequency then
it is necessary to increase it as possible. For example, the resonance eigenfrequency $\omega$ of tube piezoscanner is defined as follows: $\omega=\frac{1}{2 \pi} \frac{(1,875)^{2}}{l^{2}} \sqrt{\frac{E I_{z}}{m}}$,
where $I_{z}$ is inertia moment relative to Z axis, $l$ is length, $m$ is mass, $E=c^{2} \rho$ is Young's modulus, c is sound velocity in piezoceramics, $\rho$ is piezoceramic density. As it is seen from the formula, the increase of scanner displacement range because of the increase of its length leads to quadratic decrease of its resonance frequency. The scanners with high value of resonance frequency, firstly, are better defended from external vibration influence and secondary, allows us to follow signals in enough wide frequency band with delicacy. This gives the possibility to establish the scanning high velocity decreasing the time necessary for obtaining of information. The scanning time decrease of the given region is comfortable for one side, and is of the fundamental importance as at the harmful influence of temperature drift decreases from another one.
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# THE STRUCTURE FUNCTIONS FOR LARGE- $P_{T}$ HADRON PRODUCTION IN SEMI-INCLUSIVE DIS 

S.K. ABDULLAYEV, A.I. MUKHTAROV, M.Sh. GOJAYEV<br>Baku State University, AZ-1148, Z.Halilov str., 23, m_qocayev@mail.ru

We calculate, within perturbative QCD the expressions for unpolarized and polarized structure functions for large- $p_{T}$ baryon production in semi-inclusive DIS. After deriving the complete set of the polarized cross-section which is differential with respect to the transverse momentum, we discuss characteristic features of the azimuthal spin asymmetries, using existing parton densities and fragmentation functions at COMPASS and EIC energies.

Keywords: semi-inclusive deep inelastic scattering, double spin asymmetry, distribution and fragmentation functions
PACS: 10-29

## 1. INTRODUCTION

The standard model of the electroweak interactions of the elementary particles has achieved a great success in the description of series of the experiments, which have been carried out in the various laboratories of the world. In particular, one of its exact checking has been alone on the $e^{-} e^{+}$-colliders LEP and SLC, as the result of which the agreement with the experimental data has been obtained. Alongside with $e^{-} e^{+}$-annihilation the deep-inelastic scattering (DIS) processes of the polarized leptons on the polarized nucleons play the important role in the check of standard theory and they are intensive investigated at the present time [1-15].

In this paper we study the structure functions for the polarized baryon production in polarized semi-inclusive DIS off nucleon

$$
\begin{align*}
& e^{-}\left(\lambda_{e}\right)+N\left(\lambda_{N}\right) \Rightarrow e^{-}+B\left(\lambda_{B}\right)+X  \tag{1}\\
& \left(B=\Lambda, \Sigma^{ \pm}\right)
\end{align*}
$$

where $\lambda_{e}$ is the electron spirality, $\lambda_{N}$ and $\lambda_{B}$ are the longitudinal polarizations of nucleon-target and baryon $B$. In order that a final hadron carries large transverse momentum, another parton has to be emitted in the opposite directions. This is on $O\left(\alpha_{s}\right)$ effect in perturbative QCD and was investigated in [15] for the unpolarized semi-inclusive DIS with electron and neutrino beams. Here we extend the analysis to the polarized cases and study the polarization of baryons in semi-inclusive DIS processes. We stress that the polarization of baryons is an important source of new information.

## 2. THE HADRON FRAME

The momenta of particles are defined in Fig. 1. We define five Lorentz invariants for specifying the kinematics. The center of mass energy $S$ for the initial lepton and the nucleon is

$$
\begin{equation*}
s=(k+P)^{2} \approx 2(k P) \tag{2}
\end{equation*}
$$

where we ignored masses. Conventional DIS variables

$$
\begin{gather*}
x_{B}=\frac{Q^{2}}{2(q P)},  \tag{3}\\
Q^{2}=-q^{2}=-\left(k-k^{\prime}\right)^{2} . \tag{4}
\end{gather*}
$$

are determined by observing the final lepton. For the description of kinematics of the final hadron $B$, we introduce

$$
\begin{equation*}
z_{B}=\frac{\left(P P_{B}\right)}{(q P)} \tag{5}
\end{equation*}
$$

and the transverse component of $q$ which is orthogonal to $P$ и $P_{B}$ :

$$
\begin{equation*}
q_{t}^{\mu}=q^{\mu}-\frac{\left(q P_{B}\right)}{\left(P P_{B}\right)} P^{\mu}-\frac{(q P)}{\left(P P_{B}\right)} P_{B}^{\mu} \tag{6}
\end{equation*}
$$



Fig. 1. Feynman diagram for $e^{-} N \Rightarrow e^{-} B X$


Fig. 2. The hadron frame
$q_{t}^{\mu}$ is a space-like vector and we define its magnitude as

$$
\begin{equation*}
q_{T}=\sqrt{-q_{t}^{2}} \tag{7}
\end{equation*}
$$

In the parton model, there are no bremsstrahlung partons and all parton momenta are exactly collinear with the corresponding hadron momenta, so one has $q_{t}^{\mu}=0$. At the order $\alpha_{S}$, parton emission makes $q_{t}^{\mu}$ nonzero, in general. We will give formulas for the distribution of events as a function of $q_{T}^{2}$.

Define the hadron frame as follows, as pictured in Fig. 2. In the hadron frame, the time-component of the virtual photon momentum is zero and its space-components lie along the negative $z$-axis:

$$
\begin{equation*}
q^{\mu}=(0,0,0,-Q) \tag{8}
\end{equation*}
$$

where

$$
\begin{equation*}
Q=\sqrt{-q^{2}} \tag{9}
\end{equation*}
$$

The space-components of momenta of the incoming nucleon are exactly along the positive $z$-axis in the hadron frame. Then the components of $P$ in the hadron frame are:

$$
\begin{equation*}
P^{\mu}=\frac{Q}{2 x_{B}}(1,0,0,1) . \tag{10}
\end{equation*}
$$

We align the $x$-axis of the hadron frame so that the space-components of $P_{B}^{\mu}$ lie in the $x-z$ plane, with $P_{B}^{x}>0$. The direction of $P_{B}^{\mu}$ as seen from the hadron frame is fixed once $q_{T} / Q$ is given. One finds easily that $P_{B}^{\mu}$ can be written as

$$
\begin{equation*}
P_{B}^{\mu}=\frac{1}{2} z_{B} Q\left(1+\frac{q_{T}^{2}}{Q^{2}}, 2 \frac{q_{T}}{Q}, 0, \frac{q_{T}^{2}}{Q^{2}}-1\right) \tag{11}
\end{equation*}
$$

In order to write the lepton momentum in the hadron frame, we need to in introduce the azimuthal angle $\Phi$ between the hadron plane and the lepton plane. Then the lepton momentum can be parameterized as

$$
\begin{equation*}
k^{\mu}=\frac{1}{2} Q(\cosh \psi, \sinh \psi \cos \Phi, \sinh \psi \sin \Phi,-1) \tag{12}
\end{equation*}
$$

and

$$
\begin{equation*}
k^{\prime \mu}=k^{\mu}-q^{\mu}=\frac{1}{2} Q(\cosh \psi, \sinh \psi \cos \Phi, \sinh \psi \sin \Phi,+1) \tag{13}
\end{equation*}
$$

with

$$
\begin{equation*}
\cosh \psi=\frac{2 x_{B} s}{Q^{2}}-1 . \tag{14}
\end{equation*}
$$

With this definitions, the cross section for (1) can be expressed in terms of $s, x_{B}, Q^{2}, z_{h}, q_{T}^{2}$ and $\Phi$ in the hadron frame.

## 3. THE DIFFERENTIAL CROSS SECTION

The differential cross section for the semi-inclusive hadron production (1) can be written as

$$
\begin{equation*}
d \sigma=\frac{1}{2 s} \cdot \frac{d^{3} P_{B}}{(2 \pi)^{3} 2 E_{B}} \cdot \frac{d^{3} k^{\prime}}{(2 \pi)^{3} 2 E^{\prime}} \cdot \frac{e^{4}}{q^{4}} L_{\mu \nu}\left(k, k^{\prime}\right) W^{\mu \nu}\left(P, P_{B}, q\right) \tag{15}
\end{equation*}
$$

where $L_{\mu \nu}$ is the lepton tensor defined as

$$
\begin{equation*}
L_{\mu \nu}\left(k, k^{\prime}\right)=2\left[k_{\mu} k_{\nu}^{\prime}+k_{\mu}^{\prime} k_{v}-g_{\mu \nu}\left(k k^{\prime}\right)-i \lambda_{e} \varepsilon_{\mu \nu \rho \sigma} k^{\rho} k^{\prime \sigma}\right] \tag{16}
\end{equation*}
$$

$W^{\mu \nu}\left(P, P_{B}, q\right)$ is the hadronic tensor.
Using Lorentz invariance, current conservation and the hermiticity of the current operator, we express hadronic tensor $W^{\mu \nu}$ in a basis of nine independent structure functions $F_{k}, G_{k}, H_{k}, I_{k}$ :

$$
\begin{equation*}
W^{\mu \nu}=\sum_{k=1}^{9} W_{k}^{\mu \nu}\left[F_{k}+\lambda_{N} G_{k}+\lambda_{B} H_{K}+\lambda_{N} \lambda_{B} I_{K}\right], \tag{17}
\end{equation*}
$$

here $W_{k}^{\mu v}(k=1 \div 9)$ are nine tensors constructed from $P^{\mu}, P_{B}^{\mu}$ and $q^{\mu}$. The structure functions $F_{k}$ and $G_{k}, H_{k}$ and $I_{k}$ contain the information about hadrons. They depend only on the invariants $x_{B}, Q^{2}, z_{B}$ and $q_{T}$.

To construct the tensors $W_{k}^{\mu \nu}$, we make use of the vectors $T^{\mu}, X^{\mu}, Y^{\mu}$ and $Z^{\mu}$, defined as:

$$
\begin{align*}
T^{\mu} & =\frac{1}{Q}\left(q^{\mu}+2 x_{B} P^{\mu}\right) \\
X^{\mu} & =\frac{1}{q_{T}}\left[\frac{1}{z_{B}} P_{B}^{\mu}-q^{\mu}-\left(1+\frac{q_{T}^{2}}{Q^{2}}\right) x_{B} P^{\mu}\right] \tag{18}
\end{align*}
$$

$$
Y^{\mu}=\varepsilon^{\mu \nu \rho \sigma} Z_{v} X_{\rho} T_{\sigma}, Z^{\mu}=-\frac{q^{\mu}}{Q}
$$

These vectors are orthogonal to one another and normalized to $T_{\mu} T^{\mu}=1, \quad X_{\mu} X^{\mu}=-1, \quad Y_{\mu} Y^{\mu}=-1$, $Z_{\mu} Z^{\mu}=-1$. Note that $T^{\mu}, X^{\mu}$ and $Z^{\mu}$ are vectors, while $Y^{\mu}$ is an axial vector. Since $W_{k}^{\mu v}$ satisfies the current conservation, $q_{\mu} W^{\mu \nu}==q_{\nu} W^{\mu \nu}=0$, it is easy to see that $W^{\mu \nu}$ can be expanded in terms of nine independent tensors, for which we employ the following:

$$
\begin{align*}
& W_{1}^{\mu \nu}=X^{\mu} X^{v}+Y^{\mu} Y^{v}, \\
& W_{2}^{\mu \nu}=g^{\mu \nu}+Z^{\mu} Z^{v} \\
& W_{3}^{\mu v}=T^{\mu} X^{v}+X^{\mu} T^{v}, \\
& W_{4}^{\mu v}=X^{\mu} X^{v}-Y^{\mu} Y^{v}, \\
& W_{5}^{\mu \nu}=i\left(T^{\mu} X^{v}-X^{\mu} T^{v}\right),  \tag{19}\\
& W_{6}^{\mu v}=i\left(X^{\mu} Y^{v}-Y^{\mu} X^{v}\right), \\
& W_{7}^{\mu \nu}=i\left(T^{\mu} Y^{v}-Y^{\mu} T^{v}\right), \\
& W_{8}^{\mu v}=T^{\mu} Y^{v}+Y^{\mu} T^{v}, \\
& W_{9}^{\mu v}=X^{\mu} Y^{v}+Y^{\mu} X^{v} .
\end{align*}
$$

The first five of these tensors are even under a parity transformation while tensors 6 through 9 are odd under parity.

Tensors $W_{1,2,3,4,8,9}^{\mu \nu}$ are symmetric under interchange of $\mu$ and $\nu$ while tensors $W_{5,6,7}^{\mu \nu}$ are antisymmetric.

One can sort the tensors according to their properties under rotations about the $Z$-axis. The tensors $W_{1}^{\mu \nu}, W_{2}^{\mu \nu}$ and $W_{\sigma}^{\mu \nu}$ are invariant under such rotations and this carry angular momentum zero. The tensors $W_{3}^{\mu \nu}, W_{5}^{\mu \nu}, W_{7}^{\mu \nu}$ and $W_{8}^{\mu \nu}$ carry angular momentum $\pm 1$, while $W_{4}^{\mu \nu}$ and $W_{9}^{\mu \nu}$ carry angular momentum $\pm 2$.

In order express $L_{\mu \nu} W^{\mu \nu}$ in term of the structure functions $F_{k}, G_{k}, H_{k}$ and $I_{k}$, we write the products $L_{\mu \nu} W_{k}^{\mu \nu}$ in the form

$$
\begin{equation*}
A_{k}=\frac{1}{Q^{2}} L_{\mu \nu} W_{k}^{\mu v} \tag{20}
\end{equation*}
$$

The $A_{k}$ are then functions of the angles $\Phi$ and $\psi[14]$ :

$$
\begin{align*}
& A_{1}=(+1) \cdot\left(1+\cosh ^{2} \psi\right) \\
& A_{2}=-2 \\
& A_{3}=(-1) \cdot \cos \Phi \cdot \sinh 2 \psi \\
& A_{4}=(+1) \cdot \cos 2 \Phi \cdot \sinh ^{2} \psi \\
& A_{5}=(-2) \cdot \sin \Phi \cdot \sinh \psi \cdot \lambda_{e}  \tag{21}\\
& A_{6}=(-2) \cosh \psi \cdot \lambda_{e} \\
& A_{7}=(+2) \cdot \cos \Phi \cdot \sinh \psi \cdot \lambda_{e} \\
& A_{8}=(+1) \cdot \sin \Phi \cdot \sinh 2 \psi \\
& A_{9}=(-1) \cdot \sin 2 \Phi \cdot \sinh ^{2} \psi
\end{align*}
$$

There of the structure functions, namely $F_{k}, G_{k}, H_{k}, I_{k}(k=5,8,9)$ are zero at order $\alpha_{s}$ of perturbation theory. All these structure functions are odd functions of $\Phi$ : either $\sin \Phi$, or $\sin 2 \Phi$.

By applying the method described above, we finally obtain the cross section for the large- $p_{T}$ hadron production in DIS in the following form:

$$
\begin{align*}
& \frac{d \sigma}{d x_{B} d Q^{2} d z_{B} d q_{T}^{2} d \Phi}=\frac{\alpha_{e}^{2}}{16 \pi x_{B}^{2} s^{2} Q^{2}}\left\{\left[\left(1+\cosh ^{2} \psi\right)\left(F_{1}+\lambda_{N} \lambda_{B} I_{1}\right)-2\left(F_{2}+\lambda_{N} \lambda_{B} I_{2}\right)-\right.\right. \\
& -\cos \Phi \cdot \sinh 2 \psi\left(F_{3}+\lambda_{N} \lambda_{B} I_{3}\right)+\cos 2 \Phi \sinh ^{2} \psi\left(F_{4}+\lambda_{N} \lambda_{B} I_{4}\right)- \\
& \left.-2 \cosh \psi \cdot \lambda_{e}\left(\lambda_{N} G_{6}+\lambda_{B} H_{6}\right)+2 \cosh \psi \cdot \sinh \psi \cdot \lambda_{e}\left(\lambda_{N} G_{7}+\lambda_{B} H_{7}\right)\right\} \tag{22}
\end{align*}
$$

The effective section (22) contains 4 unpolarized ( $F_{1}, F_{2}, F_{3}$ and $F_{4}$ ) and 8 polarized ( $\left.I_{1}, I_{2}, I_{3}, I_{4}, G_{6}, G_{7}, H_{6}, H_{7}\right)$ SF. Let's discuss the possibilities of information obtaining about those and other functions. SF depend on $Q^{2}, x_{B}, q_{T}^{2}$ and $z_{B}$ variables, that's why the experimental study of baryon azimuthal distribution over $\Phi$ allows us to define $\mathrm{SF} F_{1}, F_{2}, F_{3}$ and $F_{4}$. For example, azimuthal angle symmetries

$$
\begin{align*}
& \langle\cos \Phi\rangle=-\frac{(2-y) \sqrt{1-y} F_{3}}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}},  \tag{23}\\
& \langle\cos 2 \Phi\rangle=\frac{(1-y) F_{4}}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}} \tag{24}
\end{align*}
$$

are information sources about $\mathrm{SF} F_{3}$ and $F_{4}$, here $y=\frac{Q^{2}}{x_{B} S}$ variable is introduced.
The degree of baryon longitudinal polarization at deep-inelastic scattering of longitudinal polarized electron on unpolarized nucleon is obtained as follows:

$$
\begin{gather*}
P\left(\lambda_{e}, \Phi\right)=\frac{d \sigma\left(\lambda_{e}, \lambda_{B}=1\right)-d \sigma\left(\lambda_{e}, \lambda_{B}=-1\right)}{d \sigma\left(\lambda_{e}, \lambda_{B}=1\right)+d \sigma\left(\lambda_{e}, \lambda_{B}=-1\right)}= \\
=\lambda_{e} \cdot \frac{-y(2-y) H_{6}+2 y \sqrt{1-y} H_{7} \cdot \cos \Phi}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}-2(2-y) \sqrt{1-y} F_{3} \cos \Phi+2(1-y) F_{4} \cdot \cos 2 \Phi} \tag{25}
\end{gather*}
$$

It can give the information about polarized SF $H_{6}$ and $H_{7}$.
At scattering of longitudinal polarized electron on polarized nucleon, the two-spin symmetry

$$
\begin{gather*}
A(\Phi)=\frac{d \sigma\left(\lambda_{e}, \lambda_{N}=1\right)-d \sigma\left(\lambda_{e}, \lambda_{N}=-1\right)}{d \sigma\left(\lambda_{e}, \lambda_{N}=1\right)+d \sigma\left(\lambda_{e}, \lambda_{N}=-1\right)}= \\
=\frac{-y(2-y) G_{6}+2 y \sqrt{1-y} H_{7} \cos \Phi}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}-2(2-y) \sqrt{1-y} F_{3} \cdot \cos \Phi+2(1-y) F_{4} \cos 2 \Phi} \tag{26}
\end{gather*}
$$

contains the information about polarized SF $G_{6}$ and $G_{7}$.
The degree of baryon longitudinal polarization at deep-inelastic scattering of longitudinal polarized electron on unpolarized nucleon is the information source about polarized $\mathrm{SF} I_{1}, I_{2}, I_{3}$ and $I_{4}$ :

$$
\begin{gather*}
P\left(\lambda_{N}, \Phi\right)=\frac{d \sigma\left(\lambda_{N}, \lambda_{B}=1\right)-d \sigma\left(\lambda_{N}, \lambda_{B}=-1\right)}{d \sigma\left(\lambda_{N}, \lambda_{B}=1\right)+d \sigma\left(\lambda_{N}, \lambda_{B}=-1\right)}= \\
=\lambda_{N} \frac{\left[1+(1-y)^{2}\right] I_{1}-y^{2} I_{2}-2(2-y) \sqrt{1-y} I_{3} \cdot \cos \Phi+2(1-y) I_{4} \cos 2 \Phi}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}-2(2-y) \sqrt{1-y} F_{3} \cdot \cos \Phi+2(1-y) F_{4} \cos 2 \Phi} \tag{27}
\end{gather*}
$$

It is necessary to note that SF of hadrons don't depend on azimuthal angle of baryon takeoff, therefore they are easily defined by integration over the angle of $\Phi$ of baryon longitudinal polarizations degrees $P\left(\lambda_{e}\right), P\left(\lambda_{N}\right)$ and two-spin symmetry $A$ :

$$
\begin{align*}
& P\left(\lambda_{e}\right)=-\lambda_{e} \frac{y(2-y) H_{6}}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}},  \tag{28}\\
& P\left(\lambda_{N}\right)=\lambda_{N} \frac{\left[1+(1-y)^{2}\right] I_{1}-y^{2} I_{2}}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}},  \tag{29}\\
& A=-\frac{y(2-y) G_{6}}{\left[1+(1-y)^{2}\right] F_{1}-y^{2} F_{2}}, \tag{30}
\end{align*}
$$

Within frameworks of perturbation QCD we define SF of hadrons and carry out the evaluations of longitudinal polarization degrees $P\left(\lambda_{e}\right)$ and $P\left(\lambda_{N}\right)$.


Fig. 3.
Lowest order diagram in the QCD coupling relevant for the processes (1) is shown in Fig. 3. The leading twist-2 contribution to the hadronic tensor $W^{\mu \nu}$ can be written as

$$
\begin{align*}
& W^{\mu \nu}\left(P, P_{B}, q\right)=\int_{0}^{1} \frac{d x}{x} \int_{0}^{1} \frac{d z}{z} \boldsymbol{\operatorname { r r }}\left[M_{A}\left(x, P, \lambda_{N}\right) \hat{M}_{B}\left(z, P_{B}, \lambda_{B}\right) H^{\mu \nu}\left(x P, P_{B} / z, q\right)\right] \times  \tag{31}\\
& \times 2 \pi \delta\left(\left(x P+q-P_{B} / z\right)^{2}\right)
\end{align*}
$$

where $M_{A}\left(x, P, \lambda_{N}\right)$ and $M_{B}\left(z, P_{B}, \lambda_{B}\right)$ are the distribution and fragmentation functions for nucleon $N$ and baryon $B$, respectively, and $H^{\mu v}\left(x P_{N}, P_{B} / z, q\right)$ is the corresponding hard part. $T r$ indicates the trace over relevant spinor. Since we are interested in the twist-2 cross sections, $P$ and $P_{B}$ can be regarded as light-like to define the complete set of distribution and fragmentation functions, we introduce another set of vectors $n\left(n^{2}=0\right)$ and $\omega\left(\omega^{2}=0\right)$ for $P$ and $P_{B}$, respectively, by the relation $(P n)=1$ and $\left(P_{B} \omega\right)=1$. The complete set of the twist-2 quark distribution for the proton is defined as [14].

$$
\begin{equation*}
M_{i j}^{q}\left(x, P, \lambda_{N}\right)=\int \frac{d \lambda}{2 \pi} e^{i \lambda x}<P \lambda_{N}\left|\bar{\psi}_{j}(0) \psi_{i}(\lambda n)\right| P \lambda_{N}>==\frac{1}{2} \hat{P} q(x)+\frac{1}{2} \lambda_{N} \gamma_{5} \hat{P} \Delta q(x)+\ldots, \tag{32}
\end{equation*}
$$

where $q(x)$ and $\Delta q(x)$ are, respectively, spin-average and longitudinally polarized quark distribution.
The gluon distribution is also defined as [14]

$$
\begin{align*}
& M_{g}^{\alpha \beta}\left(x, P, \lambda_{N}\right)=\frac{2}{x^{2}} \int \frac{d \lambda}{2 \pi} e^{i \lambda x}<P \lambda_{N}\left|\operatorname{tr}\left[n_{\rho} G^{\rho \alpha}(0) n_{\sigma} G^{\sigma \beta}(\lambda n)\right]\right| P \lambda_{N}>= \\
& =-\frac{1}{2 x} G(x) g_{A \perp}^{\alpha \beta}-\frac{1}{2 x} \Delta G(x) i \varepsilon^{\alpha \beta \rho \sigma} P_{\rho} n_{\sigma} \tag{33}
\end{align*}
$$

where $G^{\rho \alpha}$ is the gluon's field strength, $\operatorname{tr}$ means the trace over the color index for $G^{\rho \alpha}, g_{A \perp}^{\alpha \beta}=g^{\alpha \beta}-P^{\alpha} n^{\beta}-n^{\alpha} P^{\beta}$, $G(x)$ and $\Delta G(x)$ are, respectively, spin-average and longitudinally polarized gluon distributions.

Similarly we define twist-2 quark and gluon fragmentation functions for the spin $-1 / 2$ baryon $B$ [14]:

$$
\begin{align*}
& M_{B i j}^{q}\left(z, P_{B}, \lambda_{B}\right)=\frac{1}{N_{C}} \sum_{X} \int \frac{d \lambda}{2 \pi} e^{-i \lambda / z}<0\left|\psi_{i}(0)\right| B X><B X\left|\bar{\psi}_{j}(\lambda \omega)\right| 0>= \\
& =\frac{1}{z} \hat{P}_{B} q(z)+\frac{1}{z} \lambda_{B} \gamma_{5} \hat{P}_{B} \Delta q(z) \tag{34}
\end{align*}
$$

$$
\begin{align*}
& M_{B}^{g \alpha \beta}\left(z, P_{B}, \lambda_{B}\right)=\frac{2 z^{2}}{N_{C}^{2}-1} \sum_{X} \int \frac{d \lambda}{2 \pi} e^{-i \lambda / z}<0\left|\operatorname{tr}\left[\omega_{\rho} G^{\rho \alpha}(0)|B X><B X| \omega_{\sigma} G^{\sigma \beta}(\lambda \omega)\right]\right| 0>=  \tag{35}\\
& =-G(z) g_{B \perp}^{\alpha \beta}-\Delta G(z) i \varepsilon^{\alpha \beta \rho \sigma} P_{B \rho} \omega_{\sigma}
\end{align*}
$$

where $g_{B \perp}^{\alpha \beta}=g^{\alpha \beta}-P_{B}^{\alpha} \omega^{\beta}-\omega^{\alpha} P_{B}^{\beta}$.
By applying the method described above, we finally obtain the SF for the large- $p_{T}$ baryon production in DIS in the following form:

$$
\begin{equation*}
F_{k}\left(G_{k}, H_{k}, I_{k}\right)=\alpha_{S} \int_{x_{\text {min }}}^{1} \frac{d x}{x} \int_{z_{h}}^{1} \frac{d z}{z} f_{k}\left(g_{k}, h_{k}, i_{k}\right) \delta\left(\frac{q_{T}^{2}}{Q^{2}}-\left(\frac{1}{\hat{x}}-1\right)\left(\frac{1}{\hat{z}}-1\right)\right) \tag{36}
\end{equation*}
$$

In (35) $f_{k}\left(g_{k}, h_{k}, i_{k}\right)$ should read the following form $\left(C_{F}=4 / 3\right)$ :

$$
\begin{align*}
& f_{k}=\sum_{q} e_{q}^{2}\left\{q(x) q(z) f_{k}^{q q}+G(x) q(z) f_{k}^{g q}+q(x) G(z) f_{k}^{q g}\right\},  \tag{37}\\
& g_{k}=\sum_{q} e_{q}^{2}\left\{\Delta q(x) q(z) g_{k}^{q q}+\Delta G(x) q(z) g_{k}^{g q}+\Delta q(x) G(z) g_{k}^{q g}\right\},  \tag{38}\\
& h_{k}=\sum_{q} e_{q}^{2}\left\{q(x) \Delta q(z) h_{k}^{q q}+G(x) \Delta q(z) h_{k}^{g q}+q(x) \Delta G(z) h_{k}^{q g}\right\},  \tag{39}\\
& i_{k}=\sum_{q} e_{q}^{2}\left\{\Delta q(x) \Delta q(z) i_{k}^{q q}+\Delta G(x) \Delta q(z) i_{k}^{g q}+\Delta q(x) \Delta G(z) i_{k}^{q g}\right\},  \tag{40}\\
& f_{l}^{q q}=2 C_{F} \hat{x} \hat{z}\left[\frac{1}{Q^{2} q_{T}^{2}}\left(\frac{Q^{4}}{\hat{x}^{2} \hat{z}^{2}}+\left(Q^{2}-q_{T}^{2}\right)^{2}\right)+6\right] \text {, } \\
& f_{2}^{q q}=2 f_{4}^{q q}=8 C_{F} \hat{x} \hat{z}, \\
& f_{3}^{q q}=4 C_{F} \hat{x} \hat{z} \frac{1}{Q q_{T}}\left(Q^{2}+q_{T}^{2}\right) \text {, } \\
& f_{1}^{g q}=\hat{x}(1-\hat{x})\left[\frac{Q^{2}}{q_{T}^{2}}\left(\frac{1}{\hat{x}^{2} \hat{z}^{2}}-\frac{2}{\hat{x} \hat{z}}+2\right)+10-\frac{2}{\hat{x}}-\frac{2}{\hat{z}}\right], \\
& f_{2}^{g q}=2 f_{4}^{g q}=8 \hat{x}(1-\hat{x}) \text {, } \\
& f_{3}^{g q}=\hat{x}(1-\hat{x}) \frac{2}{Q q_{T}}\left[2\left(Q^{2}+q_{T}^{2}\right)-\frac{Q^{2}}{\hat{x} \hat{z}}\right], \\
& f_{l}^{q g}=2 G_{F} \hat{x}(1-\hat{z})\left[\frac{1}{Q^{2} q_{T}^{2}}\left(\frac{Q^{2}}{\hat{x}^{2} \hat{z}^{2}}+\frac{(1-\hat{z})^{2}}{\hat{z}^{2}}\left(Q^{2}-\frac{z^{2} q_{T}^{2}}{(1-\hat{z})^{2}}\right)\right)+6\right] \text {, } \\
& f_{2}^{q g}=2 f_{4}^{q g}=8 C_{F} \hat{x}(1-\hat{z}) \text {, } \\
& f_{3}^{q g}=4 C_{F} \hat{x}(1-\hat{z})^{2} \frac{1}{\hat{z} Q q_{T}}\left[Q^{2}+\frac{\hat{z}^{2} q_{T}^{2}}{(1-\hat{z})^{2}}\right] ; \\
& g_{6}^{q q}=-2 C_{F}\left[\left(\frac{1}{\hat{x} \hat{z}}+\hat{x} \hat{z}\right) \frac{Q^{2}}{q_{T}^{2}}-\frac{\hat{x} \hat{z}, q_{T}^{2}}{Q^{2}}\right] \text {, } \\
& g_{7}^{q q}=-4 C_{F} \hat{x} \hat{z} \frac{Q^{2}-q_{T}^{2}}{Q q_{T}}, \\
& g_{6}^{g q}=-\frac{2 \hat{x}-1}{\hat{x}}\left(2 \hat{x}+\frac{\hat{x}-1}{\hat{z}^{2}} \cdot \frac{Q^{2}}{q_{T}^{2}}\right),
\end{align*}
$$

$$
\begin{align*}
& g_{7}^{g q}=-2 \frac{Q}{q_{T}} \cdot \frac{(\hat{x}-1)(2 \hat{z}-1)}{\hat{z}}, \\
& g_{6}^{q g}=2 C_{F} \frac{\hat{z}}{\hat{x}-1}\left[\frac{1}{\hat{z}^{2}}-(\hat{x}-1)^{2}+\frac{\hat{x}^{4}}{(\hat{x}-1)^{2}} \cdot \frac{q_{T}^{4}}{Q^{4}}\right],  \tag{42}\\
& g_{7}^{q g}=4 C_{F} \frac{\hat{x} \hat{z}}{\hat{x}-1}\left(1-\frac{\hat{x}}{\hat{z}}\right) \cdot \frac{q_{T}}{Q} . \\
& h_{6,7}^{q q}=g_{6,7}^{q q}, \\
& h_{6}^{g q}=\frac{2 \hat{x}^{2}-2 \hat{x}+1}{\hat{x} \hat{z}}\left(\hat{x}+(\hat{x}-1) \frac{Q^{2}}{q_{T}^{2}}\right), \\
& h_{7}^{g q}=2 \frac{Q}{q_{T}} \frac{(\hat{x}-1)(2 \hat{x}-1)}{\hat{z}}, \\
& h_{6}^{q g}=2 C_{F} \frac{\hat{z}}{\hat{x}-1}\left[\frac{1}{\hat{z}^{2}}+(\hat{x}-1)^{2}-\frac{\hat{x}^{4}}{(\hat{x}-1)^{2}} \cdot \frac{q_{T}^{4}}{Q^{4}}\right],  \tag{43}\\
& h_{7}^{q g}=-4 C_{F} \frac{\hat{x} \hat{z}}{\hat{x}-1}\left(1-\frac{\hat{x}}{\hat{z}}\right) \cdot \frac{q_{T}}{Q}, \\
& i_{k}^{q q}=f_{k}^{q q}(k=1,2,3,4), \\
& i_{l}^{g q}=\frac{2 \hat{x}-1}{\hat{x}(\hat{x}-1)} \frac{Q^{4}(\hat{x}-1)^{2}-q_{T}^{4} \hat{x}^{2}}{Q^{2} q_{T}^{2}}, \\
& i_{3}^{g q}=\frac{2}{Q q_{T}}\left[Q^{2}(\hat{x}-1)-q_{T}^{2} \hat{x}\right], \\
& i_{l}^{q g}=2 C_{F} \hat{\hat{z}}\left[\frac{\hat{x}-2}{\hat{x}-1}+\frac{\hat{x}(\hat{x}+1)}{(\hat{x}-1)^{2}} \frac{q_{T}^{4}}{Q^{4}}+\frac{2\left(2 \hat{x}^{2}-2 \hat{x}+1\right)}{(\hat{x}-1)^{2}} \frac{q_{T}^{2}}{Q^{2}}\right], \\
& i_{2}^{q g}=2 i_{4}^{q g}=8 C_{F} \frac{\hat{x}^{2} \hat{z}}{\hat{x}-1} \cdot \frac{q_{T}^{2}}{Q^{2}}, \\
& i_{3}^{q g}=4 C_{F} \frac{\hat{x} \hat{z}}{(\hat{x}-1)^{2}} \cdot \frac{q_{T}}{Q}\left[(\hat{x}-1)^{2}+\hat{x}^{2} \frac{q_{T}^{2}}{Q^{2}}\right] \tag{44}
\end{align*}
$$

We introduced the variables:

$$
\begin{equation*}
\hat{x}=\frac{x_{B}}{x}, \quad \hat{z}=\frac{z_{B}}{z}, \tag{45}
\end{equation*}
$$

and

$$
\begin{equation*}
x_{\text {min }}=x_{B}\left(1+\frac{z_{B}}{1-z_{B}} \cdot \frac{q_{T}^{2}}{Q^{2}}\right) . \tag{46}
\end{equation*}
$$

For a given $s, Q^{2}$ and $q_{T}$, the kinematic constraint for $x_{B}$ and $z_{B}$ is

$$
\begin{gather*}
\frac{Q^{2}}{s}<x_{B}<1  \tag{47}\\
0<z_{B}<\frac{1-x_{B}}{1-x_{B}\left(1+q_{T}^{2} / Q^{2}\right)} \tag{48}
\end{gather*}
$$

For a given $Q^{2}, x_{B}$ and $z_{B}, q_{T}$ can take

$$
\begin{equation*}
0<q_{T}<Q \sqrt{\left(\frac{1}{x_{B}}-1\right)\left(\frac{1}{z_{B}}-1\right)} . \tag{49}
\end{equation*}
$$

The structure functions $F_{1}, I_{1}, G_{6}$ and $H_{6}$ have a $1 / q_{T}^{2}$ behavior, these terms arise from the emission of partons that are collinear to the incoming parton, collinear to the outgoing parton, or soft. The functions $F_{3}, G_{7}, H_{7}$ and $I_{3}$ gives contributions are of order $1 / q_{T}$.

In the semi-inclusive DIS, contribution from the gluon distribution and fragmentation functions is of the same $O\left(\alpha_{s}\right)$ effect as the quark contribution, so that $q_{T}$ differential cross section is expected to be a more sentitive tool to determine detailed form of the polarized gluon contribution than the $q_{T}$-integrated case.

## 4. NUMERICAL ESTIMATE

The polarizations $P\left(\lambda_{e}\right), P\left(\lambda_{B}\right)$ and asymmetry $A$
are still functions of five variables: $s, Q^{2}, x_{B}, z_{B}$ and $q_{T}$. We estimate them at COMPASS $\left(s=300 \mathrm{GeV}^{2}\right)$ and EIC $\left(s=10^{4} \mathrm{GeV}^{2}\right) \quad$ energies. We have chosen $\left(Q^{2}, x_{B}\right)=\left(100 \mathrm{GeV}^{2}, 0.45\right)$ for the COMPASS energy and $\left(Q^{2}, x_{B}\right)=\left(100 \mathrm{GeV}^{2}, 0.015\right)$ for the EIC energy. We use GRV parton density for the unpolarized nucleon [16], GRSV polarized parton density [17] and FSV $\Lambda$-fragmentation functions [18] for polarized and unpolarized $\Lambda$.

Figure 4 shows the $q_{T}$-dependence and $z_{B^{-}}$ dependence of the longitudinal polarization $P\left(\lambda_{e}\right)$ for $e+p \Rightarrow e+\Lambda+X \quad((a)$ and $(b))$ at the COMPASS kinematics.

Figure 5 shows the same polarizations as Fig. 4 but for


Fig. 4. The longitudinal polarization $P\left(\lambda_{e}=1\right)$ for $e+p \rightarrow e+\Lambda+X$ at the COMPASS energy. (a) and (b) show the $q_{T}-$ dependence and the $z_{B}$-dependence for scenarios $1,2,3$


Fig. 5. The same as Fig. 4 but for EIC energy


Fig. 6. The longitudinal polarization $P\left(\lambda_{N}=1\right)$ for $e+p \rightarrow e+\Lambda+X$ at the COMPASS energy. (a) and (b) show the $q_{T}-$ dependence and the $z_{B}$-dependence for scenarios $1,2,3$


Fig. 7. The same as Fig. 6 but for EIC energy
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# DIELECTRIC PROPERTIES OF DUAL-FREQUENCY LIQUID CRYSTAL 5CB- C2-H22 

T.D. IBRAGIMOV, A.K. MAMEDOV<br>H.M.Abdullayev Institute of Physics of Azerbaijan National Academy of Sciences AZ1143 H.Javid Avenue, 33, Baku, Azerbaijan

G.M. BAYRAMOV<br>Baku State University<br>AZ1148 Z.Khalilov str, 23, Baku, Azerbaijan


#### Abstract

The novel dual-frequency liquid crystal (LC) consisting of LC 4-n-pentyl-4'-cyanobiphenyl (5CB) with positive dielectric anisotropy and two LCs 4-hexyloxyphenyl ester 4'-hexyloxy-3-nitrobenzoic acid (C2) and 4-n-pentanoyloxy-benzoic acid-4'-hexyloxyphenyl ester (H 22) with negative dielectric anisotropies was developed. Meanwhile, the interval of the LC phase of the mixture was extended within $11-65$ ${ }^{\circ} \mathrm{C}$. Temperature dependences of dielectric permeability components of the $5 \mathrm{CB}-\mathrm{C} 2-\mathrm{H} 22$ mixture and also the crossover frequency were defined. It was shown that an increase in temperature of the sample leads to reduction of perpendicular component of dielectric permeability and an increase in crossover frequency. The last is characterized by the activation energy connected with rotations of the long molecular axes.


Keywords: dual-frequency liquid crystal, crossover frequency, activation energy, permeability
PACS: 77.84.Nh, 78.28.Jq, 61.30.Gd, 61.30.Eb

## INTRODUCTION

Optical properties of a well-aligned layer of a liquid crystal (LC) are characterized by extraordinary $n_{e}$ and ordinary $\mathbf{n}_{0}$ refractive indices. Meanwhile, the difference $\Delta \varepsilon$ between dielectric permeabilities $\varepsilon_{\|}$and $\varepsilon \perp$, corresponding to extraordinary and ordinary refractive indices, defines dielectric anisotropy of the LC. It is necessary to note that $\varepsilon_{\|}$ and $\varepsilon \perp$ are components of the dielectric permeability measured along and perpendicular to the direction of LC long molecular axes called by the director.

Dual-frequency liquid crystal (DFLC) represents a mixture consisting of molecules of liquid crystals with positive and negative dielectric anisotropies. The sign of dielectric anisotropy of such mixture can change from positive to negative magnitudes at a change of electric field frequency. Possibility of sign inversion of dielectric anisotropy on some crossover frequency $f_{t}$ allows operating the switching processes in LC. Meanwhile, dielectric anisotropy on low frequencies $\left(f<f_{t}\right)$ has a positive sign and it has negative one at high frequencies $\left(f>f_{t}\right)$. With an increase of the applied electric field frequency, $\varepsilon_{\|}$decreases while $\varepsilon \perp$ remains invariable. Thus, there is a reorientation of molecular dipoles of LC with the positive dielectric anisotropy in parallel to an electric field vector at application of low frequency field to the DFLC layer with the parallel-directed orientation of molecules. The application of voltage with the high frequency causes reorientation of molecular dipoles of LC molecules with negative dielectric anisotropy in orthogonal direction to the vector of electric field. As a result, there is a process of a relaxation of molecules and returning of LC director to the starting position.

Use of DFLC expands a span of electrooptical effects and possibility of application of LC in various electrooptical devices. In particular, the DFLC system in combination with the polymer, having refractive index equal to ordinary refractive index of LC, allows operating the transmission of an electrooptical cell [1]. The small particles - DFLC system is used for a filtration and modulation of infra-red radiation [2-4].

In work [5] it is informed about obtaining of plasmon modulators of high-contrast signals based on DFLC in work [5]. Authors of paper [6] have developed DFLC with high two-refraction and ultralow crossover frequency which can be used at the elevated temperatures. The method of phase modulation with the high speed using dual-frequency liquid crystals is described in work [7]. This system uses an electronic feedback connection in order to simplify the control. For large phase shifts, phase modulation speeds are an order of magnitude faster than for existing techniques. Thus, synthesis of the two-frequency liquid crystal mixture possessing a wide temperature interval of the mesogene phase, great magnitudes of dielectric anisotropy, low value of crossover frequency and small switching times will create possibilities not only for improvement of operated characteristics of existing electrooptical devices but also designing of novel type of similar devices.

In the given work, the results of study of dielectric parameters of the novel synthesized dual-frequency liquid crystal are reported.

## EXPERIMENTAL

Three-component mixture of following liquid crystals was used for obtaining of dual-frequency LC:
4-n-pentyl-4'-cyanobiphenyl (5CB) with $\Delta \varepsilon=+11.5$, sequence of phase transitions $\mathrm{Cr} 18^{\circ} \mathrm{C} \mathrm{N} 35,2^{\circ} \mathrm{C}$ I, and structural formula


4-hexyloxyphenyl ester 4'-hexyloxy-3-nitrobenzoic acid (C2) with $\Delta \varepsilon=-8.5$, sequence of phase transitions $\mathrm{Cr} 36^{\circ} \mathrm{C} \mathrm{S} \mathrm{A}_{\mathrm{A}} 71^{\circ} \mathrm{C} \mathrm{I}$, and structural formula


4-n-pentanoyloxy-benzoic acid-4'-hexyloxyphenyl ester (H 22) with $\Delta \varepsilon=-2.6$, sequence of phase transitions $\mathrm{Cr} 44^{\circ} \mathrm{C} \mathrm{N}$ $75^{\circ} \mathrm{C} \mathrm{I}$, and structural formula

and molar ratio of $1: 1$ : 1.5 , correspondingly. Observation under polarization microscope showed that the mixture has nematic phase in the temperature range of $11-65^{\circ} \mathrm{C}$.

A study of frequency dependence of dielectric permeability of a mixture 5CB - C2-H22 was carried out in cells with substrates from conductive glasses. Meanwhile, dependences $\varepsilon \perp$ and $\varepsilon_{\|}$on frequency were measured with working voltage nearby 1 V at planar and homeotropic orientations of LC molecules, accordingly. Planar orientation of molecules was reached by following manners. The polyamide lacquer was dissolved in dimethyl formamide (5 $\%$ solution) and passed through the glass filter. The drop of the obtained solution was put on a plate surface and the system rotated in a centrifuge with frequency of 3000 rpm for a uniform covering. After solvent drying in the drying cupboard, plates were maintained at the temperature $300^{\circ} \mathrm{C}$ within 0,5 hours . After this stage of heat-treatment (polymerization), uniform film of a polyamide lacquer was formed on a substrate surface. Then the film is rubbed by means of a fabric. For obtaining of the homeotropic orientation of LC molecules, a drop of the soap solution of $1 \%$ in hot $\left(60^{\circ} \mathrm{C}\right)$ water fells on a hot substrate from an electrode $\left(\mathrm{SnO}_{2}\right)$ which rotated in a centrifuge with frequency $20 \mathrm{~s}^{-1}$. After that the substrate was dried up in siccative cupboard.

The cell was filled by LC in the isotropic phase and was located in special oven. A temperature of the cell with LC was measured by the copper-constantan thermocouple with accuracy of $0.5^{\circ} \mathrm{C}$. Dielectric permeability was defined from the relation of capacities of the filled and empty cells which in their turn, were measured on the device BM 560 Tesla.

## RESULTS AND DISCUSSION

Frequency dependence of dielectric permeabilities $\varepsilon \perp$ and $\varepsilon_{\|}$of the mixture $5 \mathrm{CB}-\mathrm{C} 2-\mathrm{H} 22$ at temperature $23^{\circ} \mathrm{C}$. is shown on Fig. 1. The dispersion of $\varepsilon \perp$ occurs at very high frequencies ( $\sim 1 \mathrm{MHz}$ ), which is connected with a relaxation of dipole groups -COO. Two dispersions are observed for $\varepsilon_{\| \mid}$. The first of them corresponds to longitudinal component of group - $\mathrm{NO}_{2}$ which begins directly at low frequencies ( $\sim 1$ kHz ). The second relaxation, which occurs at frequencies of 100 kHz , corresponds to relaxation of dipole groups $-\mathrm{C} \equiv \mathrm{N}$. The point of crossing of dispersive curves (crossover frequency) corresponds to transition of the mixture from the state of positive dielectric anisotropy to negative one and makes up $104 \mathrm{\kappa Hz}$ at temperature $23^{\circ} \mathrm{C}$.

Temperature dependence of $\varepsilon \perp$ is shown in Fig.2.


Fig.1. Frequency dependence of dielectric permeabilities $\varepsilon_{\|}$ (a) and $\varepsilon \perp$ (b) of the mixture $5 \mathrm{CB}-\mathrm{C} 2-\mathrm{H} 22$ at temperature $23^{\circ} \mathrm{C}$.


Fig.2.Temperature dependence of dielectric permittivity component $\varepsilon \perp$ of the mixture $5 \mathrm{CB}-\mathrm{C} 2-\mathrm{H} 22$ on the frequency of 40 kHz .

As seen from this figure, an increase in temperature of the sample 5CB - C2 - H22 results in reduction of perpendicular component of dielectric permeability. Temperature dependence of crossover frequency is shown on Fig.3. Apparently, it increases from 90 kHz to 300 kHz at change of temperature from $15^{\circ} \mathrm{C}$ to $50^{\circ} \mathrm{C}$.


Fig.3. Temperature dependence of crossover frequency of a mixture 5CB - C2-H22.


Fig. 4. Dielectric anisotropy as function of temperature of the cell at various frequencies of the applied electric field: a is $50 \mathrm{kHz} ; \mathrm{b}$ is $100 \mathrm{kHz} ; \mathrm{c}$ is 200 kHz ; d is 300 kHz .
$\Delta \varepsilon$ is always positive in a wide frequency range of the applied electric voltage (Fig.4) at high temperatures.

Temperature behavior of crossover frequency can be fitted by a straight line in the inverse-logarithmic coordinates (Fig. 5), that specifies on activation nature of the given change:

$$
f \mathrm{c} \sim \exp \left(-\mathrm{E}_{f} / \mathrm{k}_{\mathrm{B}} \mathrm{~T}\right)
$$

where $\mathrm{k}_{\mathrm{B}}$ is the Boltzmann constant and $\mathrm{E}_{f}$ is the activation energy representing the energy barrier connected with rotations of the long molecular axes.

Extrapolation of the given straight line on the inverse temperature axis and linear fit field the magnitude of activation energy $E_{f}=0.29 \mathrm{eV}$.


Fig. 5. Crossover frequency $f_{\mathrm{c}}$ versus the inverse temperature $1 / \mathrm{T}$.

## CONCLUSION

The interval of LC phase of the developed novel dualfrequency LC, consisting of LC 5CB with positive dielectric anisotropy and two LCs with negative dielectric anisotropies C 2 and H 22 , has been extended within $11-65^{\circ} \mathrm{C}$. Increasing temperature of the sample results in reduction of perpendicular component of dielectric permeability and an increase of crossover frequency. The last is characterized by the activation energy connected with rotations of the long molecular axes.

## ACKNOWLEDGMENT

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# $\Delta^{0}$ - RESONANCE PRODUCTION IN MULTI-NUCLEON $\boldsymbol{\pi}^{-12} \mathbf{C}$ - INTERACTIONS AT THE MOMENTUM OF 40GeV/c 

Y. H. HUSEYNALIYEV<br>Azerbaijan State Pedagogical University, Bakr/Azerbaijan<br>E-mail: yashartur@yahoo.com

The experimental results on properties of multi-nucleon $\pi^{-12} \mathrm{C}$ - interactions at the momentum of $p_{\pi}-=40 \mathrm{GeV} / \mathrm{c}$ obtained from the 2 m propane bubble chamber of the laboratory of High Energies of Joint Institute for Nuclear Research (Dubna, Russia) are discussed. To select the multi-nucleon $\pi^{-12} C$ - interactions the criterion is used that the number of identified protons with momentum $p_{p}<1 G e V / c$ is great or equal two in each event ( $n_{p} \geq 2$ ). To analyze the properties of multi-nucleon $\pi^{-12} C-$ interactions the variable $R$ is used. The values of the $R$ as a ratio of the inclusive spectra of charged $\pi$-mesons and protons emitted in multi-nucleon events and in all ones are determined, i.e.

$$
R=\frac{\left[1 / N_{e v}(d N / d y)\right]_{n_{p} \geq 2}}{\left[1 / N_{e v}(d N / d y)\right]_{\pi^{-12} C}}
$$

As the characteristics of secondary particles the transverse momentum $\left(p_{t}\right)$, cumulative number ( $\beta^{0}$, the values of which are determined as $\beta^{0}=\left(E-p_{l}\right) / M_{N}$, where $E$ is a total energy, $p_{l}$ is a longitudinal momentum and $M_{N}$ is a nucleon mass), kinetic energy $(T)$ and emission angle $(\theta)$ dependences (in laboratory frame) of the $R$ are studied. The indications on occurrence of a $\Delta^{0}-$ baryon resonance and relatively high contribution of deep-inelastic processes in multi-nucleon events are received.

Keywords: $\pi^{-12} C, \Delta^{0}$-baryon resonance, $\pi$-meson, proton, transverse momentum, cumulative number, kinetic energy, emission angle, effective mass distribution
PACS: $25.75 . \mathrm{Gz}, 25.75$. q, 11.25.Hf, 123.1K, 13.85. $-\mathrm{t}, 25.80$. e, 14.20. Gk

## INTRODUCTION

Study of behavior of the characteristics in hadronnucleus and nucleus-nucleus interactions as a function of collision centrality, Q , is an important experimental method for obtaining information on the phases of nuclear matter, because the increase in Q could lead to an increase in baryon density of nuclear matter. In other words, changes in the behavior of some centrality in dependence of characteristics of events will be a signal on the phase transition. This is considered the best method to achieve a phase of quark-gluon plasma of strongly-interacting nuclear matter. Some experimental results have demonstrated the existence of changes in behavioral characteristics of events as a function of the collision centrality [1-8].

The easiest option to set centrality is the use the number of protons emitted in the reactions to consider multi-nucleon processes. By studying the multi-nucleon events in hadron-nucleus and nucleus-nucleus interactions one can get useful information about collective phenomena, for example formation of bound states of the resonances in the nucleus. It should be noted that production of some baryon resonances has been studied in [9] in detail. Physics of these processes serves as a bridge that joins the study of mechanisms for the production of high-energy particles, and new phases of strongly interacting nuclear matter. But there is one very important question: what are the criteria to separate the multinucleon processes in experiment? There another question is arising: can we extract resonance in an event using only
particle characteristics and without using any method, which was done in [9]?

## 1. THE EXPERIMENTAL METHOD ON $\Pi^{12} \mathrm{C}$ INTERACTION

The experimental data were obtained using the 2 m propane bubble chamber of the Laboratory of High Energies of Joint Institute for Nuclear Research (JINR) (Dubna, Russia) exposed to a beam of relativistic $\pi^{-}$mesons at $40 \mathrm{GeV} / \mathrm{c}$ at Serpukhov Accelerator. The number of $\pi^{-12} C$-interactions equals to 8791 , where the corresponding inelastic cross section is $\sigma_{\text {in }}=(87.5 \pm 1.0) m b \quad$ [10]. The methodological issues connected with the processing of the stereo photos, selection and identification of types of interactions in propane $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$, reconstruction of the kinematical characteristics of the secondary particles, their identification, and inclusion of corrections due to the loss of particles emitted under large angle to the object plane of a camera are described in details in [11-13]. Practically all secondaries, emitted at a $4 \pi$ total solid angle, were detected in the chamber. A minimum momentum for pion registration was about $70 \mathrm{MeV} / \mathrm{c}$. Separation of protons and $\pi^{+}$-mesons was done visually based on their ionization in region $p<700 \mathrm{MeV} / c$ and protons were identified, since a momentum $140 \mathrm{MeV} / \mathrm{c}$ at which the track starts to be precisely visible (length $>3 \mathrm{~cm}$ ). The analysis on $\delta$-electrons showed that the admixture of protons among the fast positive singly charged particles identified as $\pi^{+}$-mesons was $12 \pm 5 \%$ of the measured mean multiplicity of protons. It should be mentioned that $\pi^{-}$-
mesons make up the main fraction ( $>95 \%$ ) among the negatively charged particles [14].

## 2. PROPERTY OF MULTI-NUCLEON $\Pi^{12} \mathrm{C}$ INTERACTIONS AT $\quad P_{\pi^{-}}=40 \mathrm{GEV} / \mathrm{C}$

In this paper the inclusive properties of $\pi^{ \pm}$-mesons and protons production (with momentum $\mathrm{P}_{\mathrm{p}}<1 \mathrm{GeV} / \mathrm{c}$ ) are studied by comparing data, when the number of protons is great or equal two (multi-nucleon event) with inclusive properties of all $\pi^{-12} \mathrm{C}$ events, i.e. from process

$$
\begin{equation*}
\pi^{-}+{ }^{12} C \rightarrow n p+n_{1} \pi^{ \pm}+X \tag{1}
\end{equation*}
$$

( $n$ is a number of protons with $\mathrm{P}_{\mathrm{p}}<1 \mathrm{GeV} / \mathrm{c}, n_{1}$ is number $\pi^{ \pm}$-mesons, and $X$ is all rest) is allocated process

$$
\begin{equation*}
\pi^{-}+{ }^{12} C \rightarrow n^{\prime} p+n_{1}^{\prime} \pi^{ \pm}+X^{\prime} \tag{2}
\end{equation*}
$$

( $n^{\prime} \geq 2$ is a number of protons with $\mathrm{P}_{\mathrm{p}}<1 \mathrm{GeV} / \mathrm{c}, n_{1}^{\prime}$ is a number of $\pi^{ \pm}$-mesons and $X^{\prime}$ is all rest in event) and inclusive properties of process (2) by means of variable $R^{k}(y)$ are compared with inclusive properties of process (1).

The variable $R^{k}(y)$ is defined as a ratio of inclusive spectra of particles of type $k$ ( $k$ denotes $\pi^{ \pm}$-meson or proton) depending on a variable $y$ received in process (2) to similar spectra, received in (1), i.e.

$$
R^{k}(y)=\frac{(d N / d y)_{2}}{(d N / d y)_{1}}
$$

As the characteristics of secondary particles $(y)$ the transverse momentum $\left(p_{t}\right)$, cumulative number ( $\beta^{0}$, the values of which is determined as $\beta^{0}=\left(E-p_{l}\right) / M_{N}$ , where $E$ is a total energy, $p_{l}$ is a longitudinal momentum and $M_{N}$ is the nucleon mass), kinetic energy ( $T$ ) and emission angle ( $\theta$ ) dependences (in laboratory frame) of the $R$ are studied. The number of multi-nucleon $\pi^{-12} C$ - interactions equals to 3571 . The interactions of the projectiles with "quasi-free" nucleons of the target were not taken into account.

The characteristics $p_{t}, \beta^{0}$ and $T$ allow describing such parameters of nuclear substance, as the geometrical sizes of area of radiation, a mass and "temperature" of nuclear matter, accordingly. In addition, $\beta^{0}$ describes minimum target mass, by which an interaction takes place. Therefore, the values of $R^{k}(y)$, distinct from $\overline{n_{1}^{\prime}} / \overline{n_{1}}$ in case of $\pi^{ \pm}$- mesons and from $\overline{n^{\prime}} / \bar{n}$ in case of protons $\left(\overline{n_{1}}, \overline{n_{1}^{\prime}}, \bar{n}\right.$ and $\overline{n^{\prime}}$ are the average values of $n_{1}, n_{1}, n$ and $n$, accordingly), will be interpreted as manifestation of dynamic effects, related with multinucleon processes.

## 3. EXPERIMENTAL RESULTS

In fig. 1a, b values of $R^{k}\left(p_{t}\right)\left(\bullet-\pi^{+}\right.$-meson, $\circ-\pi^{-}-$ meson and $\square \underline{-p r o t o n)}$ are presented. For the ratios $\overline{n_{1}^{\prime}} / \overline{n_{1}}$ and $\overline{n^{\prime}} / \bar{n}$ following values are found accordingly: $0.96 \pm 0.01$ (for $\pi^{+}$-meson, in figures it is shown by dashed lines); $1.05 \pm 0.01$ (for $\pi^{-}$-meson, in figures it is shown by dot lines); $1.81 \pm 0.02$ (for proton, in figures it is shown by dashed-dot lines).


Fig. 1.The $R\left(p_{t}\right)$ dependence for $\pi^{ \pm}$- mesons (a) and protons (b), emitted in $\pi^{-12} C$ - interactions at $p_{\pi^{-}}=40 \mathrm{GeV} / \mathrm{c}$.

Errors of ratios for different type of particles are shown by the empty or filled boxes near to lines whose values are given in the text at appropriate places. From fig. $1 \mathrm{a}, \mathrm{b}$ it is seen, that:
1.1) for $\pi^{ \pm}$-mesons, the values of $R\left(p_{t}\right)$ does not differ from $\overline{n_{1}^{\prime} /} \overline{n_{1}}$ at all values of $p_{t}$;
1.2) for protons, $R\left(p_{t}\right) \approx \bar{n}^{\prime} / \bar{n}$ at all $p_{t}$.
1.3) in $p_{t}>0.75 \mathrm{GeV} / \mathrm{c}$, the $R\left(p_{t}\right)$ for $\pi^{+}$- and $\pi^{-}$mesons coincide (fig.la).

It means that emission of $\pi$-mesons practically independent of their sign of charge. The distribution of protons is also the same, but with different numerical
factor, 1.81 (fig. 1 b ). The latter is due to the fact that, in the number of protons in multi-nucleon events selection is made ( $n^{\prime} \geq 2$ ).

According to data presented in fig. 2 a , b one can conclude, that


Fig.2a.The $R\left(\beta^{0}\right)$ dependence on $\beta^{0}$ for $\pi^{ \pm}$- mesons, emitted in $\pi^{-12} C$-interactions at $\mathrm{p}_{\pi}=40 \mathrm{GeV} / \mathrm{c}$.


Fig.2b.The $R\left(\beta^{0}\right)$ dependence on $\beta^{0}$ for protons, emitted in $\pi^{-12} C$ - interactions at $\mathrm{p}_{\pi}=40 \mathrm{GeV} / \mathrm{c}$.
2.1) for $\pi^{+}$-mesons, $R\left(\beta^{0}\right) \approx \overline{n_{1}^{\prime}} / \overline{n_{1}}$ at $\beta^{0}<1$ and $R\left(\beta^{0}\right) \geq \overline{n_{1}^{\prime}} / \overline{n_{1}}$ at $\beta^{0}>1 ;$
2.2) for $\pi^{-}$-mesons, $R\left(\beta^{0}\right)<\overline{n_{1}^{\prime}} / \overline{n_{1}}$ at $\beta^{0}<0.1$ and $R\left(\beta^{0}\right) \geq \overline{n_{1}^{\prime}} / \overline{n_{1}}$ at $\beta^{0}>0.1 ;$
2.3) for protons, $\quad R\left(\beta^{0}\right) \geq \bar{n}^{\top} / \bar{n} \quad$ at $\beta^{0}<1$ and

$$
R\left(\beta^{0}\right) \leq \overline{n^{\prime}} / \bar{n} \text { at } \beta^{0}>1
$$

The values of $R(T)$ are presented in fig.3, and it is seen that:
3.1) for $\pi^{+}$-mesons, $R(T) \approx \overline{n_{1}^{\prime}} / \overline{n_{1}}$;
3.2) for $\pi^{-}$-mesons, $R(T)>n_{1}^{\prime} / \overline{n_{1}}$ at $T<1 \mathrm{GeV}$ and

$$
R(T) \leq \overline{n_{1}^{\prime}} / \overline{n_{1}} \text { at } T>1 \mathrm{GeV}
$$

3.3) for protons, $R(T) \approx \overline{n^{\prime} /} / \bar{n}$.

## 4. DISCUSSION OF EXPERIMENTAL RESULTS

According to data given in the previous section, one can see that, the increase in the number of the nucleons participating in interaction, does not lead to any noticeable change in the distributions of secondary $\pi^{ \pm}$mesons and protons on the $p_{t}$ (results 1).


Fig. 3a.The $R(T)$ dependence for $\pi^{ \pm}$- mesons (a), emitted in $\pi^{-12} \mathrm{C}$-interactions at $p_{\pi}=40 \mathrm{GeV} / \mathrm{c}$.

This result may indicate that:

- the role of multiple collisions in multi-nucleon processes is negligible;
- in multi-nucleon processes in a significant part of cases nucleons inside the nucleus occupy less volume than the volume occupied by them in case of all processes.

In this case it is necessary to assume, that the interaction of the primary hadron occurs to a group of rigidly-correlated nucleons. This assumption in due time has been used by academician Baldin to explain the basic properties of a cumulative effect [15] and in searching the effect of nuclear shock waves in [16]. The author has also used assumption. However, the results 3.1 and 3.2 of the independence $R^{\pi^{+}, p}\left(p_{t}\right)$ from $p_{t}$ are somewhat puzzled by the fact that in an area of radiation in case of rigid correlations of nucleons the "temperature" of the system should increase. First of all it should be reflected in a spectrum of protons by occurrence of hightemperature components. For elimination of the arising contradiction it is necessary to introduce a mechanism by which the system of rigidly-correlated nucleons "cools". For this purpose we turn the result 3.2, which indicates that in processes (2) the yield of $\pi^{-}$-mesons with momentum close to momentum of protons, more than in the processes (1).


Fig. 3b.The $R(T)$ dependence for protons (b), emitted in

$$
\pi^{-12} \mathrm{C} \text { - interactions at } p_{\pi^{-}}=40 \mathrm{GeV} / \mathrm{c}
$$

Probably, this result is the reason of "cooling" of rigidlycorrelated nucleons system through the mechanism of formation and decay of baryon resonances into proton and $\pi^{-}$-mesons. Confirming to this statement we should note that in paper [17] an attempt was made to determine the inclusive cross sections of a $\Delta$ baryon and $\mathrm{N}^{*}$ nucleon resonances production in process (1) with allocation of process (2). Invariant mass spectra of pairs proton- $\pi^{-}$ meson were analyzed. The author of that paper managed to obtain a relatively high yield of $\Delta$ in process (2). These data do not exclude an opportunity of occurrence in processes (2) in some cases a phase of resonances.

In multi-nucleon processes in the cumulative area $\left(\beta^{0}>1\right)$ the yield of protons with momentum, greater than $1 \mathrm{GeV} / \mathrm{c}$ (relativistic protons) is more, than in all events. Anoshin, etc. [18] has found, that the probability of a pion production with values $\beta^{0}>0.6$ is $(2.0 \pm 0.2) \%$ and of course the probability of proton emission with values $\beta^{0}>0.6$ in interactions in $\mathrm{P}_{\pi}=40 \mathrm{GeV} / \mathrm{c}$ is more, than this value, i.e. $(37 \pm 1) \%$ [19]. It explains why a point of regime change could not be observed on the behavior of R as function $\beta^{0}$ for pions. The results obtained in [10, 20] confirm the assumption which found that multi-nucleon events can be correctly identified using the following criterion: the number of protons greater than $3 \div 4$ and the values $\beta^{0}>0,6$ for the pions produced in $\pi^{-12} C-$ interactions at $P_{\pi}^{-}=40 \mathrm{GeV} / \mathrm{c}$. It means that the area of new physics - multi-nucleon physics begins after values $\beta^{0}>0.6$.

$$
\text { For } \pi^{+} \text {-mesons } R^{\pi^{+}}\left(\beta^{0}\right)>\overline{n_{1}^{\prime} / n_{1}} \text { at } \beta^{0}>1 \text { and }
$$ that $R^{\pi^{+}}\left(\beta^{0}\right)<\overline{n_{1}^{\prime}} / \overline{n_{1}}$ at $\beta^{0}<1$, i.e. excess $\pi^{+}$- mesons in $\beta^{0}>1$ is related to the admixture of unidentified protons among $\pi^{+}$-mesons. This fact, together with result 2.2 (at $\left.\beta^{0}<0,1\right)$ which indicates a weakening leading effect in multi-nucleon processes can be seen as an indication of the large contribution of inelastic processes in multinucleon events, i.e. manifestation of quark freedom degrees in nuclei in multi-nucleon processes. These results can have a great value for understanding of internuclei processes at small distances when separate nucleons lose the individuality and the processes connected with quark degrees of nuclei are dominating,

i.e. we can consider, that in some cases the group of rigidly - correlated nucleons with the big internal energy as a result of the further increase in temperature turns to a quark-gluon plasma which is cooled by emission of particles of greater spins, than at nucleons, including $\Delta$ and $\mathrm{N}^{*}$. Therefore, the properties of $\pi^{ \pm}$-mesons with $T$ $<1 \mathrm{GeV}$ should be investigated more carefully.

According to data, resulted on fig. 4 it is seen, that in all range of definition of $T, R^{\pi^{+}}(T) \approx 1$ and $R^{\pi^{-}}(T)>1$ at $T<0,25 \mathrm{GeV}$ and $R^{\pi^{-}}(T) \approx 1$ at $T$ $\geq 0,25 \mathrm{GeV}$. Thus, we see, that the yield of $\pi^{-}$-mesons with $T<0,25 \mathrm{GeV}$ in multi-nucleon processes is more, than in all $\pi^{-12} \mathrm{C}$-interactions at $p_{\pi^{-}}=40 \mathrm{GeV} / \mathrm{c}$. This result probably serves as one more fact in favor of existence of a phase of baryon resonances in multi-nucleon systems. Let's explain told. It is known, that the probability of absorption of $\pi^{-}$- mesons with $\mathrm{T}<0,25 \mathrm{GeV}$ by group rigidly-correlated nucleons is greater and consequently, to explain the received result, it is necessary to assume, that these $\pi^{-}$- mesons emit out of area of absorption. One possible way of such emission could be the disintegration of slow baryon resonances.


Fig.4. The $R(T)$ dependence for $\pi^{ \pm}$-mesons with kinetic energy $T<1 \mathrm{GeV}$ (• $-\pi^{+}$-meson, $\circ-\pi^{-}-$meson $)$emitted in $\pi^{-12} C$ - interactions at $p_{\pi}=40 \mathrm{GeV} / \mathrm{c}$.

## 5. ANALYSIS OF ANGULAR DISTRIBUTIONS OF $\Pi^{ \pm}$-MESONS AND PROTONS

The results obtained in the previous sections show that multi-nucleon processes differ from all events in $\pi^{-}$mesons with kinetic energies $T<0.25 \mathrm{GeV}$. Large yield of soft $\pi^{-}$- mesons was explained due to the mechanism of neutral baryon resonances production with their subsequent decay into protons and $\pi^{-}$-mesons. Therefore, the angular distributions of $\pi^{ \pm}$- mesons and protons with $T<0.25 \mathrm{GeV}$ in lab frame were analyzed in order to verify this assumption. For comparison, similar data for $\pi^{ \pm}$mesons and protons with $T>0.25 \mathrm{GeV}$ were obtained.

Fig. 5 presents experimental data for $\pi^{ \pm}$-mesons and protons with $T<0.25 \mathrm{GeV}$.


Fig.5a. $R(\cos \theta)$ dependence for $\pi^{ \pm}$-mesons
$\left(\bullet-\pi^{+}, \circ-\pi^{-}\right)$with $T<0.25 \mathrm{GeV}$, emitted in the $\pi^{-12} C$ - interactions at $40 \mathrm{GeV} / \mathrm{c}$.


Fig.5b. $R(\cos \theta)$ dependence for protons( $\square)$ with
$\mathrm{T}<0.25 \mathrm{GeV}$, emitted in the $\pi^{-12} C-$ interactions at $40 \mathrm{GeV} / \mathrm{c}$.

One can see that:

1) for $\pi^{+}$-mesons, within the error bars $R^{\pi^{+}}(\cos \theta) \approx \overline{n_{1}^{\prime}} / \overline{n_{1}}(0.99 \pm 0.02)$ in the whole studied range of $\theta$, here $\theta$, is the emission angle of $\pi^{+}$mesons $\overline{n_{1}^{\prime}}$ and $\overline{n_{1}}$ are the average multiplicities of secondary $\pi^{+}$-mesons with kinetic energies $T$ $<0.25 \mathrm{GeV}$ in multi-nucleon and in all events, respectively),
2) for $\pi^{-}$-mesons, $R^{\pi^{-}}(\cos \theta)=1.4 \pm 0.1$ in $\cos \theta<-0.6$ ( $\theta$ is an emission angle of $\pi^{-}$-meson), i.e. more than $\overline{n_{2}^{\prime}} / \overline{n_{2}}=1.18 \pm 0.03$;
3) for protons, within the error bars, $R(\cos \theta)$ coincides with the value $\overline{n^{\prime}} / \bar{n}(1.81 \pm 0.03)$ in the whole studied range $\theta$.


Fig.6a. $R(\cos \theta)$ dependence for mesons $\left(\bullet-\pi^{+}-, \circ-\pi^{-}-\right)$with kinetic energies $0,25<\mathrm{T}<1 \mathrm{GeV}$, emitted in $\pi^{-12} C$ interactions at $40 \mathrm{GeV} / \mathrm{c}$.


Fig.6b. $R(\cos \theta)$ dependence for protons ( $\square$ ) with kinetic energies $0,25<\mathrm{T}<1 \mathrm{GeV}$, emitted in the $\pi^{-12} C$-interactions at $\mathrm{P}_{\pi^{-}}=40 \mathrm{GeV} / \mathrm{c}$.

The data, presented in fig. 6 and fig.7, shows that for charged pions and protons with $0.25<T<1 \mathrm{GeV}$ and for $\pi^{ \pm}$-mesons with $T>1 \mathrm{GeV}$ in the whole domain of definition of $\theta$.

## 6. EFFECTIVE MASS DISTRIBUTION OF $\Pi^{-} P$ PAIRS

Effective mass distribution of $\pi$ p pairs emitted in multi-nucleon $\pi^{-12} C$-interactions at the momentum of incident negative pions, which equal to $40 \mathrm{GeV} / \mathrm{c}$, is shown in Fig.8. Here, the restrictions mentioned above $\left(\mathrm{T}_{\pi^{-}}<0,25 \mathrm{GeV}, \beta^{0}\left(\pi^{-}\right)>0.6, \cos \theta\left(\pi^{-}\right)<-0.6\right)$ are taken into account. The experimental data was fitted by relativistic Breit-Wigner function type $y=A^{*} w^{*} x^{*} M /\left(\left(x^{\wedge} 2-M^{\wedge} 2\right)^{\wedge} 2+\right.$ $\mathrm{w}^{\wedge} 2{ }^{*} \mathrm{M}^{\wedge} 2$ ). The fitted parameters are the following: Reduced Chi-Sqr=0.13877; Adj. R-Square=0.97423; width of the neutral baryon resonance with error, $\mathrm{w}=161.4818 \pm 9.71773$; the mass of the neutral baryon resonance with error, $\mathrm{M}=1234.70704 \pm 2.53113$ and
amplitude of the distribution with error, $\mathrm{A}=13050.58843 \pm 563.82774$. The fitted parameters are in good consistence with other paper [9].

Thus, one could argue that the main difference between the selected multi-nucleon and all processes is the behavior of $\pi^{-}$-mesons with $T<0.25 \mathrm{GeV}$ and $\cos \theta<-$. 6 .

## CONCLUSION

It is found that, multi-nucleon events can be correctly identified using the following criteria: the number of protons greater than $3 \div 4$ and the values $\beta^{0}>0,6$ for pions produced in $\pi^{-12} C$-interactions with the $\mathrm{P}_{\pi^{-}}$ $=40 \mathrm{GeV} / \mathrm{c}$.


Fig.7. $R(\cos \theta)$ dependence for $\pi^{ \pm}-$mesons $\left(\bullet-\pi^{+}-\right.$ meson, $\circ-\pi^{-}$-meson) with kinetic energies $T>0.25 \mathrm{GeV}$, emitted in the $\pi^{-12} C$ - interactions at $\mathrm{P}_{\pi}=40 \mathrm{GeV} / \mathrm{c}$.

It turned out that multi-nucleon $\pi^{-12} C$ - interaction (with the number of identified protons is greater or equal two),
basically differ from all $\pi^{-12} C$-events by large yield of "soft" $\pi^{-}$-mesons with kinetic energies $\mathrm{T}<0.25 \mathrm{GeV}$ and emission angle $\cos \theta<-0.6$ in the laboratory frame. This fact can be explained by the dominant role of the mechanism of neutral baryon resonance production in multi-nucleon processes with a relatively large cumulative number. It is found that the neutral $\Delta$-baryon resonance can be extracted by using the particle characteristics, such as transverse momentum, cumulative number, kinetic energy and emission angle.


Fig.8. Effective mass distribution of $\pi$ p pairs emitted in multi-nucleon $\quad \pi^{-12} C$-interactions at $\mathrm{P}_{\pi^{-}}$ $=40 \mathrm{GeV} / \mathrm{c}$
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# ANOMALIES OF THE INDUCED IMPURITY PHOTOCONDUCTIVITY IN GALLIUM MONOSELENIDE CRYSTALS 

A.SH. ABDINOV, R.F. BABAYEVA*, YA.G. GASANOV **, S.I. AMIROVA, N.A. RAGIMOVA, R.M. RZAYEV<br>Baku State University, Az 1145, Baku, Z.Khalilov str., 23<br>*Azerbaijan State Economic University, ** Azerbaijan Medical University


#### Abstract

Under various external conditions the basic characteristics and parameters of induced impurity photoconductivity (IIPC) in $p-G a S e$ crystals with various initial specific dark resistances have been investigated experimentally. It has appeared that in high-resistance crystals this photo-electric phenomenon is accompanied by a number of anomalies. It is ascertained that IIPC found out in high-resistance $p-G a S e$ crystals are caused with partial disorder of these crystals.


Keywords: impurity photoconductivity, trapping level, specific resistance, background illumination, drift barriers, recombination barriers, probing light.
PACS: 61.46

## 1. INTRODUCTION

Among $\mathrm{A}^{\mathrm{III}} \mathrm{B}^{\mathrm{VI}}$ semiconductor compounds with layered structure gallium monoselenide (GaSe) crystals gain special attention as a perspective material for optoelectronics, having high enough photosensitivity (at temperatures up to $\sim 350 \mathrm{~K}$ ) and an optical transparency in $0.30 \div 0.63 \mu m$ region and $0.65 \div 18 \mu m$, accordingly. Strong ionic-covalent binding in layers and considerably weak (Van-der-Vaals binding with the small ioniccovalent contribution) binding between layers (along the "C" axis of the crystal) besides strong anisotropy of electric, optical, thermal, mechanical properties of these crystals, causes also various anomalies of the non-equilibrium electronic phenomena in them. The layered structure does GaSe single crystals perspective also for creation various contact structures, photodetectors and light sources, as well as for bistable and threshold switches. The combination of switching property with high photosensitivity and highly effective injection electroluminescence in a visible region allows to create on the basis of these crystals various generators and relaxation oscillators for optoelectronics, including devices which are called vitrids and are competitors for multilayered (with one or several $p-n$ junctions) semiconductor devices, such as dinistors, thyristors, phototriggers, light sources with " S "-shaped currentvoltage characteristic. Advantage of the last (vitrids) as compared to devices with $p-n$ junctions consist in possibilities to operate at any polarity of controlling external electric voltage and independence of switching voltage value on the steepness of operating impulse front .

In the scientific literature appeared information also about possibilities of creation on the basis of gallium monoselenide crystals sources of terahertz laser radiation applied in manufacture of photodetectors and photoconverters for infra-red (IR) radiation, control of photosensitivity range under the effect of various external influences and by means of change of intra-crystal conditions.

In our opinion, it is interesting also the fact that though in this material usual positive impurity photoconductivity is not observed almost, however take place other impurity photoeffects - negative photoconductivity, IR-quenching of intrinsic photoconductivity, induced impurity photoconductivity, induced by electric field negative photoconductivity [1, 2]. The specified properties, firstly considerably expand photosensitivity spectrum gallium monoselenide crystals towards near IR spectrum region (up to $\sim 2.60 \mu m$ ); secondly allow to control their photoelectric properties purposefully; thirdly make these semiconductors a suitable material also for creation of various photodetectors and the converters representing a great interest for optoelectronics.

Though in some early works [3, 4] it was reported about detection in $p-G a S e$ crystals induced impurity photoconductivity (IIPC) of various type (IBIPC induced by background illumination and IIIPC - induced by injection impurity photoconductivity), however herein the reasons of their anomalies remained not found out.

In particular it is established that unlike experimentally established in the majority of other semiconductor materials, as well as the contradiction of existing scientific notations on this phenomenon [5] in semiconductors, in general in $p-G a S e$ crystals experimentally measured value of IIPC itself ( $\Delta i_{i p c}$ ) and the value of duration of the relaxation time ( $\tau_{i p c}$ ) after switching off the effect of probing light appear considerably high. In so doing specific dependences $\Delta i_{i p c}$ values, as well their shapes, key parameters of its spectral distribution, light (lux-current) and current-voltage characteristics, kinetics on the value of exciting factors, injecting ability of current-carrying contacts, initial dark specific resistance (value of $\rho_{d o}$ at 77), alloying level for studied sample and temperature.

All above mentioned problems possess certain scientific-practical value and will demand detailed
experimental research of IIPC in $p-G a S e$ single crystals.

Naturally these researches besides enrichment of knowledge of electronic properties of gallium monoselenide crystals can be useful also for development of physics of the induced impurity photoconductivity in semiconductors in general.

In the given work set a goal on the basis of detailed experimental research of IIPC in $p-G a S e$ single crystals to find out the reasons of its anomalies in the specified material.

## 2. RESEARCH TECHNIQUE AND SAMPLES

Studied samples were cut off from various sections of the same pure (specially not alloyed) and alloyed by gadolinium atoms with various percentage $\left(N_{G d} \approx 10^{-5}\right.$; $10^{-4} ; 10^{-3} ; 10^{-2}$ and $10^{-1} \mathrm{at} . \%$ ) of the single crystalline ingot ( $p-G a S e$ and $p-G a S e<G d>)$ on cleavage planes. Both types' ingots were grown up by a method of slow cooling at a constant temperature gradient [6] and alloying with $G d$ of various composition was carried out by technology similar to applied elsewhere [7] for reception alloyed with rare-earth elements (REE) $n$-InSe crystals.

Samples represented plane-parallel plates of $d \approx 0.20 \div 0.50 \mathrm{~mm}$ thickness (along the " C " axis of the crystal) and $3 \div 4.3 \div 5 \mathrm{~mm}^{2}$ area (on "C" plane of the crystal). Their specific dark resistance $\left(\rho_{d}\right)$ was defined by standard two-probe method at 300 K for various samples along and across the layers. At $300 K \rho_{d}$ value were $\sim 10^{1} \div 10^{6} \Omega \cdot \mathrm{~cm}$ and $10^{2} \div 10^{8} \Omega \cdot \mathrm{~cm}$ for various samples, along and across the layers accordingly. With decreasing of temperature to 77 K it sharply increased (almost by 3-4 order of magnitude) and for various samples were $\rho_{d} \approx 10^{2} \div 10^{8} \Omega \cdot \mathrm{~cm}$ and $\approx 10^{3} \div 10^{10} \Omega \cdot \mathrm{~cm}$ along and across the layers accordingly. As a material for current carrying contacts $I n, S n$, as well as silver paste or aquadag were used. Contacts were created by soldering In (or $S n$ ) without a flux and application silver paste (or aquadag) in open air.

Depending on alloying level ( $\mathrm{N}_{\mathrm{Gd}}$ value) a value of $\rho_{d o}$ of $p-G a S e<G d>$ crystals at $77 K$ varied within $10^{2} \div 10^{11} \Omega \mathrm{~cm}$.

Measurements were carried out on the experimental installation assembled on the basis of two monochromators (MDR-12 and MDR-12U type) with quartz lenses. As illumination sources incandescent lamps were applied intended specially for used monochromators.

Under all conditions considered by us illumination of investigated samples (both background illumination and a probing light beam) was carried out on "C" plane of the crystal. Measurements at research IBIPC were carried out both along and in perpendicular direction to layers, and at research IIIPC - in a direction parallel to "C" axis of the crystal.

At BCGA measurements the method of two light sources were used, in which one high-intensity beam of light with the fixed wavelength (with fixed energy of
radiation quantum $h v_{c}$ as a rule corresponding to a maximum of a spectrum of intrinsic photoconductivity of the studied sample) and second - probing one with a wide radiation spectrum. Both radiation beams are received (selected) by means of used by us in experiment monochromators from incandescent lamps. From a probing radiation beam by means of MDR-12 narrow monochromatic beam with variable energy ( $h v_{V}$ ) was selected.

Measurements were carried out in $77 \leq T \leq 300 K$

$$
U \leq 3 \cdot 10^{3} \mathrm{~V} / \mathrm{cm}, \quad \Phi \leq 5 \cdot 10^{2} L u x \quad \text { and }
$$

$\mathbf{0 . 3 0} \leq \lambda \leq \mathbf{3 . 0 0} \mu \mathrm{m}$ intervals of temperature ( T ), external electric voltage applied to the sample ( $U$ ), intensity ( $\Phi$ ) and light wavelength $(\lambda)$ accordingly.

At IIIPC measurements the first beam of light (the light beam with the fixed wavelength or quantum energy) was not used and unlike IBIPC case, instead of weak voltage, on the sample higher external voltage (corresponding to area of full filling of traps [8]) was applied. By change of value of this voltage injection level (level of IIIPC excitation in the studied sample) varied.

## 3. EXPERIMENTAL RESULTS

All basic IIPC characteristics (spectral distribution, light characteristics, kinetics, temperature dependence and dependence on the external electric voltage applied to the sample) were measured in studied samples (fig. 1-6).

Comparison of the received experimental results on spectral distribution, kinetics, light characteristics of IBIPC and IIIPC, as well as on influence $\rho_{d o}$ and T on these phenomena has shown that thereby qualitative differences are not observed. Only some quantitative differences take place. At that at IBIPC observable features under other identical conditions are shown more brightly. Therefore in given article we give only experimentally measured graphs on IBIPC, with the exception of the graph in which dependence of $\Delta i_{i p c}$ on the value of the inducing external electric voltage $\left(U_{i}\right)$ is represented.

As a result of the carried out measurements it is established that gallium monoselenide single crystals in IIPC properties at low temperatures $(T<300 K)$ also are divided on two groups: low-resistance and highresistance ones.

In both groups of crystals at $T \leq 170 \div 190 K$ (for various samples depending on value $\rho_{d o}$ ) is observed pronounced IIPC which value and basic characteristics considerably depend also on $\rho_{d o}$. Under other identical conditions influence of specific dark resistance ( $\rho_{d o}$ ) on the above mentioned parameters and characteristics of IIPC with growth of $\rho_{d O}$ manifests itself more strongly, and with rise in temperature is strongly weakened. With rise in temperature value of IIPC ( $\Delta i_{i p c}$ value) also decreases.

In low-resistance crystals parameters of IIPC spectrum (fig. 1, curve 1) appear independent of excitation level (intensity of background illumination and
voltage of injecting electric field at IBIPC and IIIPC accordingly).


Fig. 1.IIPC spectrum in $p-G a S e$ crystals under various excitation levels. $\mathrm{T}=77 \mathrm{~K} ; \lambda_{c}=0.58 \mu m ; \lambda_{I}$ $=1.60 \mu \mathrm{~m} ; U=5 \mathrm{~V} ; \rho_{d o}, \Omega \cdot \mathrm{~cm}: 1-10^{3} ; 2-6-10^{8}$; $\Phi_{\text {int, }}$ rel. units: 1, 2-0.1; 3-0.15; 4-0.25; 5-0.5; 6-0.8.

Thus both IBIPC and IIIPC spectrum covers $0.80 \leq \lambda \leq 2.80 \mu \mathrm{~m}$ wavelength range and has a maximum at $\lambda_{\text {in }}=1.60 \mu \mathrm{~m}$. Besides in these (low-resistance) crystals IIPC has fast character. In particular, at switching on probing light stationary value $\Delta i_{i p c}$ is established quickly and without inertia (almost instantly) falls down to zero after switching-off effect of probing light (fig. 2, curve 1).

Unlike low-resistance crystals, in high-resistance ones (fig. 1, curves 2-6) position of maximum ( $\lambda_{i m}$ ) and long-wavelength cut-off ( $\lambda_{i c}$ ) on the spectral distribution of IIPC appear dependent on $\rho_{d o}$ and with growth of the last at weak $\Phi_{l}$ (as well as also at not so high $U_{i}$ ) are slightly displaced to longer waves (fig. 1, curves 2-4). With growth of excitation level ( $\Phi$ or $U_{i}$ values) and with rise of the temperature (at $T \leq 100 \div 120 K$ for various samples depending on $\rho_{d o}$ value) dependences $\lambda_{i m}$ and $\lambda_{i c}$ on $\rho_{d o}$ are gradually weakened and at last absolutely disappear.

In high-resistance crystals, unlike low-resistance ones, decay of IIPC after switching off effect of probing light has long-term relaxing character (fig. 2, curves 2-4) residual IIPC is observed. Thus value of the residual IIPC $\left(\Delta i_{r c}=\Delta i_{i p c}-\Delta i_{i p c}{ }^{\prime}\right.$, where $\Delta i_{i c}{ }^{\prime}-$ IIPC value through 30 sec after switching-off probing light) besides $\Phi_{i m p}$ (fig. 2, curves 2-4) $\Phi_{\text {int }}$ (or $U_{i}$ ) appears dependent also on temperature and $\rho_{d o}$. At low temperatures (fig. 3, curve 1) $\Delta i_{r c}$ value decreases with increase of T (fig. 3, curve 1 ), and increases with growth of $\rho_{d o}$ (fig. 3, curve 2).

Both in low-resistance and high-resistance crystals light characteristic of IIPC (dependence $\Delta i_{\text {пф }}$ on $\Phi_{\mathrm{i}}$ ) has power-low character ( $\Delta i_{i p c} \sim \Phi_{i}^{\alpha}$ ). And value of $\alpha$,
besides $\Phi_{i}$ appears dependent also on $\rho_{d o}$ (fig. 4, curve 1-5).

Dependence of value ( $\Delta i_{i p c}$ ) induced by electric field impurity photoconductivity (IIIPC) on the external electric voltage applied to the sample $\left(U_{i}\right)$ has nonmonotonic character: at small $U_{i}$ it increases and at higher values of $U_{i}$ decreases with increasing voltage (fig. 5). However a steepness of $\Delta i_{n \phi}\left(U_{i}\right)$ curves and their inflection point appreciably depend on $\rho_{d o}$.

For comparison on the same sample also spectral distribution of the negative photoconductivity, induced impurity photoconductivity and IR-quenching of intrinsic photoconductivity (fig. 6) were measured.


Fig. 2. IIPC kinetics in $p-G a S e$ crystals under various excitation levels $(1,2)$ and probing light intensity $(1,3,4)$. $\mathrm{T}=77 \mathrm{~K} ; \lambda_{c}=0.58 \mu m ; \lambda_{I}=$ $1.60 \mu m ; \rho_{d o}=10^{8} \Omega \cdot \mathrm{~cm} ; U=5 \mathrm{~V} ; \Phi_{\text {int }}$, rel. units: 1 , 3, 4-0.1; 2-0.8; $\Phi_{\text {imp }}$, rel. units: 1, 2-0.2; 30.4; 4 - 0.8


Fig. 3. Dependence of $\Delta i_{\text {ipc }}$ value on initial specific dark resistance of the sample (curve 1) and temperature (curve 2) in $p-G a S e$ crystals. $T, K: 1-77$; $\Phi_{\text {int }}=0.8$ rel. units; $\Phi_{\text {imp }}=0.8$ rel. units; $\lambda_{c}=0.58 \mu m$; $\lambda_{\text {imp }}=1.60 \mu \mathrm{~m} ; \rho_{d o}, \Omega \cdot \mathrm{~cm}: 2-2 \cdot 10^{9}$


Fig. 4. Light dependence of IIPC in $p-G a S e$ crystals with various initial specific dark resistance $\left(\rho_{d o}\right) . T=77 \mathrm{~K} ; \Phi_{\text {int }}=0.8$ rel. units; $\lambda_{c}=0.58 \mu \mathrm{~m}$; $\lambda_{i m p}=1.60 \mu m ; U=5 \mathrm{~V} ; \rho_{d o}, \Omega \mathrm{~cm}: 1-10^{3} ; 2-10^{8}$; $3-2 \cdot 10^{6} ; 4-5 \cdot 10^{7} ; 5-2 \cdot 10^{9}$


Fig. 5.Dependence of ИIIPC ( $\Delta i_{\text {пф }}$ ) on external electric voltage $\left(U_{i}\right)$ in $p-G a S e$ crystals. $T=77 \mathrm{~K}$ : $\lambda_{\text {imp }}=1.60 \mu \mathrm{~m} ; \Phi_{\text {int }}=0.8$ rel.units; $\rho_{d o} \Omega \cdot \mathrm{~cm}: 1-10^{3}$; $2-10^{6} ; 3-5 \cdot 10^{7} ; 4-10^{8} ; 5-2 \cdot 10^{9}$

## 4. DISCUSSION

The experimental measurements carried out by us show that from the point of view of existing scientific conceptions on IIPC in semiconductors [5], in highresistance $p-G a S e$ crystals this photoelectric
phenomenon exhibits a number of anomalies. In particular, unlike specified in [5] with which are well correlated received by us results for low-resistance -$p-G a S e$ crystals, in high-resistance crystals at low temperatures and low excitation levels a position of the maximum and long-wave limit of IIPC spectrum depend on excitation level and $\rho_{d o}$ value; kinetics of IIPC has slow relaxing character - it is observed residual IIPC, its value ( $\Delta i_{\text {rc }}$ ) and relaxation time ( $\tau_{r c}$ ) which depend on excitation level of and $\rho_{d o}$; in an initial part of light characteristic of IIPC the superlinear branch of dependence $\Delta i_{\phi}\left(\Phi_{n}\right)$, which exponent depending on excitation level and $\rho_{T O}$ changes within $2 \div 5$; dependence $\Delta i_{i p c}\left(U_{i}\right)$ has non-monotonic character ( $\Delta i_{i p c}$ - at small $U_{i}$ increases, and at higher $U_{i}$ decreases with external voltage applied to the sample).


Fig. 6.Spectral distribution of negative photoconductivity (curve 1), induced impurity photoconductivity (curve 2) and IR-quenching of intrinsic photoconductivity (curve 3 ) in $p-G a S e$ crystals. $T=77 \mathrm{~K} ; \Phi_{\text {int }}=0.8$ rel. units; $\lambda_{\text {int }}=0.58$ $\mu m ; \lambda_{i m p}=0.8 \mu \mathrm{~m} ; \rho_{d o}=5 \cdot 10^{7} \Omega \cdot \mathrm{~cm}$.

The value of parameters characterizing all these anomalies with growth of alloying level of $p-G a S e$ crystal with Gd atoms also changes non-monotonically. In particular, with growth of alloying level $\left(N_{G d}\right)$ they at first (to $N_{G d} \approx 10^{-4}$ ат. \%) increase and further decreasing at last, at $N_{G d} \geq 10^{-2}$ ат. \%, almost absolutely disappear.

The comparative analysis of the received experimental results taking into account information existing in the scientific literature on electronic properties of $p-G a S e$ crystals and scientific concepts on IPF mechanism in semiconductors at all, allows to tell following about IPF mechanism in semiconductors.

As it is established elsewhere [1-4] in the forbidden band of $p-G a S e$ single crystals exist various recombination centers (slow and fast [9]), there are also trapping levels (capture levels with various depth energy $-\varepsilon_{\mathrm{t}}$ ). At effect on these crystals external factors generating non-equilibrium charge carriers (light from fundamental absorption region or injecting external electric voltage) a part of the created non-equilibrium charge carriers at low temperatures (at $k T<\varepsilon_{t}$ ) are captured by these trapping levels. As a result of the last, non-equilibrium filled trapping levels become as though "active" impurity centers which can be emptying under the influence of stronger external energy field (for example, at switching effect [9]), and under action of impurity (probing) light with quantum energy $\varepsilon_{t} \leq h v_{\mathrm{i}}<\varepsilon_{\mathrm{g}}$, where $\varepsilon_{g}$ width of the forbidden band of the considered semiconductor material. In the latter case it is observed IIPC which value is defined by density $\left(N_{t}\right)$ and degree of filling of trapping levels, and a spectrum - by their energy depth $\left(\varepsilon_{t}\right)$. According to put forward elsewhere [5] fundamental conceptions on IIPC, herein its light characteristic (dependence $\Delta i_{n \phi}$ on $\Phi_{i}$ ) should consist of an initial linear, subsequent sub-linear and finishing saturation part. According to these considerations herein duration of decay process of IIPC after switching off probing light should be defined by lifetime of the charge carriers released under the effect of probing light from trapping levels. In quasi-homogeneous semiconductors it usually equals to $\tau \leq 10^{-6} s$, i.e. thus the long-term (or residual) relaxation of IIPC should not take place. As to dependence $\Delta i_{i p c}\left(U_{i}\right)$, it should consist of an initial linear, subsequent sub-linear and final saturation branch. Actually, in low-resistance $p-G a S e$ crystals under all external conditions considered by us, excitation levels and temperatures these criteria are almost fulfilled. However in the low temperatures range at weak excitations, as has already been mentioned in the beginning of the present section, experimentally absolutely other situations are observed. The resume of the works done to date on electronic properties of highresistance $p-G a S e$ crystals allows to tell that highresistance $p-G a S e$ single crystals may be described satisfactorily on the basis of two-barrier energy model of partially-disorder semiconductor [10], according to which they as a whole consist of low-resistance matrixes (LRR), but with chaotic high-resistance inclusions (HRR). Besides, in the forbidden band of these crystals exist shallow $(\alpha)$ and deep ( $\beta$ ) trapping levels, as well as fast
$(S)$ and slow ( $r$ ) recombination centers [1-4]. And all these local levels are distributed on volume of the studied sample non-uniformly: $\alpha$-levels and $S$-centers predominantly are localized in LRR, while $\beta$-levels and r centers possess higher density in HRR. In LRR-HRR boundaries recombination barriers exist and in the allowed energy bands between adjacent HRR drift barriers exist. Under conditions considered by us IIPC is created mainly owing to excitation of quasi-equilibrium charge carriers captured by $\beta$-levels. Therefore it is not excluded also creation of IIPC owing to facilitated tunneling of charge carriers through recombination barriers. With growth of excitation level and with rise of the temperature light (or electric) and temperature smoothing of the potential relief occurs [11]. Therefore IIPC component facilitated by tunneling is weakened. Last in turn leads to displacement of the maximum and long-wave limit of spectrum for IIPC to shorter wavelengths with growth of excitation level and increasing of the temperature. Residual IIPC also is caused with presence of recombination barriers. Presence of drift barriers, in our opinion, connects sharper than linear dependence $\Delta i_{i p c}\left(\Phi_{n}\right)$ in an initial branch of light characteristic of IIPC, and also rather high value of $\Delta i_{i p c}$, than taking place in low-resistance crystals. Thus besides excess concentration of the photocarriers generated under the influence of probing light, in creation of IIPC the appreciable role plays also growth of the charge carriers mobility owing to deleting of drift barriers.

Within the limits of the offered model a falling part of $\Delta i_{i p c}$ versus ( $U_{i}$ ) curves can will be explained by a partial emptying $\beta$-levels owing to their tunnel breakdown at the voltage close to switching voltage [9] in this material.

Effect of the alloying with gadolinium atoms on characteristics of IIPC in $p-G a S$ crystals, most likely is caused by corresponding dependence of disorder degree of investigated samples on level of alloying with rare-earth element [12].

## 5. CONCLUSION

Thus, it is possible to conclude that the found out anomalies of induced impurity photoconductivity in highresistance $p-G a S e$ crystals, first of all are caused by partial disorder of these crystals and predominantly localization bearing direct responsibility for creation in IIPC trapping levels in chaotic high-resistance inclusions existing in them.
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# THE CALCULATION OF SPECTRAL CONSTANTS OF ISOBUTANOL MOLECULE ROTATIONAL ABSORPTION SPECTRUM 

G.I. ISMAILZADEH, I.Z. MOVSUMOV, M.R. MENZELEYEV<br>H.M.Abdullayev Institute of Physics of Azerbaijan National Academy of Sciences Az-1143, 33 H.Javid av., Baku


#### Abstract

The semiempirical calculations of rotational constants of isobutyl alcohol $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCH}_{2} \mathrm{OH}$ expected isomeric forms have been provided on the base of model with rigid molecular skeleton structure. The conformations structures have been analyzed equations and calculation results are presented.


Keywords: isobutanol, rotational absorption spectrum,
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Methods of microwave (MW) gas spectroscopy allow us to have trustworthy information about structure of investigated substance at the molecular level. This information could be used as the basis for further macroscopic structures construction, study of the substance chemical and physical properties nature. Therefore, the investigations of molecular structure of such compounds class as alcohols and especially their monoatomic variety (alcanoles) by means of MW gas spectroscopy methods are possible to refer to the number of rather actual scientific problems. Particular interest here is attracted by the specificity of intramolecular motion dynamic, basically closed with presence of hydroxyl atomic groups, which are mainly responsible not only for the features of electrical properties of initial molecules, but also for the realization of intermolecular hydrogen bonds.

Isobutanol $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCH}_{2} \mathrm{OH}$ molecule is certainly one of the most perspective objects from the point of potential information value. At the same time its molecular system structure features (sufficient length of molecular chain, presence of two methyl groups etc) are the cause of quite complex MW absorption spectra liable to fine structure effects of different nature and corresponding difficulties of identification of different isomeric forms spectra. Thereupon the provision of direct experiments has been anticipated by adequate designtheoretical researches - the initial and basic part of total investigation complex.
It has to be apparent that for the purpose of preliminary estimation of total number and relative stability of expected isomeric forms the first required step is to provide the calculations of the potential function of the asymmetric atomic groups' internal rotation. At this stage there isn't necessity to implement precision but same time complex (even for the comparison of simple molecules) ab-initio calculations, considering that the use of the MW gas spectroscopy methods in the further experimental researches will provide appropriate information about molecular structure. In other words the most reasonable way for preliminary evaluation of isobutyl alcohol potential function of internal rotation is the provision of the less laborious semi empiric calculations based on
consideration of two types of intramolecular interactions [ 1 ]:

- Exchange interactions of electron clouds of the bonds adjacent to the internal rotation valence bond;
- Interactions of non-valence bonded atoms, which are realized in the process of asymmetric atomic groups of internal rotation (free interactions).

Besides that in the calculations for such class of molecular systems it is reasonable to take into consideration the ability of realization of electrostatic interactions experimentally founded and described in article [ 2 ] in the form of $\mathrm{OH} \cdots \mathrm{C}$ type hydrogen bonds.

Results of such semiempirical calculations model have showed availability of isobutanol in seven stable, energy-nonequivalent conformational conditions related to the mechanisms of simplex or duplex rotations of asymmetric atomic groups OH and $\mathrm{CH}_{2} \mathrm{OH}$ around axes of internal rotation coincided with valence bond $\mathrm{C}_{4}-\mathrm{O}(\psi)$ and $\mathrm{C}_{3}-\mathrm{C}_{4}(\varphi)$ directions respectively. It has been noted that realization of inversion T-g isomer with internal rotation angles $\varphi=0^{\circ}$ and $\psi= \pm 120^{\circ}$ is not confirmed by such type of calculations. This possibly related with effect of steric repulsion of hydroxyl hydrogen atom by hydrogen atoms of two nearby located methyl groups. Together with this, results of more precision ab-initio calculations, given in article [ 3 ] suppose availability of that isomeric form, so it has been taken into account in further theoretical investigation process (fig.1, table 1).

The rotational constant values ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ ) of all mentioned above isobutanol molecule isomeric forms together with some other parameters of their structure have been obtained as the result of conventional calculations, based on postulation of investigated molecular system skeleton rigidity in the process of intramolecular rotation of its asymmetric segments ( OH and $\mathrm{CH}_{2} \mathrm{OH}$ ). Taking into consideration this condition the universal equations for the determination of all atoms coordinates in adequate coordinate frames have been developed (table 2).

$T-T^{2}$

$T-I$


It ${ }^{*}$



G-I

$0-{ }^{\prime}$

$0 \cdot z^{-1}$


9-7.

Fiq.1. Isobutanol molecule \& its isomeric forms

Table 1.
Isobutyl alcohol $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCH}_{2} \mathrm{OH}$ isomeric forms

| № | Conformer | $\varphi$ | $\psi$ |
| :---: | :---: | :---: | :---: |
| 1 | T-t | 0 | 0 |
| 2 | T-g | 0 | $\pm 120^{\circ}$ |
| 3 | T-g' | 0 | $\pm 30^{\circ}$ |
| 4 | G-t | $120^{\circ}$ | $0^{\circ}$ |
| 5 | G-g | $120^{\circ}$ | $120^{\circ}$ |
| 6 | G-g' | $120^{\circ}$ | $-120^{\circ}$ |
| 7 | G-g' | $120^{\circ}$ | $30^{\circ}$ |
| 8 | G-g' ${ }^{\circ}$ | $120^{\circ}$ | $-30^{\circ}$ |

Universal equations for isobutyl alcohol molecule $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCH}_{2} \mathrm{OH}$ atoms coordinates determination

| $C_{1}$ | $X$ | $r_{(C-C)} \cdot \sin (\angle C C C) \cdot \cos \left(\psi+\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin (\angle C C C)}\right)\right)$ |
| :---: | :---: | :---: |
|  | $Y$ | $-_{r_{\text {(C-C) }}} \cdot \cos (\angle C C C)$ |
|  | Z | $r_{(C-C)} \cdot \sin (\angle C C C) \cdot \sin \left(\psi+\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin (\angle C C C)}\right)\right)$ |
| $C_{2}$ | $X$ | $r_{(C-C)} \cdot \sin (\angle C C O) \cdot \cos \left(\psi-\arcsin \left(\frac{\sin (\angle C C C 2)}{\sin (\angle C C C)}\right)\right)$ |
|  | $Y$ | $-r_{(C-C)} \cdot \cos (\angle C C C)$ |
|  | Z | $r_{(C-C)} \cdot \sin (\angle C C C) \cdot \sin \left(\psi-\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin (\angle C C C)}\right)\right)$ |
| $C_{3}$ | $X$ | 0 |
|  | $Y$ | 0 |
|  | Z | 0 |
| $C_{4}$ | $X$ | 0 |
|  | $Y$ | $-r_{\text {c-c }}$ |
|  | $Z$ | 0 |
| $O$ | $X$ | $r_{(C-O)} \cdot \sin (\angle C C O)$ |
|  | $Y$ | $-r_{(c-c)}+r_{(c-o)} \cdot \cos (\angle C C O)$ |
|  | $Z$ | 0 |
| $H_{l}$ | $X$ | $\sqrt{\left(X_{11}\right)^{2}+\left(X_{12}\right)^{2}} \times \cos \left(\psi+\arctan \left(\frac{X_{12}}{X_{11}}\right)\right),$ <br> where $\begin{aligned} & X_{11}=\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times \\ & \cos \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right) \\ & X_{12}=\binom{\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right)} \times \\ & \frac{\sin (\angle C C C / 2)}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)\right)} \end{aligned}$ |
|  | $Y$ | $\begin{aligned} & \left(\sqrt{\left.r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times\right. \\ & \left.\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right)\right) \times \\ & \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)\right)}\right)\right) \end{aligned}$ |
|  | Z | $\sqrt{\left(Z_{11}\right)^{2}+\left(Z_{12}\right)^{2}} \times \sin \left(\psi+\arctan \left(\frac{Z_{12}}{Z_{11}}\right)\right)$ <br> where $\begin{aligned} & Z_{11}=\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times \\ & \sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right) \\ & Z_{12}=\binom{\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right)} \times \\ & \frac{\sin (\angle C C C / 2)}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)\right)} \end{aligned}$ |
| $\mathrm{H}_{2}$ | $X$ | $\begin{gathered} \sqrt{\left(X_{21}\right)^{2}+\left(X_{22}\right)^{2}} \cdot \cos \left(\psi+\arctan \left(\frac{X_{22}}{X_{21}}\right)\right) \\ \text { where } \end{gathered}$ |


|  |  | $\begin{gathered} X_{21}=K \cdot \cos (\alpha+\beta) \\ X_{22}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2} \cdot \sin \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{(C-H H} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right)} \\ \left.\left.K=\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right.}\right)\right)^{2}+\left(r_{(C-H)} \cdot \sqrt{\sin ^{2}(\angle C C H)-\sin ^{2}(\angle H C H / 2)}\right)^{2} \\ \alpha=\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right) \\ \beta=\arctan \left(\frac{r_{(C-H)} \cdot \cdot \sqrt{\left.\sin ^{2}(L C C H)\right)-\sin ^{2}(\angle H C H / 2)}}{\left.r_{(C-C-C)}\right)-r_{(C-H)} \cdot \cos (\angle C C H)}\right) \end{gathered}$ |
| :---: | :---: | :---: |
|  | $Y$ | $\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{C C-H H} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right)$ |
|  | $Z$ | $\begin{gathered} \sqrt{\left(Z_{21}\right)^{2}+\left(Z_{22}\right)^{2}} \cdot \sin \left(\psi+\arctan \left(\frac{X_{22}}{X_{21}}\right)\right) \\ \text { where } \\ Z_{21}=K \cdot \cos (\alpha+\beta) \\ Z_{22}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
| $\mathrm{H}_{3}$ | $X$ | $\begin{gathered} \sqrt{\left(X_{31}\right)^{2}+\left(X_{32}\right)^{2}} \cdot \cos \left(\psi+\arctan \left(\frac{X_{32}}{X_{31}}\right)\right) \\ \text { where } \\ X_{31}=K \cdot \cos (\alpha+\beta) \\ X_{32}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
|  | $Y$ | $\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right.$ ) |
|  | $Z$ | $\begin{gathered} \sqrt{\left(Z_{31}\right)^{2}+\left(Z_{32}\right)^{2}} \cdot \sin \left(\psi+\arctan \left(\frac{Z_{32}}{Z_{31}}\right)\right) \\ \text { where } \\ Z_{31}=K \cdot \cos (\alpha+\beta) \\ Z_{32}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
| $\mathrm{H}_{4}$ | $X$ |  |


|  | $Y$ | $\begin{aligned} & \left(\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times\right. \\ & \left.\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right)\right) \\ & \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)\right)}\right)\right) \\ & \hline \end{aligned}$ |
| :---: | :---: | :---: |
|  | Z | $\begin{aligned} & \sqrt{\left(Z_{41}\right)^{2}+\left(Z_{42}\right)^{2}} \times \sin \left(\psi+\arctan \left(\frac{Z_{42}}{Z_{41}}\right)\right) \\ & \text { where } \\ & Z_{41}=\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times \\ & \sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right) \\ & Z_{42}=\left(\sqrt{\left(r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)\right)^{2}+\left(r_{(C-H)} \cdot \sin (\angle C C H)\right)^{2}} \times\right. \\ & \left.\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle C C H)}{r_{(C-C)}-r_{(C-H)} \cdot \cos (\angle C C H)}\right)\right)\right) \times \\ & \left(-\frac{\sin (\angle C C C / 2)}{\sin \left(\arccos \left(\sqrt{\cos ^{2}(\angle C C C / 2)-\left(\sin ^{2}(\angle C C C / 2)-\cos ^{2}(\angle C C C / 2)\right)^{2}}\right)\right)}\right) \end{aligned}$ |
| $H_{5}$ | $X$ | $\sqrt{\left(X_{51}\right)^{2}+\left(X_{52}\right)^{2}} \cdot \cos \left(\psi+\arctan \left(\frac{X_{52}}{X_{51}}\right)\right)$ <br> where $\begin{gathered} X_{51}=K \cdot \cos (\alpha+\beta) \\ X_{52}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(-\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
|  | $Y$ | $\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right.$ ( |
|  | Z | $\begin{gathered} \sqrt{\left(Z_{51}\right)^{2}+\left(Z_{52}\right)^{2}} \cdot \sin \left(\psi+\arctan \left(\frac{Z_{52}}{Z_{51}}\right)\right) \\ Z_{51}=K \cdot \cos (\alpha+\beta) \\ Z_{52}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(-\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
| $H_{6}$ | $X$ | $\begin{gathered} \sqrt{\left(X_{61}\right)^{2}+\left(X_{62}\right)^{2}} \cdot \cos \left(\psi+\arctan \left(\frac{X_{62}}{X_{61}}\right)\right) \\ \text { where } \\ X_{61}=K \cdot \cos (\alpha+\beta) \\ X_{62}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(-\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
|  | $Y$ | $\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \cos \left(\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right)$ |
|  | $Z$ | $\sqrt{\left(Z_{61}\right)^{2}+\left(Z_{62}\right)^{2}} \cdot \sin \left(\psi+\arctan \left(\frac{Z_{62}}{Z_{61}}\right)\right)$ <br> where $\begin{gathered} Z_{61}=K \cdot \cos (\alpha+\beta) \\ Z_{62}=\sqrt{(K \cdot \sin (\alpha+\beta))^{2}+\left(-r_{(C-H)} \cdot \sin (\angle H C H / 2)\right)^{2}} \cdot \sin \left(-\arcsin \left(\frac{\sin (\angle C C C / 2)}{\sin \alpha}\right)+\arctan \left(\frac{-r_{(C-H)} \cdot \sin (\angle H C H / 2)}{K \cdot \sin (\alpha+\beta)}\right)\right) \end{gathered}$ |
| $\mathrm{H}_{7}$ | $X$ | $-r_{(C-H)} \cdot \sin (\angle C C H \quad) \cdot \cos \psi$ |
|  | $Y$ | $-r_{(C-H)} \cdot \cos (\angle C C H)$ |
|  | Z | - $r_{(C-H)} \cdot \sin (\angle C C H \quad) \cdot \sin \psi$ |
| $H_{8}$ | $X$ | $-r_{(C-H)} \cdot \sqrt{\sin ^{2}(\angle C C H)-\sin ^{2}(\angle H C H \quad / 2)}$ |
|  | $Y$ | - $r_{(C-C)}+r_{(C-H)} \cdot \cos (\angle C C H)$ |


|  | Z | $r_{(C-H)} \cdot \sin (\angle H C H \quad / 2)$ |
| :---: | :---: | :---: |
| $\mathrm{H}_{9}$ | $X$ | $-r_{(C-H)} \cdot \sqrt{\sin ^{2}(\angle C C H \quad)-\sin ^{2}(\angle H C H \quad / 2)}$ |
|  | $Y$ | - $r_{(C-C)}+r_{(C-H)} \cdot \cos (\angle C C H)$ |
|  | $Z$ | $-^{(C-H)}{ }^{\text {an }}$ ( $\left.\angle H C H / 2\right)$ |
| $H_{10}$ | $X$ | $r_{(C-O)} \cdot \sin (\angle C C O)-r_{(O-H)} \cdot[\cos (\angle C O H) \cdot \sin (\angle C C O)-\sin (\angle \mathrm{COH}) \cdot \cos (\angle C C O) \cdot \cos \varphi]$ |
|  | Y | $-r_{(C-C)}+r_{(C-O)} \cdot \cos (\angle C C O)-r_{(O-H)} \cdot[\cos (\angle C O H) \cdot \cos (\angle C C O)+\sin (\angle C O H) \cdot \sin (\angle C C O) \cdot \cos \varphi]$ |
|  | Z | $r_{(O-H)} \cdot \sin (\angle C O H) \cdot \sin \varphi$ |

Table 3.
Rotational constants of isobutyl alcohol $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHCH}_{2} \mathrm{OH}$ molecule isomeric forms

| № | Conformer | A | B | C | $\Delta$ | $\chi$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | T-t | 6242.624620 | 3983.956018 | 3171.755311 | 48.48698812 | -0.4710288 |
| 2 | T-g | 6127.823330 | 4107.103513 | 3254.305320 | 50.24241774 | -0.40644312 |
| 3 | T-g’ | 6225.011060 | 3998.807669 | 3178.201711 | 48.56812657 | -0.46133423 |
| 4 | G-t | 7647.817790 | 3488.776538 | 2638.033515 | 19.37166809 | -0.6603674 |
| 5 | G-g | 7560.573110 | 3540.231101 | 2685.685045 | 21.42847912 | -0.64940895 |
| 6 | G-g’ | 7600.749230 | 3577.008260 | 2681.487695 | 19.31224439 | -0.6359126 |
| 7 | G-g’ | 7631.470217 | 3494.458987 | 2637.442032 | 19.23465968 | -0.65678329 |
| 8 | G-g’" | 7642.824724 | 3494.363588 | 2648.317504 | 19.92731945 | -0.66120939 |

The values of structural parameters, i.e. noted here length of valence bonds and values of the valence angles for methyl groups have been taken from article [ 4 ] as for isopropyl alcohol molecule, for the last part of molecular skeleton - from articles [5,6] as for n-propanol molecule. The values of rotational constants obtained by this way are presented in table 3.

This makes possible to calculate values of the frequencies of rotational transitions composing all supposed conformations MW absorption spectra. It has been noted, that the use of the simplified model with rigid skeleton without taking into account the influence of such intramolecular motion specific form as internal rotation of
methyl groups, hydroxyl inversion relatively to the isobutanol molecular frame symmetry plane, of course, limiting availability of precise information regarding of the values of fine structure spectral characteristics frequencies related to specified conformation spectral lines A-E doubling or inversional splitting of T-g' isomer spectra. Nevertheless with that presented in table 3 values of isobutanol molecule isomeric forms rotational constants are certainly interesting, first of all, from the point of their use as the start point in process of preliminary identification of microwave absorption spectra of isobutanol.
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# THE POLYMORPHOUS TRANSFORMATIONS IN $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathbf{T e}$ AND $\mathrm{Cu}_{1.75} \mathbf{C d}_{0.05} \mathbf{T e}$ CRYSTALS 

U.I. ALIYEV, U.G. ASADOV, A.G. BABAYEV, K.M. JAFAROV, F.G. MAGERRAMOVA, R.D. ALIYEVA<br>H.M.Abdullayev Institute of Physics of Azerbaijan National Academy of Sciences<br>AZ-1143, G.Javid av., 33, Baku<br>e-mail: yusifasadov @rambler.ru


#### Abstract

The existing polymorphous transformations in $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ and $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ crystals are registered by high-temperature X-ray method in temperature interval $290-1100 \mathrm{~K}$. The thermal expansion coefficients of each existing modification are calculated from temperature dependence of lattice parameters. The influence of partial substitution of Cu by Zn and Cd on phase formation, temperature and number of polymorphous transformations in $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}^{\text {and }} \mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ crystals is shown.


Keywords:crystal structure, phase transition, high temperature
PACS: 64.60-i

## INTRODUCTION

The crystal structure of $\mathrm{Cu}_{1.80} \mathrm{Te}$ non-stoichiometric composition is defined in [1-5] and it is shown that $\mathrm{Cu}_{1.80} \mathrm{Te}$ has the hexagonal structure with lattice parameters $a=2 a_{0}=8.37 \AA, c=3 c_{0}=21.60 \AA, \mathrm{Z}=24$, sp. gr. P 3 m 1 , density is $\rho_{\mathrm{x}}=7.45 \mathrm{gr} / \mathrm{cm}^{3}$ (here $a_{0}=4.246 \AA, \mathrm{c}_{0}=7.289$ $\AA, \mathrm{Z}=2$, sp. gr. $\mathrm{P} 6 / \mathrm{mmm}$, density is $\rho_{\mathrm{x}}=7.33 \mathrm{gr} / \mathrm{sm}^{3}$, so called Novotnov phase $\mathrm{Cu}_{2} \mathrm{Te}$ [6]) at room temperature.

At high temperature $\mathrm{Cu}_{1.80} \mathrm{Te}, \mathrm{ZnTe}$ and CdTe crystallize in HC structure with lattice parameters: $a=6.083 \AA\left(\mathrm{Cu}_{1.80} \mathrm{Te}\right) ; a=6.103 \AA(\mathrm{ZnTe})$ and $a=6.477 \AA$ (CdTe) $[2,8,11]$.

The analogy of structures, elementary cells and cation ion radiuses $\left(\mathrm{Cu}^{1+}-0.98, \mathrm{Cu}^{2+}-0.80, \mathrm{Zn}^{2+}-0.83, \mathrm{Cd}^{2+}-0.99\right)$ in $\mathrm{Cu}_{1.80} \mathrm{Te}, \mathrm{ZnTe}$ and CdTe gives the foundation that Cu atoms in $\mathrm{Cu}_{1.80} \mathrm{Te}$ can be isomorphically substituted by Zn and Cd and one can obtain the continuous series of mixed crystals.

The part of cuprum atoms are isomorphically substituted by Zn atoms and Cd in non-stoichiometric composition $\mathrm{Cu}_{1.80} \mathrm{Te}$, i.e. $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ and $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ with the aim of consider of their influence on $\mathrm{Cu}_{1.80} \mathrm{Te}$ structure, phase-formation, polymorphous transformation temperature. These problems are discussed on the given paper.

## EXPERIMENTAL PART

$\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ and $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ are synthesized separately and grown up by Bridgman method for solution of given tasks.

The samples are obtained from initial components ("electrolytic» cuprum, zinc and cadmium) in vacuumprocessed up to $10^{-3} \mathrm{~Pa}$ quartz ampoule with inner diameter 1 cm and length 10 cm .

The ampoule is put in the furnace so that its part is in the furnace band at air melting point ( 725 K ) during 3 h . Further, the furnace temperature is increased with velocity $50 \mathrm{~K} / \mathrm{h}$ up to 1450 K , i.e. higher $\mathrm{Cu}_{2} \mathrm{Te}$ melting point ( 1398 K ). The ampoule is cooled slowly up to 400 K after two-hour enduring at this temperature with cyclic vibration and it is annealed at this temperature during 300 hours with the aim of homogenization. After this the furnace with ampoules is cooled up to room temperature.

The X-ray analysis is carried out for establishment of one-phase obtained samples. From synthesized samples of $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ and $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ the powdergrams, the interplanar spacing calculations:
a) The powdergram calculations obtained from $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ shows that the composition at room temperature is two-phase one and consists of orthorhombic modification with lattice parameters $a=7.319 \AA=c_{0}$, $b=22.236 \AA=3 c_{0}, \quad c=36.458 \AA=5 c_{0} \quad$ and hexagonal of modifications with lattice parameters $a=8.374 \AA=2 a_{0}$, $c=21.598 \AA=3 c_{0}$ (table1). As it is shown in [2], the orthorhombic phase with such parameters is the superstructure in the relation to hexagonal phase $a_{0}=4.248 \AA, c_{0}=7.234 \AA$.
b) The powdergram calculations obtained from $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ also proves its two-phase composition (table 2) which consists of orthorhombic and hexagonal modification.

The experimentally found combination of Bridgman method and slowly cooling is used for obtaining of $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ and $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ single crystals. The synthesized polycrystalline substances are put into ampoules (specially prepared for Bridgman method). The ampoules vacuum-processed up to pressure $10^{-3} \mathrm{~Pa}$ with corresponding compositions are put into furnace the temperature of which is regulated with the help of thermoregulator. Further, the temperature is slowly increased up to composition melting. After three-hour enduring the ampoule temperature decrease with velocity $2 \mathrm{~mm} / \mathrm{h}$. In the third band of furnace having the constant temperature 350 K , the samples in the ampoule are annealed during four weeks.

It is important to note that single crystals in laboratory conditions are usually grown up from the melt or gas phase. The crystal grown task is difficult if these compounds in solid states can exist in more than one crystal structure in the dependence on temperature. As a rule, the crystals of high-temperature modifications are grown up from melts and polymorphous substance steams. The crystals of the all rest modifications are obtained from only cooling as a result of polymorphous transformation and the crystals of low-temperature modifications stay at room temperature. The single crystal modifications of this
modification depend mainly on density difference of matrix and daughter crystal: a) if matrix crystal density weakly differs from new modification density, i.e. $\rho_{\mathrm{I}} \geq \rho_{\text {II }}$ then transformation of single crystal - single crystal type
takes place; b) if $\rho_{\mathrm{I}} \gg \rho_{\text {II }}$ or $\rho_{\mathrm{I}} \ll \rho_{\text {II }}$ then transformation of single crystal - polycrystal type takes place. From such crystal it is impossible to obtain the single crystal by the method of polymorphous transformation.

Table 1. The powdergram calculation of $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ composition Radiation $\mathrm{CuK}_{\alpha}\left(\lambda_{\alpha}=1.5418 \AA\right)$, Ni is filter. Mode: $35 \mathrm{kV}, 10 \mathrm{~mA}$, exp. 16 h .

| $\mathrm{D}_{\text {exp. }}$. $\AA$ ) | $\mathrm{I} / \mathrm{I}_{0}$ | Orthorhombic |  | Hexagonal |  | Elementary cell parameters |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{D}_{\text {calc }}(\AA)$ | hkl | $\mathrm{D}_{\text {calc. }}(\AA)$ | hkl |  |
| 7.252 | 60 | - | - | 7.253 | 100 | Orthorhombic |
| 5.827 | 41 | 5.796 | 122 | - | - |  |
| 4.901 | 22 | 5.008 | 132 | - | - | $\mathrm{a}=7.319 \AA$ |
| 4.331 | 30 | - | - | 4.331 | 104 | $\mathrm{b}=22.236 \AA$ |
| 3.624 | 100 | 3.628 | 153,0.0.10 | 3.626 | 200 | $\mathrm{c}=36.458$ § |
| 3.371 | 100 | 3.370 | 155 | - | - | $\mathrm{Z}=104$ |
| 2.536 | 10 | 2.539 | 248 | 2.530 | 108 | sp.gr. Pnma |
| 2.407 | 20 | 2.404 | 312 | 2.402 | 301 | $\rho_{\mathrm{x}}=7.095 \mathrm{gr} / \mathrm{cm}^{3}$ |
| 2.148 | 10 | 2.151 | 308 | - | - |  |
| 2.132 | 63 | 2.135 | 351 | - | - |  |
| 2.067 | 31 | 2.065 | 338 | - | - |  |
| 1.981 | 100 | 1.977 | 357 | - | - | Hexagonal |
| 1.824 | 92 | 1.824 | 382, 411 | 1.823 | 315 |  |
| 1.543 | 14 | 1.544 | 468 | 1.542 | 319, 413 | $\mathrm{a}=8.374 \AA$ |
| 1.519 | 21 | 1.517 | 477 | 1.518 | 414 | $\mathrm{c}=21.598 \AA$ |
| 1.439 | 34 | 1.436 | 530 | 1.437 | 502, 0.0.15 | $\mathrm{Z}=24$ |
| 1.393 | 40 | 1.394 | 508 | 1.392 | 331 | sp.gr. P3m1 |
| 1.377 | 30 | 1.377 | 509 | 1.375 | 505 | $\rho_{\mathrm{x}}=7.347 \mathrm{gr} / \mathrm{cm}^{3}$ |
| 1.334 | 21 | 1.334 | 4.10 .9 | - | - |  |
| 1.241 | 10 | 1.241 | 595 | 1.241 | 509 |  |
| 1.170 | 11 | 1.171 | 653 | 1.172 | 3.3.10 |  |
| 1.139 | 32 | 1.139 | 670 | 1.135 | 524 |  |
| 1.074 | 13 | 1.077 | 696 | 1.079 | 609 |  |
| 1.031 | 51 | 1.031 | 725 | 1.031 | 532 |  |
| 0.964 | 11 | 0.965 | 779 | 0.967 | 538 |  |
| 0.930 | 11 | 0.931 | 7.10.7 | 0.928 | 540 |  |
| 0.878 | 24 | 0.878 | 872 | 0.878 | 548 |  |
| 0.856 | 32 | 0.856 | 893 | 0.854 | 639 |  |
| 0.815 | 39 | 0.813 | 900 | 0.815 | 731 |  |
| 0.794 | 41 | 0.794 | 962 | 0.795 | 468 |  |

The investigations at high temperatures are carried out on diffractometer ДРОН- $3 \mathrm{M}\left(\mathrm{CuK}_{\alpha}\right.$ is radiation, Ni is filter) with high-temperature installation УPBT-2000 in vacuum ( $10^{-2} \mathrm{~Pa}$ ).

The angular resolution is $\sim 0,1^{\circ}$. The regime of continuous scanning is used. In experiments the angle definition error doesn't exist $\Delta \theta= \pm 0,02^{\circ}$.
$\mathbf{C u}_{1.50} \underline{\mathbf{Z n}}_{0.30} \mathbf{T e}$. At room temperature (293K) the fixed 9 diffraction reflections in angle interval $10^{\circ} \leq 2 \theta \leq 100^{\circ}$ are indicated on the base of orthorhombic lattice parameters $a=7.319 \AA \simeq c_{0}, \quad b=22.236 \AA \simeq 3 c_{0}, \quad \mathrm{c}=36.458 \AA \simeq 5 \mathrm{c}_{0} \quad$ and hexagonal modification with lattice parameters $a=8.374$ $\AA \simeq 2 \mathrm{a}_{0}, \quad \mathrm{c}=21.598 \quad \AA \simeq 3 c_{0}, \quad$ i.e. $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te} \rightarrow(\mathrm{CuZn})_{1.80} \mathrm{Te}$ two-phase crystals (see table3). As it is mentioned in $[2,6]$ the orthorhombic modification is the hexagonal modification superstructure.

After diffractogram record at room temperature the furnace is switch on and the control records are made through each 100 K . The sample temperature before each record is supported during 40 minutes.

At these conditions up to 473 K the reflection number and their intensity fixed at room temperature stay constant. At temperature increase higher 473 K the diffraction
picture changes (table 3), i.e. the new diffraction reflections appear. Besides reflections (025) and (199), the rest ones can consider as components of split earlier existed diffraction reflections. The reflections from (113), (117) and (411) planes of hexagonal lattice correspondingly are also overlapped on (210), (257) and (458) reflections of orthorhombic one.

The diffraction reflections appearing at 473 K because of splitting disappear at 573 K and in previous angle interval 7 reflections are fixed. At 673 K the repeated splitting of some reflections belonging to both orthorhombic and hexagonal modifications. At 773 K besides reflections from orthorhombic and hexagonal modifications the four reflections from (111), (200), (220) and (311) belonging to lattice of high-temperature HCC modification with parameter $a=6,120 \AA$. The annealing at this temperature or heating continuation leads to total transformation of orthorhombic and hexagonal modification into HCC modification.

The calculation results of lattice parameters on diffractogram are graphically shown on fig. 1 where $a(T)$, $\mathrm{b}(\mathrm{T}), \mathrm{c}(\mathrm{T}), \mathrm{V}(\mathrm{T})$ and $\rho(\mathrm{T})$ орторомбической, $\mathrm{a}(\mathrm{T}), \mathrm{c}(\mathrm{T})$, $\mathrm{V}(\mathrm{T})$ and $\rho(\mathrm{T})$ hexagonal and $\mathrm{a}(\mathrm{T}), \mathrm{V}(\mathrm{T})$ and $\rho(\mathrm{T})$ ГЦК modifications.

Table 2. The powdergram calculation of $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ composition, Radiation $\mathrm{CuK}_{\alpha}\left(\lambda_{\alpha}=1.5418 \AA\right)$, Ni is filter. Mode: $35 \mathrm{kV}, 10 \mathrm{~mA}$, exp. 16 h .

| $\mathrm{D}_{\text {exp. }}(\AA)$ | $\mathrm{I} / \mathrm{I}_{0}$ | Orthorhombic |  | Hexagonal |  | Elementary cell parameters |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{D}_{\text {calc. }}(\AA)$ | hkl | $\mathrm{D}_{\text {calc. }}(\AA)$ | hkl |  |
| 7.049 | 35 | 7.049 | 024 | - | - | Orthorhombic |
| 3.957 | 60 | 3.954 | 136 | - | - |  |
| 3.708 | 30 | 3.708 | 060 | 3.711 | 405 | $\mathrm{a}=7.380 \AA$ |
| 3.581 | 100 | 3.578 | 146 | 3.574 | 201 | $\mathrm{b}=22.250 \AA$ |
| 3.222 | 40 | 3.222 | 156 | 3.221 | 106 | $\mathrm{c}=36.274 \AA$ |
| 2.627 | 30 | 2.627 | 176 | - | - | $\mathrm{Z}=104$ |
| 2.537 | 30 | 2.539 | 248 | 2.534 | 108 | sp.gr. Pnma |
| 2.453 | 20 | 2.452 | 087 | - | - | $\rho_{\mathrm{x}}=7.130 \mathrm{gr} / \mathrm{cm}^{3}$ |
| 2.394 | 60 | 2.394 | 271 | 2.397 | 009, 301 |  |
| 2.281 | 50 | 2.279 | 275 | 2.282 | 109 |  |
| 2.265 | 10 | 2.265 | 306 | 2.267 | 118 |  |
| 2.081 | 60 | 2.081 | 319 | 2.082 | 119 | Hexagonal |
| 1.999 | 25 | 1.998 | 0.10 .8 | 2.001 | 209 |  |
| 1.945 | 20 | 1.942 | 289 | 1.946 | 224 | $\mathrm{a}=8.370 \AA$ |
| 1.833 | 10 | 1.856 | 380, 400 | 1.856 | 2.0.10 | $\mathrm{c}=21.573 \AA$ |
| 1.802 | 60 | 1.803 | 421 | 1.805 | 219 | $\mathrm{Z}=24$ |
| 1.798 | 26 | 1.798 | 414 | 1.798 | 308, 0.0.12 | sp.gr. P3m1 |
| 1.587 | 70 | 1.587 | 3.10 .6 | 1.589 | 324 | $\rho_{\mathrm{x}}=7.437 \mathrm{gr} / \mathrm{cm}^{3}$ |
| 1.442 | 80 | 1.442 | 514 | 1.441 | 501 |  |
| 1.438 | 100 | - | - | 1.438 | 502, 0.0.15 |  |
| 1.339 | 20 | 1.338 | 565 | 1.341 | 506 |  |

As it is seen from fig. 1 a parameter of orthorhombic, $\underline{a}$ and $\underline{c}$ parameters of hexagonal and a parameter of HCC modification in the dependence on temperature increase linearly, but $\underline{b}$ parrameter of orthorhombic modification linearly increases up to 470 K , further decreases and beginning from 570 K linearly increases up to transformation temperature. The $\underline{c}$ parameter linearly decreases up to 470 K and at 570 K increases beginning from 570 K up to transformation temperature linearly
decreases. This is explained by redistribution of cautions and vacancies.

The thermal expansion coefficients (TEC) both orthorhombic, hexagonal and HCC modifications which are given in table 4, are calculated from temperature dependence of lattice parameters. As it is seen from the table, at all temperatures TEC along [001] $\alpha_{[001]}$ direction of orthorhombic modification is negative one , i.e. $\alpha_{[001]}<0$.

Table 3
Rentgenographic data for $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$, Radiation $\mathrm{CuK}_{\alpha}\left(\lambda_{\alpha}=1.5418 \AA\right), \mathrm{Ni}$ is filter, mode $35 \mathrm{kV}, 8 \mathrm{~mA}$, exp. 24 h .

| $\mathrm{T}_{\text {exp }} \mathrm{K}$ | $\theta$ | $\mathrm{I} / \mathrm{I}_{0}$ | $\mathrm{D}_{\text {exp. }}$. $\AA$ ( ${ }^{\text {a }}$ | Hexagonal |  | Orthorhombic |  | Elementary cell parameters |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\begin{gathered} \mathrm{D}_{\text {calc }}(\AA \\ ) \\ \hline \end{gathered}$ | hkl | $\mathrm{D}_{\text {calc }}(\AA)$ | hkl |  |
| 293 | $\begin{aligned} & 6^{\circ} 06^{\prime} \\ & 10^{\circ} 15^{\prime} \\ & 12^{\circ} 17^{\prime} \\ & 13^{\circ} 13^{\prime} \\ & 18^{\circ} 41^{\prime} \\ & 21^{\circ} 02^{\prime} \\ & 25^{\circ} 02^{\prime} \\ & 29^{\circ} 58^{\prime} \\ & 34^{\circ} 02^{\prime} \end{aligned}$ | 60 45 100 100 60 10 40 50 30 | $\begin{aligned} & \hline 7.252 \\ & 4.331 \\ & 3.624 \\ & 3.371 \\ & 2.407 \\ & 2.148 \\ & 1.820 \\ & 1.543 \\ & 1.377 \end{aligned}$ | $\begin{gathered} \hline 7.2528 \\ 4.331 \\ 3.6262 \\ - \\ 2.4024 \\ - \\ 1.8234 \\ 1.5415 \\ 1.3750 \end{gathered}$ | 100 104 200 - 301 - 315 319,413 505 | 3.6275 <br> 3.3703 <br> 2.4039 <br> 1.1508 <br> 1.8196 <br> 1.5437 <br> 1.3767 | $\begin{gathered} - \\ - \\ 153,0010 \\ 155 \\ 312 \\ 308 \\ 401 \\ 468 \\ 509 \end{gathered}$ | $\begin{gathered} \text { Hexagonal, } a=8.374 \AA, c=21.598 \AA \\ \text { sp.gr.P3m1, } Z=24, \rho_{\mathrm{x}}=7.347 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { Orthorhombic, } a=7.290 \AA, \\ b=22.325 \AA \\ c=36.244 \AA \text {, sp.gr. Pnma } \\ Z=104, \rho_{\mathrm{x}}=7.095 \mathrm{gr} / \mathrm{cm}^{3} \end{gathered}$ |
| 473 | $6^{\circ} 04^{\prime}$ $7^{\circ} 15^{\prime}$ $10^{\circ} 13^{\prime}$ $10^{\circ} 19^{\prime}$ $12^{\circ} 13^{\prime}$ $12^{\circ} 18^{\prime}$ $13^{\circ} 10^{\prime}$ $13^{\circ} 14^{\prime}$ $18^{\circ} 06^{\prime}$ $18^{\circ} 38^{\prime}$ $21^{\circ} 00^{\prime}$ $22^{\circ} 21^{\prime}$ $24^{\circ} 56^{\prime}$ $29^{\circ} 10^{\prime}$ $24^{\circ} 51^{\prime}$ $33^{\circ} 39^{\prime}$ | 70 10 45 30 100 100 70 30 40 30 40 20 15 15 20 50 | 7.293 6.109 4.346 4.304 3.647 3.619 3.384 3.366 2.481 2.412 2.151 2.027 1.829 1.582 1.549 1.379 | 7.2899 - 4.3454 - 3.6449 - - - 2.4824 2.4148 - - 1.8324 1.5865 1.5477 1.3817 | 100 <br> - <br> 104 <br> - <br> 200 <br> - <br> - <br> - <br> 117 <br> 301 <br> - <br> - <br> 315 <br> 411 <br> 319,413 <br> 505 | $\begin{gathered} 6.0982 \\ - \\ 4.3045 \\ 3.6466 \\ 3.6178 \\ 3.3822 \\ 3.3718 \\ 2.4861 \\ - \\ 2.1522 \\ 2.0271 \\ 1.8248 \\ 1.5887 \\ 1.5458 \\ 1.3791 \\ \hline \end{gathered}$ | - 025 - 142 153,0010 210 057 155 257 - 308 199 401 458 468 509 | $\begin{gathered} \text { Hexagonal, } \mathrm{a}=8.421 \AA \\ \mathrm{c}=21.642 \AA \\ \text { sp.gr. } P 3 \mathrm{~m} 1 \\ \mathrm{Z}=24 \\ \rho_{\mathrm{x}}=7.251 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { Orthorhombic, } \mathrm{a}=7.333 \AA \\ \mathrm{~b}=22.233 \AA \\ \mathrm{c}=36.244 \AA \\ \text { sp.gr. Pnma } \\ \mathrm{Z}=104 \\ \rho_{\mathrm{x}}=7.039 \mathrm{gr} / \mathrm{cm}^{3} \end{gathered}$ |


| 573 | $\begin{gathered} 6^{\circ} 04^{\prime} \\ 10^{\circ} 13^{\prime} \\ 12^{\circ} 18^{\prime} \\ 13^{\circ} 10^{\prime} \\ 18^{\circ} 06^{\prime} \\ 22^{\circ} 21^{\prime} \\ 24^{\circ} 56^{\prime} \end{gathered}$ | $\begin{gathered} 40 \\ 50 \\ 100 \\ 100 \\ 60 \\ 30 \\ 5 \end{gathered}$ | $\begin{aligned} & 7.335 \\ & 4.346 \\ & 3.668 \\ & 3.389 \\ & 2.488 \\ & 2.039 \\ & 1.832 \end{aligned}$ | $\begin{gathered} 7.3245 \\ 4.3454 \\ 3.6622 \\ - \\ 2.4920 \\ - \\ 1.8370 \end{gathered}$ | $\begin{gathered} 100 \\ 104 \\ 200 \\ - \\ 117 \\ - \\ 315 \end{gathered}$ | $\begin{gathered} - \\ - \\ 3.6675 \\ 3.3886 \\ - \\ 2.0295 \\ 1.8324 \end{gathered}$ | - - 0.0 .10 057 - 119 401 | $\begin{gathered} \text { Hexagonal, } a=8.471 \AA, c=21.567 \AA \\ \text { sp.gr.P3m1, } Z=24, \rho_{\mathrm{x}}=7.190 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { Orthorhombic, } a=7.362 \AA, \\ b=22.704 \AA \\ c=35.333 \AA \text {, sp.gr. Pnma } \\ Z=104, \rho_{\mathrm{x}}=7.087 \mathrm{gr} / \mathrm{cm}^{3} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 673 | $\begin{aligned} & 6^{\circ} 02^{\prime} \\ & 10^{\circ} 12^{\prime} \\ & 12^{\circ} 05^{\prime} \\ & 12^{\circ} 09^{\prime} \\ & 13^{\circ} 07^{\prime} \\ & 17^{\circ} 44^{\prime} \\ & 18^{\circ} 01^{\prime} \\ & 18^{\circ} 41^{\prime} \\ & 19^{\circ} 16^{\prime} \\ & 24^{\circ} 49^{\prime} \end{aligned}$ | $\begin{gathered} 40 \\ 20 \\ 100 \\ 40 \\ 100 \\ 20 \\ 20 \\ 20 \\ 30 \\ 40 \end{gathered}$ | $\begin{aligned} & 7.335 \\ & 4.353 \\ & 3.683 \\ & 3.662 \\ & 3.396 \\ & 2.531 \\ & 2.492 \\ & 2.471 \\ & 2.336 \\ & 1.836 \end{aligned}$ | $\begin{gathered} 7.3343 \\ 4.3528 \\ 3.6674 \\ 3.6517 \\ - \\ - \\ 2.4963 \\ - \\ - \\ 1.8410 \end{gathered}$ | $\begin{gathered} \hline 100 \\ 104 \\ 200 \\ 113 \\ - \\ - \\ 117 \\ - \\ - \\ 315 \\ \hline \end{gathered}$ | $\begin{gathered} - \\ - \\ 3.6674 \\ - \\ 3.3966 \\ 2.5321 \\ - \\ 2.4708 \\ 2.3383 \\ - \\ \hline \end{gathered}$ | $\begin{gathered} 153,0010 \\ - \\ 057 \\ 086 \\ - \\ 090 \\ 191 \end{gathered}$ | $\begin{gathered} \text { Hexagonal, } \mathrm{a}=8.506 \AA, \mathrm{c}=21.585 \AA \\ \text { sp.gr. } \mathrm{P} 3 \mathrm{ml} 1, \mathrm{Z}=24 \\ \rho_{\mathrm{x}}=7.125 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { Orthorhombic, } \mathrm{a}=7.699 \AA, \mathrm{~b}=22.473 \AA \\ \mathrm{c}=35.007 \AA, \mathrm{Z}=104 \\ \text { sp.gr. Pnma } \\ \rho_{\mathrm{x}}=6.910 \mathrm{gr} / \mathrm{cm}^{3} \end{gathered}$ |
| 773 | $\begin{aligned} & \hline 10^{\circ} 10^{\prime} \\ & 12^{\circ} 35^{\prime} \\ & 13^{\circ} 05^{\prime} \\ & 14^{\circ} 35^{\prime} \\ & 17^{\circ} 43^{\prime} \\ & 17^{\circ} 59^{\prime} \\ & 19^{\circ} 15^{\prime} \\ & 20^{\circ} 52^{\prime} \\ & 24^{\circ} 41^{\prime} \end{aligned}$ | $\begin{gathered} \hline 30 \\ 30 \\ 100 \\ 40 \\ 30 \\ 30 \\ 50 \\ 50 \\ 40 \end{gathered}$ | $\begin{aligned} & \hline 4.368 \\ & 3.534 \\ & 3.405 \\ & 3.062 \\ & 2.533 \\ & 2.497 \\ & 2.338 \\ & 2.164 \\ & 1.841 \end{aligned}$ | 4.3677 3.5337 - 3.0602 2.5334 2.5046 - 2.1639 1.8453 | 104 $(111)^{*}$ - $(200)^{*}$ 108 117 - $(220)^{*}$ $315(311)^{*}$ | $\begin{gathered} - \\ - \\ 3.4050 \\ - \\ 2.5337 \\ - \\ 2.3382 \\ - \\ 1.8429 \end{gathered}$ | $\begin{gathered} - \\ - \\ 057 \\ - \\ 086 \\ - \\ 191 \\ - \\ 401 \end{gathered}$ | $\begin{gathered} \text { Hexagonal, } \mathrm{a}=8.616 \AA, \mathrm{c}=21.547 \AA \\ \text { sp.gr. P3m1, } \mathrm{Z}=24 \\ \rho_{\mathrm{x}}=6.956 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { Orthorhombic, } \mathrm{a}=7.423 \AA, \mathrm{~b}=22.222 \AA \\ \mathrm{c}=37.088 \AA, \mathrm{Z}=104 \\ \text { Pnma, } \rho_{\mathrm{x}}=6.910 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { HCC: } \mathrm{a}=6.120 \AA \end{gathered}$ |
| 973 | $\begin{aligned} & 12^{\circ} 34^{\prime} \\ & 14^{\circ} 33^{\prime} \\ & 20^{\circ} 49^{\prime} \\ & 24^{\circ} 37^{\prime} \end{aligned}$ | $\begin{gathered} 100 \\ 40 \\ 60 \\ 80 \end{gathered}$ | $\begin{aligned} & 3.544 \\ & 3.070 \\ & 2.170 \\ & 2.851 \end{aligned}$ | $\begin{aligned} & 3.5442 \\ & 3.0693 \\ & 2.0703 \\ & 1.8509 \end{aligned}$ | $\begin{aligned} & 111 \\ & 200 \\ & 220 \\ & 311 \end{aligned}$ |  |  | $\begin{gathered} \mathrm{Z}=4, \text { пр.гр.Fm3m } \\ \rho_{\mathrm{x}}=7.005 \mathrm{gr} / \mathrm{cm}^{3} \\ \text { HCC: } \mathrm{a}=6.139 \AA, \mathrm{Z}=4 \\ \mathrm{Fm} 3 \mathrm{~m}, \rho_{\mathrm{x}}=6.943 \mathrm{gr} / \mathrm{cm}^{3} \end{gathered}$ |

Table 4. Thermal expansion of $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}\left(* 10^{-6} \mathrm{grad}^{-1}\right)$ modification.

| Modification | $\mathrm{T}_{\text {exp }}$, K | $\alpha_{[100]}$ | $\alpha_{[010]}$ | $\alpha_{[001]}$ | $\bar{\alpha}=\frac{\alpha_{[100]}+\alpha_{[010]}+\alpha_{[001]}}{3}$ | $\bar{\beta}=\alpha_{[100]}+\alpha_{[010]}+\alpha_{[001]}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Orthorhombic | 293-373 | 70.302 | 121.485 | -353.734 | -53.982 | -65,33 |
|  | 373-473 | 2.728 | 120.761 | -206.976 | -27.829 | -72,32 |
|  | 473-573 | 39.547 | -26.858 | 136.806 | 49.832 | 4,88 |
|  | 573-673 | 52.975 | 40.175 | -40.573 | 17.526 | 18,01 |
|  | 673-773 | 29.726 | 5.567 | -26.876 | 2.806 | 25,78 |
| Hexagonal | 293-373 | 32.855 |  | 2.316 | 22.675 | 67,27 |
|  | 373-473 | 26.215 |  | 1.389 | 17.940 | 59,22 |
|  | 473-573 | 30.901 |  | 16.667 | 26.156 | 66,30 |
|  | 573-673 | 3.555 |  | 1.387 | 2.832 | 51,04 |
|  | 673-773 | 21.319 |  | 0.924 | 14.521 | 49,98 |
| HCC | 773-873 | 16.340 |  |  | 16.340 | 49.020 |
|  | 873-973 | 14.682 |  |  | 14.682 | 44.046 |
|  | 973-1073 | 14.660 |  |  | 14.660 | 43.980 |

$\mathbf{C u}_{1.75} \underline{\mathbf{C d}}_{0.05} \mathbf{T e}$. At room temperature in angle interval $10^{\circ} \leq 2 \theta \leq 80$ ten diffraction reflections from $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ crystal which as powdergrams (table 2) are indicated on the base of elementary cell parameters of orthorhombic and hexagonal modifications identically to $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ crystal (table 5), are fixed. Note that some reflections especially most intensive ones indicate on the base of elementary sell parameters of $\mathrm{Cu}_{1.80} \mathrm{Te}$ hexagonal modification, i.e. the reflections from (009), (0.0.12) and (0.0.15) planes of hexagonal lattice overlap on reflections from (094), (414) and (530) planes of orthorhombic one. The diffraction picture fixed at room temperature stays constant up to 573 K . At 573 K the splitting of three most
intensive reflections (009), (0012) and (0015) and at 673 K the splitting totally ends. Moreover, the insensitivities of (414) orthorhombic and (0012) hexagonal modifications become less ones than reflection intensivities from (413) plane of orthorhombic and new (004) modifications which appear at splitting. The diffraction reflections from (003), (004) and (005) planes appearing as a result of reflection splitting from (009), (0012) and (0015) planes belong to new hexagonal modification with lattice parameters $a=4.20 \AA, c=7.26 \AA$ close to parameter values of Novotnov hexagonal phase for stoichiometric composition $\mathrm{Cu}_{2} \mathrm{Te}$. At $761 \pm 1 \mathrm{~K}$ both splitted reflections and ones belonging to first hexagonal modification disappear. In previous angle
interval only five reflections belonging to orthorhombic modification are fixed and reflections from (311) and (222) planes belonging to high-temperature HCC modification overlap on (289) and (3010) reflections. At
$833 \pm 2 \mathrm{~K}$ all reflections from orthorhombic modification totally disappear and in previous angle interval only reflections from (311) и (222) planes of cubic modification with lattice parameter $\mathrm{a}=6.727 \AA$ stay.

Table 5.
The diffractogram calculation of $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ crystal at different temperatures Radiation $\mathrm{CuK}_{a}\left(\lambda_{a}=1.5418 \AA\right)$, Ni is filter, mode $35 \mathrm{kV}, 10 \mathrm{~mA}$.

| $\mathrm{T}_{\text {exp }}, \mathrm{K}$ | $\mathrm{D}_{\exp }(\AA)$ | I/ $/{ }_{0}$ | Orthorhombic |  | Hexagonal |  | Elementary cell parameters |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\mathrm{D}_{\text {calc }}(\AA)$ | hkl | $\mathrm{D}_{\text {calc }}(\AA)$ | hkl |  |
| 290 | 2.627 | 30 | 2.627 | 176 | - |  | Orthorhombic, $\mathrm{a}=7.330 \AA, \mathrm{~b}=22.250 \AA$ |
|  | 2.453 | 20 | 2.452 | 087 | - |  | $\mathrm{c}=36.274 \AA$, sp.gr. Pnma |
|  | 2.397 | 50 | 2.395 | 094 | 2.397 | 009 | $\mathrm{Z}=104, \rho_{\mathrm{x}}=7.130 \mathrm{gr} / \mathrm{cm}^{3}$ |
|  | 2.265 | 10 | 2.265 | 306 | 2.267 | 118 |  |
|  | 2.081 | 20 | 2.081 | 319 | 2.080 | 119 | Hexagonal-I, |
|  | 1.994 | 30 | 1.994 | 3.2.10 | 2.000 | 209 | $\mathrm{a}=8.370 \AA$ |
|  | 1.833 | 10 | 1.856 | 380,400 | 1.855 | 2.0.10 | $\mathrm{c}=21.573 \AA$ |
|  | 1.798 | 30 | 1.797 | 414 | 1.798 | 0.0.12,402 | sp.gr.P3m1, $\mathrm{Z}=24$, |
|  | 1.587 | 70 | 1.587 | 3.10 .6 | 1.589 | 324 | $\rho_{\mathrm{x}}=7.437 \mathrm{gr} / \mathrm{cm}^{3}$ |
|  | 1.438 | 100 | 1.438 | 530 | 1.438 | 0.0.15,502 |  |
| 673 | 2.642 | 10 | 2.641 | 176 | - | - | Orthombic, $\mathrm{a}=7.369 \AA$ |
|  | 2.464 | 10 | 2.463 | 087 | - | - | $\mathrm{b}=22.417 \AA$ |
|  | 2.425 | 30 | 2.425 | 258 | 2.425 | $(003)_{1}$ | $\mathrm{c}=36.179 \AA$ |
|  | 2.408 | 80 | 2.402 | 094 | 2.408 | 009 | sp.gr. Pnma |
|  | 2.087 | 20 | 2.087 | 319 | 2.083 | 119 | $\mathrm{Z}=104, \rho_{\mathrm{x}}=7.058 \mathrm{gr} / \mathrm{cm}^{3}$ |
|  | 2.000 | 20 | 2.000 | 3.2.10 | 2.002 | 209 | Hexagonal-I, |
|  | 1.944 | 10 | 1.943 | 366 | - | - | $\mathrm{a}=8.412 \AA$ |
|  | 1.868 | 10 | 1.869 | 368 | 1.856 | 2.0.10 | $\mathrm{c}=21.701 \AA$ |
|  | 1.848 | 10 | 1.847 | 380,400 | - | - | sp.gr. $\mathrm{P} 3 \mathrm{ml}, \mathrm{Z}=24$, |
|  | 1.819 | 100 | 1.815 | 413 | 1.819 | (004) ${ }_{1}$ | $\rho_{\mathrm{x}}=7.319 \mathrm{gr} / \mathrm{cm}^{3}$ |
|  | 1.806 | 50 | 1.800 | 414 | 1.806 | 0.0.12,402 | Hexagonal-II, |
|  | 1.597 | 20 | 1.597 | 3.10 .6 | 1.596 | 324 | $a=4.237 \AA$ |
|  | 1.455 | 30 | 1.455 | 504 | 1.455 | (005) ${ }_{1}$ | $\mathrm{c}=7.275 \AA$ |
|  | 1.445 | 90 | 1.446 | 530 | 1.445 | 0.0.15,502 |  |
| 773 | 2.330 | 20 | 2.330 | 267 | - | - | Orthorhombic |
|  | 2.110 | 10 | 2.112 | 328 | - | - | $\mathrm{a}=7.423 \AA, \mathrm{~b}=22.857 \AA$ |
|  | 2.028 | 20 | 2.028 | 3.0.10 | 2.028 | (311)* | $\mathrm{c}=35.253 \AA$, sp.gr. Pnma |
|  | 1.942 | 100 | 1.942 | 289 | 1.942 | (222)* | $\mathrm{Z}=104, \rho_{\mathrm{x}}=6.997 \mathrm{gr} / \mathrm{cm}^{3}$ |
|  | 1.429 | 10 | 1.429 | 496 | - | - | HCC: $\mathrm{a}=6.727 \AA, \mathrm{Z}=4$ |
|  |  |  |  |  |  |  | sp.gr. Fm3m, $\rho_{\mathrm{x}}=5.329 \mathrm{gr} / \mathrm{cm}^{3}$ |
| 873 | 2.030 | 10 | 2.029 | 311 |  |  | HCC: $\mathrm{a}=6.734 \AA, \mathrm{Z}=4$ |
|  | 1.944 | 100 | 1.944 | 222 |  |  | sp.gr. Fm3m, $\rho_{\mathrm{x}}=5.313 \mathrm{gr} / \mathrm{cm}^{3}$ |

*     - reflections from HCC modification

Table 6.
Thermal expansion of $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}\left({ }^{*} 10^{-6} \mathrm{grad}^{-1}\right)$ modification.

| Modification | $\mathrm{T}_{\text {exp }}, \mathrm{K}$ | $\alpha_{[100]}$ | $\alpha_{[010]}$ | $\alpha_{[001]}$ | $\bar{\alpha}=\frac{\alpha_{[100]+} \alpha_{[010]+} \alpha_{[001]}}{3}$ | $\bar{\beta}=\alpha_{[100]}+\alpha_{[010]}+\alpha_{[001]}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Orthorhombic | 290-373 | 23.603 | 15.593 | -6.975 | 10.740 | 32.221 |
|  | 373-473 | 5.448 | 15.266 | -3.586 | 5.709 | 17.128 |
|  | 473-573 | 24.503 | 25.106 | -14.349 | 11.753 | 35.260 |
|  | 573-673 | 6.790 | 25.044 | -2.487 | 9.782 | 29.347 |
|  | 673-773 | -67.851 | -74.050 | 96.188 | -15.238 | -45.713 |
|  | 773-833 | -84.256 | -35.504 | 71.637 | -16.041 | -48.123 |
| Hexagonal | 290-373 | 17.273 |  | 16.180 | 16.909 | 50.726 |
|  | 373-473 | 13.123 |  | 14.351 | 13.532 | 40.597 |
|  | 473-573 | 9.532 |  | 18.491 | 12.518 | 37.555 |
|  | 573-673 | 13.094 |  | 13.381 | 13.190 | 39.569 |
|  | 673-773 | 22.587 |  | 18.893 | 21.356 | 64.067 |
| HCC | 833-873 | 94.838 |  |  | 94.838 | 284.514 |
|  | 873-973 | 9.859 |  |  | 9.859 | 29.577 |

The graphically temperature dependences of crystal lattice parameters, atomic volume and densities of $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ modifications are given on fig.2. As it is seen from fig. $2 \underline{a}$ and $\underline{c}$ parameters of hexagonal modification in the dependence on temperature linearly increase and $\underline{a}$ и $\underline{b}$ parameters of orthorhombic modification in temperature interval 293-673K also linearly increase and higher this temperature strongly decrease, $\underline{c}$ parameter up to 673 K linearly decrease and higher this temperature strongly increases up to transformation into cubic modification.


Fig.1.Temperature dependence of elementary cell parameters of hexagonal, orthorhombic and HCC of $\mathrm{Cu}_{1.50} \mathrm{Zn}_{0.30} \mathrm{Te}$ modification: are $\underline{\text { a }}$ and $\underline{\mathrm{c}}$, volume $V$ and density $\rho$ of hexagonal modification; $\odot$ are $\underline{a}, \underline{b}$ and $\mathcal{c}$, volume $V$ and density $\rho$ of orthorhombic modification; $\bullet$ are $\underline{a}$ parameter, $V$ is volume and $\rho$ density of HCC modification

From temperature dependence of lattice parameters of existing modifications TEC are calculated by main crystallographic directions which are given in table 6 . The strongly anisotropy on main crystallographic directions of orthorhombic modification is connected with weakening of
covalent (short) bonds at increased temperature and their irregular position in crystal lattice.


Fig.2.Temperature dependence of elementary cell parameters of hexagonal, orthorhombic and HCC $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05}$ Te modifications: $\odot$ are $\underline{a}$ and $\underline{c}$ parameters, V volume and density $\rho$ of hexagonal modification; are $\underline{a}, \underline{b}$ и $\underline{c}$ parameters, $V$ volume and density $\rho$ of orthorombic one; $\boldsymbol{\bullet}$ are $\underline{a}$ parameter, $V$ is volume and $\rho$ density of HCC modification

The Novotnov hexagonal modification forming at 673 K also essentially influences on parameter values of $\mathrm{Cu}_{1.75} \mathrm{Cd}_{0.05} \mathrm{Te}$ orthorhombic modification. The anomaly in temperature dependence of crystal lattice of orthorhombic modification is observed with formation of this modification.
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# THE THERMAL CONDUCTIVITY OF $(\mathbf{P b S})_{1-x}\left(\operatorname{Sm}_{2} \mathbf{S}_{3}\right)_{x}(x=0 \div 0.04)$ SOLID SOLUTIONS 

G.A. GASANOV, E.G. JAFAROV, U.S. NAMAZOV<br>of Azerbaijan Republic Academy o Ministry of NationalSecurity named by Heydar Aliyeva AZ-1029,A.Gayibov str.,6, Baku, Azerbaijan Republic, hummat.hasanov@gmail.com

The temperature dependences (in $170 \div 670 \mathrm{~K}$ interval) of $\lambda$ thermal conductivity of $(P b S)_{1-x}\left(S_{2} S_{3}\right)_{x} \quad(0-4 \mathrm{~mol} . \%$ $\operatorname{Sm}_{2} S_{3}$ ) solid solutions are obtained. The isotherms of $\lambda_{l}$ lattice thermal conductivity $\lambda_{l}$ are constructed on the base of these data and the effective cross section of phonon scattering on $S m$ impurity atoms is estimated. The region of $\lambda_{l}$ anomalous growth is revealed in the region of $1.25-2.0 \mathrm{~mol} . \% \mathrm{Sm}_{2} S_{3}$ concentrations not corresponding with usually observed decrease of $\lambda_{l}$ at increase impurity concentration. It is supposed that anomalous growth of $\lambda_{l}$ begins to take place when in the crystal the continuous chain of overlapping deformative fields formed by separate atoms forms; the partial compensation of strengths in crystal lattice takes place and phonon dispersion decreases. The universal character of revealed effect is supposed.

Keywords: thermal conductivity, isotherm, solid solution
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## INTRODUCTION

The compounds of $A^{I V} B^{V I}$ type and solid solutions on their base belong to the number of well known semiconductor materials which are wide used in IRtechniques, thermoelectricity, tensometry and etc [1,2]. In these solid solutions the concentration anomalies of properties [3,4] the presence of which is connected with critic phenomena having the percolation nature and belonging to any solid solution [5], are observed in the series of the given solid solutions in the impurity small concentration region by us.

The solid solutions on $P b S$ base in $(\mathrm{PbS})_{1-\mathrm{x}}\left(\mathrm{Sm}_{2} \mathrm{~S}_{3}\right)_{x}(x=0 \div 0.04)$ base crystallizing in the structure by NaCl type are the object of the present investigation [6]. The anomalies on the concentration dependences of Hall coefficients, electric conduction and thermal expansion coefficient near $\sim 1 \mathrm{~mol} . \% \mathrm{Sm}_{2} \mathrm{~S}_{3}$ are observed in these solid solutions [6].

The investigation of temperature dependences of $\lambda$ thermal conductivity and construction of isotherms on their base are the aims of the present work.

## THE EXPERIMENT TECHNIQUE

The $(P b S)_{1-x}\left(\mathrm{Sm}_{2} S_{3}\right)_{x}\left(0-4 \mathrm{~mol} \% \quad \mathrm{Sm}_{2} S_{3}\right)$ alloys are prepared by ampoule method from elements of high purity and are endured by homogenization annealing at 900 K during 200 h . The two series of alloys with the similar composition set are prepared at the synthesis for exclusion of accidental errors. $\lambda$ measurement is carried out by the method of dynamic calorimeter in the mode of monotone heat [ 3 ] in $170 \div 670 \mathrm{~K}$ temperature interval on cylinder samples by $1,5 \mathrm{~cm}$ diameter and $0,5 \mathrm{~cm}$ height. The samples are prepared by hot pressure method at temperature 770 K and pressure $4000 \mathrm{~kg} / \mathrm{cm}^{2}$, annealed during 200 h at 900 K and cooled in the air. After the given
treatment the region of solid solutions on $P b S$ base is $\sim 3$ mol. \% about which the results of microstructure investigation, parameter precision measurement and microhardness one prove. The temperature dependences $\lambda$ for all samples are obtained. $\lambda$ measurement is carried out on each sample not less than 3 times and the results are averaged. The curve shift $\lambda$ (T)from measurement to another one on the same sample usually doesn't exceed $\sim 5 \%$ and is explained by some nonidentity at sample positioning in the device which takes place. The absence of $\lambda(\mathrm{T})$ curve systematic shift fact at repeat processes of heat-cooling during the measurements evidences about unimportance of the thermocycling influence on $\lambda$ value and on enough sample degree of homogeneity achieved at thermal treatment. The resultant dependence $\lambda(\mathrm{T})$ for each from the compositions is constructed by the way of data averaging obtained for first and second alloy series. The electric conduction $\sigma$ is measured by four-probe method with the delicacy not less than $\sim 5 \%$. The assignment of electronic thermal conductivity component $\lambda_{e}$ is carried out by Videman Frantz law; $\lambda_{e}=L \sigma T$. The Lorentz number $L$ is defined by the formula which is right for degenerated semiconductors, $\mathrm{L}=(\mathrm{r}+2)\left(\mathrm{k}_{0} / \mathrm{e}\right)^{2}(r$ is degree coefficient in the dependence on free length on energy $\lambda=\varepsilon^{\prime}$ ) [7] in supposition of carrier dominated scattering on acoustic lattice oscillations ( $\mathrm{r}=0.1$ ).

## THE RESULTS AND DISCUSSION

The dependences $\lambda(T)$ for samples of the different compositions are given on fig.1. The clearly expressed minimum at $\sim 400 \div 450 \mathrm{~K}$ on all curves takes place.

It is known that heat transfer in semiconductors in general case can be carried out by crystal lattice oscillations, electronic gas, electromagnetic radiation and also by bipolar diffusion of charge carriers [4.5]. That's why the expression for calculation of total thermal conductivity $\lambda$ can be written in the form:

$$
\begin{equation*}
\lambda=\lambda_{l}+\lambda_{e}+\lambda_{p h}+\lambda_{b} \tag{1}
\end{equation*}
$$

where $\lambda_{l}, \lambda_{e}, \lambda_{p h}, \lambda_{b}$ are lattice, photon and bipolar components of $\lambda$ correspondingly. The growth $\lambda$ after $400 \div 450 \mathrm{~K}$ can be caused by increase of electron transfer, however, the estimation of electron component shows that $\lambda_{e}$ makes the unimportant contribution into total thermal conductivity (not more than 7\%) and can't provide the extremal character of $\lambda(\mathrm{T})$ dependences. That's why one can suppose that the bipolar diffusion of charge carriers caused by appearance of intrinsic conductivity takes place as $P b S$ [8]. The fact that intrinsic conductivity is observed at enough low temperatures is connected with complex structure of valency band of $p-P b S$ the parameters of which essentially depend on temperature.


Fig.1. The temperature dependences of thermal conductivity in solid solutions $(P b S)_{1-x}\left(\operatorname{Sm}_{2} S_{3}\right)_{x} . \operatorname{Sm}_{2} S_{3}$ (in mol.\%) concentration: $1-0,2-0.75,3-1.25,4-1.75,5-$ 2.0, 6-4.0.

According to many works $[4,5]$ the valency band of lead chalcogenides consists of two overlapping subbands with different state density divided by energy gap $\Delta E$, decreases with temperature growth and becomes equal to zero at $450 \div 500 \mathrm{~K}$. The further temperature growth leads to the fact that subbands of "easy" and "heavy" holes change places. The impurity $\mathrm{Sm}_{2} S_{3}$ introduction leads to increase of forbidden band width, but the valency band structure PbS and $(\mathrm{PbS})_{1-x}\left(\mathrm{Sm}_{2} \mathrm{~S}_{3}\right)_{x}$ solid solutions stay identical ones [7].

The heat transfer by electromagnetic radiation is significant in that case when the absorptivity in the region of heat radiation is mall one $[8,10]$. As the absorption
coefficient of $P b S$ is big enough ( $\alpha \approx 200 \mathrm{~cm}^{-1}$ ) and in $(\mathrm{PbS})_{1-x}\left(\mathrm{Sm}_{2} \mathrm{~S}_{3}\right)_{x}$ alloys $\alpha$ value exceed by a factor of ten [8], the heat transfer by electromagnetic radiation can be ignored. The estimation of photon thermal conductivity shows that in whole temperature interval contribution of $\lambda_{p h}$ in total conductivity doesn't exceed $0,5 \%$.

Taking under consideration the insignificant contribution $\lambda_{e}$ and $\lambda_{p h}$ in total alloy thermal conductivity $(\mathrm{PbS})_{1-x}\left(\mathrm{Sm}_{2} \mathrm{~S}_{3}\right)_{x}$ can be expressed by the sum of lattice and bipolar components $\lambda=\lambda_{l}+\lambda_{b}$. The temperature dependences of thermal resistance calculated by taking under consideration lattice and bipolar components: $W_{\text {exp }}=1 /\left(\lambda_{l}+\lambda_{b}\right)$. In temperature interval $170 \div 400 \mathrm{~K}$ the linear growth $W_{\text {exp }}$ is observed and at temperatures higher $\sim 400 \mathrm{~K}$ the thermal resistance decreases.

It is known [4] that at $T \geq \Theta(\Theta$ is Debye temperature) the phonon mean free path is limited by interphonon interaction of phonons with lattice defects. At taking under consideration only three-phonon processes and scattering on defects in the correspondence with Debye-Payerls theory the lattice thermal resistance can be expressed in the following form:

$$
\begin{equation*}
W_{\pi}=1 / \lambda_{l}=A T+B, \tag{2}
\end{equation*}
$$

where $A$ is coefficient taking under consideration the oscillation anharmonicity degree of crystal lattice and $B$ defines the additional thermal resistance caused by the lattice defects. Extrapolating the linear part of $W_{\text {exp }}(T)$ to high temperatures (dotted line on Fig.2), one can define the contribution of bipolar component of thermal conductivity by distance between dotted line and experimental curve:

$$
\lambda_{b}=1 / W_{\text {exp }}-1 / W_{r}
$$

The estimations made with correspondence with them show that the contribution of bipolar component is big one and at temperature $\sim 670 \mathrm{~K}$ achieves $\sim 60 \%$ of total thermal conductivity.

The concentration dependences $\lambda_{l}$ (before beginning of carrier bipolar diffusion) and ( $\lambda_{l}+\lambda_{b}$ ) (after beginning of carrier bipolar diffusion) are constructed on the base of $\alpha$ and $\sigma$ temperature dependences (Fig.3). From this picture it is seen that dependences have the clearly expressed nonmonotonic character: on all curves in concentration interval $1.25-2.0 \mathrm{~mol} . \% \mathrm{Sm}_{2} \mathrm{~S}_{3}$ the region of anomalous growth of lattice conductivity takes place.

Usually $\lambda_{l}$ decreases because of phonon scattering on impurity atoms with growth of impurity concentration in solid solution region. In limits Klemens theory $\lambda_{l}$ decrease in region of slid solutions is defined by the mass difference and lattice main and impurity atoms, difference
of bond forces in neighborhood impurity atom and also by elastic stress caused by difference of atom sizes [6]. In the investigated system $\lambda_{l}$ decrease is observed in the regions of 0-1.25 and $2.0-4 \mathrm{~mol} . \% \mathrm{Sm}_{2} \mathrm{~S}_{3}$ compositions.


Fig.2. The temperature dependences of thermal resistance in $(P b S)_{1-x}\left(\mathrm{Sm}_{2} S_{3}\right)_{x}$ solid solutions. The concentration $\mathrm{Sm}_{2} S_{3}$ (in mol.\%): $1-0,2-0.75,3-1.25,4-1.75,5-$ 2.0, 6-4.0.

The anomalous growth $\lambda_{l}$ in intermediate concentration interval we connect with critical phenomena of percolation type taking place in crystal impurity subsystem [3].

The impurity atoms are centers of local lattice distortions, sources of internal stress and deformations decreasing inversely to distance in third degree [7]. As the atom marked shifts form on length equal to one-two atom distances, the elastic deformation field can be considered as short-range one and can use the conception of character radius of deformation interaction $R_{0}$. At small impurity concentration when the distance between them is much bigger than $R_{0}$ the deformation fields formed by separate atoms aren't practically overlapping and make the additive contribution in lattice thermal resistance increasing it.

As impurity concentration increases, the overlapping of elastic fields of neighbor atoms leading to partial compensation of elastic stress of opposite sign takes place. In short-range approximation supposing the distribution statistic character of impurity atoms by means of the percolation theory [8] using $R_{0}$ values one can estimate the concentration $x_{c}$ (percolation threshold) at which the collective interaction corresponding to formation of unit chain of overlapping deformation fields going through whole crystal (so-called "infinitive cluster"), begins. We can solve the inverse task: by the value of critic concentration $x_{c}$ we can define $R_{0}$ radius. Considering that $x_{c}$ corresponds to $\sim 1.25 \mathrm{~mol} . \% \mathrm{Sm}_{2} S_{3}$ we obtain $R_{0} \approx(1 / 2) \cdot \alpha_{0} \quad\left(\alpha_{0}\right.$ is elementary cell
parameter) that corresponds with short-range character of deformation interaction. The transition from dissolved solid solutions to concentration ones when the continuous cluster forms should be accompanied by critic phenomena, analogical phase transitions of second order [2]. As the partial compensation of opposite sign stress leading to decrease of general level of elastic lattice stress corresponds to percolation channel formation, one can suppose that this leads to increase of lattice thermal conductivity.


Fig.3. The isotherms of lattice thermal conductivity in $(\mathrm{PbS})_{1-x}\left(\mathrm{Sm}_{2} \mathrm{~S}_{3}\right)_{x}$. Т,К: 1-170, 2-220, 3-295, 4420, 5-570, 6-670 solid solutions.

The growth $\lambda_{l}$ in anomalous region is connected with increase of infinitive cluster density. After that as compensation process of elastic stress catches the whole crystal and whole volume is filled by "impurity liquid", the further impurity atom introduction leads to new lattice distortions and therefore to decrease of lattice thermal conductivity. The situation can be analogical to Mott transition when percolation channel formation on electron membranes of separate atoms leads to appearance of electric conductivity (metal-dielectric transition). In considered case the percolation channels form by deformation fields of separate impurity atoms. At critic concentrations the probability of impurity atom ordering processes strongly increases. The simple calculation shows that composition $\sim 1.0 \mathrm{~mol} . \% \mathrm{Sm}_{2} \mathrm{~S}_{3}$ is the optimal one for ordered distribution of impurity atoms over nodes of primitive cubic lattice with period $\alpha=3 \alpha_{0}$, but at $\sim 1.6 \mathrm{~mol} . \% \mathrm{Sm}_{2} S_{3}$ the formation of superstructure with HCC -lattice of impurity atoms is possible and with period $\alpha=4 \alpha_{0}$ ( $\alpha_{0}$ is alloy elementary cell parameter). The significant growth $\lambda_{l}$ in $\lambda_{l}$ interval can directly show on the presence of order processes.

The nonsignificant contribution of electronic component of thermal conductivity in the investigated alloys doesn't allow us to connect the observable concentration anomalies $\lambda_{l}$ with change of Lorentz number which can takes place at strong doping as a result of electron-electron interaction [9].

By concentration dependence $\lambda$ in
$0-1.25 \mathrm{~mol} . \% \mathrm{Sm}_{2} S_{3}$ region the estimation of effective phonon cross sections on Sm impurity atoms with the use of Yoffe formula [4] is made:

$$
\begin{equation*}
\frac{\lambda}{\lambda_{0}}=1+\Phi \frac{N}{N_{0}} \cdot \frac{l_{0}}{d}, \tag{3}
\end{equation*}
$$

where $\lambda_{0}$ and $\lambda$ are crystal thermal conductivity coefficients without impurities, $N$ and $N_{o}$ are number
of impurity and all atoms in volume unit correspondingly. $d$ is distance between atoms, $l_{0}$ is average phonon free path introducing into expression for thermal conductivity coefficient of non-doped crystal; $\lambda_{0}=1_{0} \mathrm{C}_{\mathrm{V}} \nu_{\mathrm{g}} / 3$ (where $C_{V}$ is volumetric heat capacity and $\nu_{g}$ is average group velocity, $\Phi$ is coefficient introducing into expression for effective cross section of $S=\Phi \cdot d^{2}$ phonon scattering. Substituting the values $\lambda_{0}, \lambda, N, N_{0}$ and also $C_{V}$ and $\nu_{g}$ in (3) we obtain that $\Phi=1.9$ and $S=1.9 d^{2}=0.48 a_{0}^{2}$ at 300 K. The obtained $S$ shows that the impurity atoms aren't the centers of phonon effective scattering in solid solutions under consideration.
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# LUMINESCENT PROPERTIES OF YbGa $\mathbf{S}_{4}:$ Er $^{3+}$ SINGLE CRYSTALS 

B.G. TAGIYEV ${ }^{1,2}$, O.B. TAGIYEV ${ }^{1,3}$, F.A. KAZIMOVA ${ }^{1}$, U.F. KASUMOV ${ }^{1}$<br>${ }^{1}$ Institute of Physics of ANAS<br>AZ 1143, H.Javid ave., 33,<br>${ }^{2}$ National Space Academy, Bina, Baku, Az1045, 25 kilometer<br>${ }^{3}$ Branch of Moscow State University named by M.V.Lomonosov in Baku<br>E-mail:oktay@physics.ab.az

The photoluminescent properties of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}$ crystal at excitation by emission with $\lambda=337,1 \mathrm{~nm}$ and $\lambda=976 \mathrm{~nm}$ in the dependence on temperature. The samples are obtained with the help of solid-state reaction. The mechanisms of Stokes and anti-Stokes luminescence of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}$ crystals are defined.

Keywords: photoluminescence, rare-earth element, kinetics, anti-Stokes luminescence. PACS: 76.30, 78.55

## INTRODUCTION

The process-dependent parameters of the growth of triple earth chalcogenide semiconductors by $\mathrm{Sr}(\mathrm{Eu}, \mathrm{Yb}, \mathrm{Sm}, \mathrm{Ca}, \mathrm{Ba}) \mathrm{Ga}(\mathrm{Al})_{2} \mathrm{~S}(\mathrm{Se}, \mathrm{O})_{4}$ type and also of doping by rare-earth elements define their emissive properties. One can change the transformation efficiency of different energy types into light one and luminescence color of these compounds by the selection of corresponding sensitizers and activators. The oriented optimization, i.e. the improvement of obtaining technology of new luminescent materials perspective for the formation of luminophors with the special properties allowing their usage for emission visualization beyond visible range of spectrum and lighting, is possible on the vase of establishment of feedback between growth and doping parameters of these materials with their structural, optical, luminescent and laser properties [1,2,3,4].

The mode is developed and 10 representatives of triple chalcogenides of $\mathrm{A}^{\mathrm{II}} \mathrm{B}^{\mathrm{III}}{ }_{2} \mathrm{C}_{4}{ }^{\mathrm{VI}}$ type including $\mathrm{YbGa}_{2} \mathrm{~S}_{4}$ are obtained in [5]. The oriented crystallization and annealing with slow temperature decrease (5degree/h) are applied for single crystal obtaining. The crystal structure parameters have the values $a=20,112 ; b=20,082$ and $c=12,132 \AA$. The obtained compounds are treated by micro-structural, X-ray-phase, thermographic analyses and microhardness measurement. The detail thermographic investigation and chemical analysis of the compounds show that they are individual phases having the character melting points regularly decreasing from gallium-containing compounds up to indium-containing ones, and also from europium-containing up to ytterbiumcontaining ones. The investigation results of photoluminescence spectrum of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}$ :Er crystal at different temperatures and luminescence kinetics are given in present paper.

## THE SAMPLE OBTAINING AND THE EXPERIMENT

$\mathrm{YbGa}_{2} \mathrm{~S}_{4}$ samples are obtained from double YbS and $\mathrm{Ga}_{2} \mathrm{~S}_{3}$ compounds by the way of solid-state reaction in graphite crucible covered by activated carbon. Er doping is carried out by $\mathrm{ErF}_{3}$ use in synthesis process. The
powder after drying is treated by $\mathrm{H}_{2} \mathrm{~S}$ stream at $900^{\circ} \mathrm{C}$ during 4 hours. X-ray analysis of the powder shows that all samples well crystallize, in particular, after treatment. It is proved that treatment improves the crystallization and solubility of $\mathrm{Er}^{3+}$ ions.

The impulse diode laser is used for excitation at 976 nm . The light radiated by the sample, is collected by optical fiber situated perpendicular to sample surface on distance 10 mm and is analyzed by HR460 Yobin-Ybon spectrometer and multi-channel detectors Spectramax and TRIAX 320 Hamamutsu PDA into visible and IR regions correspondingly.

## THE RESULTS AND DISCUSSION

The photoluminescence spectrum of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}$ crystal at $\lambda_{e x}=337,1 \mathrm{~nm}$ in temperature interval $78-300 \mathrm{~K}$ is shown on fig.1. The spectrum consists of three parts of emissive transitions. The first region is wave length interval $550-650 \mathrm{~nm}$ (is connected with $f$-d transition of $\mathrm{Yb}^{2+}$ ion $[6,7]$ ), second region is in interval $800-870 \mathrm{~nm}$ and the third one is in interval $870-950 \mathrm{~nm}$. These narrowband emissions are connected with transitions ${ }^{4} I_{9 / 2} \rightarrow{ }^{4} I_{15 / 2}$ and ${ }^{4} I_{11 / 2} \rightarrow{ }^{4} I_{15 / 2}$ of $\mathrm{Er}^{3+}$ ions [8]. We observe also emission of $\mathrm{Er}^{3+}$ ion with $I_{13 / 2} \rightarrow^{4} I_{15 / 2}$ transition in IR spectrum region (1480-1600nm) (fig.2) [8].


Fig.1. The luminescence spectrum of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}$ crystal at temperature different values.


Fig.2. The luminescence spectrum of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}$ crystal in IR region at $\lambda_{\text {exc }}=337.1 \mathrm{~nm}$ and $\mathrm{T}=300 \mathrm{~K}$.


Fig. 3. The temperature dependences of PhL intensity for maxima $595 \mathrm{~nm}-1$ and $900 \mathrm{~nm}-2$.


Fig. 4. Time dependences of $\mathrm{Er}^{3+}$ ion emission lines at 595 nm of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}$ crystal at different temperatures.

The activation energies of luminescence centers 009 and $0,07 \mathrm{eV}$ responsible for emission 595 and 900 nm correspondingly are defined from temperature dependence of intensity (fig.3). The kinetics of emission
maximum at 595 nm at different temperatures is presented on fig.4. At 78 K the emission kinetics in interval $0-20 \mu \mathrm{~s}$ has hyperbolic character with the following transition on exponential regularity. This can be connected with two different states for $\mathrm{Yb}^{2+}$ ion $[9,10]$. The life time decreases with temperature growth (fig.5).


Fig. 5. The dependence of life time on temperature.


Fig.6. The spectrum of anti-Stokes emission of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}\left(\lambda_{\mathrm{ex}}=976 \mathrm{~nm}\right.$ and $\left.\mathrm{T}=300 \mathrm{~K}\right)$.


Fig.7. The energy scheme of anti-Stokes luminescence in $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}^{3+}\left(\lambda_{\mathrm{ex}}=976 \mathrm{~nm}\right.$ and $\left.\mathrm{T}=300 \mathrm{~K}\right)$.

The study of $\mathrm{Er}^{3+}$ ion at $\lambda_{\text {max }}=1560 n m$ gives the possibility of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}$ crystal usage in the capacity of active mediums for lasers emitting in the region 1530 nm . The principle of operation of optical divisors using REE in the capacity of active material bases on the following fact. During preparation the base material is doped by rare-earth elements. Their ions form the active medium of wave length of special bands corresponding to absorption bands of doping material. The impurity ions can be excited by emission of laser pumping of corresponding wave length and further, they can relatively easily drop the excited electrons on low level in relaxation process. This process can't correspond to two-level model of interaction taken under consideration as the main one, such process goes with phonon emission and without it. In first case the phonons are formed (transition energy causes the environment oscillations). In second case the phonon excitation takes place.

Moreover, the transition from excited level to relaxation one carries out through intermediate metastable level caused by upper laser level. Thus, interaction model becomes the three-level one. In any case, for the normal interaction the photon energy in signal flow should be equal to difference of excited level energy and relaxation one.

Last time the materials where there are towards ytterbium ( Yb ) and erbium (Er) ions are applied for emission amplification at 1550 nm . Er ions have absorption peaks in region of wave length 532, 660, 808, $980,1480 \mathrm{~nm}$. From this it is followed that known laser types with wave lengths 800,980 and 1480 nm can serve as pumping source. The three-level interaction models of interaction correspond to 800 and 980 nm and two-level model correspond to 1480 nm .

These lasers are used widely enough, taking under consideration (because of three-level interaction) very low noise level (3-5dB order).

However, lasers on 1480 nm though they are effective ones ( $70 \%$ from laser on 980 nm ), are considered the more preferable ones and can realize the low enough noise level ( 5 dB order). One can use the laser pumping diodes working on wave length 1053 nm at Yb ion use in the capacity of component. Their use allows us the obtaining the more pumping source.
The anti-Stokes emission (fig.6) is revealed at excitation of $\mathrm{YbGa}_{2} \mathrm{~S}_{4}: \mathrm{Er}[11]$ compound by emission of wave length 976 nm . We suppose the following mechanism of antiStokes emission (fig.7). The photon absorption with wave length 976 nm leads to ${ }^{2} F_{7 / 2} \rightarrow{ }^{2} F_{5 / 2}$ electron transition in $\mathrm{Yb}^{3+}$ ion. The migration of excitation energy on crystal one can lead to the excitation energy transfer from ${ }^{2} \mathrm{~F}_{5 / 2}$ level of $\mathrm{Yb}^{3+}$ ion on near energy level $4 \mathrm{I} 11_{/ 2}$ of excited state of $\mathrm{Er}^{3+}$ ion. The absorption of second photon leads to ${ }^{4} I_{11 / 2} \rightarrow{ }^{2} F_{7 / 2}$ transition in $\mathrm{Er}^{3+}$ ion and moreover, the energy transition from $\mathrm{Yb}^{3+}$ also takes place. The corresponding emitting transitions into main state $\left({ }^{2} H_{11 / 2} \rightarrow{ }^{4} I_{15 / 2},{ }^{4} S_{3 / 2} \rightarrow{ }^{4} I_{15 / 2},{ }^{4} F_{9 / 2} \rightarrow{ }^{4} I_{15 / 2}\right)$ take place after thermal relaxtion from ${ }^{2} F_{7 / 2}$ level to ${ }^{2} H_{11 / 2},{ }^{4} S_{3 / 2}$ and ${ }^{4} F_{9 / 2}$, levels and the emission at 520,540 and 650 nm is observed. The nature of this process is caused by realization of two acts of elementary excitations of the same $\mathrm{Er}^{3+}$ ion.

## CONCLUSION

The luminescent materials doped by $\mathrm{Er}^{3+}$ and having the emission at 1550 nm present the big interest for thin-film integral technology, standard telecommunication zona C ( $1530-1560 \mathrm{~nm}$ ). It is established that the consecutive excitation energy transfer from sensibilizator to emitting activator, i.e. the consecutive sensibilization is the mechanism of observable anti-Stokes emission.

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